

Measuring the growth of structure by matching dark matter haloes to galaxies with VIPERS and SDSS

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ABSTRACT

We test the history of structure formation from redshift 1 to today by matching galaxies from the VIMOS Public Extragalactic Redshift Survey (VIPERS) and Sloan Digital Sky Survey (SDSS) with dark matter haloes in the MultiDark, Small MultiDark Planck (SMDPL), N -body simulation. We first show that the standard subhalo abundance matching (SHAM) recipe implemented with MultiDark fits the clustering of galaxies well both at redshift 0 for SDSS and at redshift 1 for VIPERS. This is an important validation of the SHAM model at high redshift. We then remap the simulation time steps to test alternative growth histories and infer the growth index $\gamma = 0.6 \pm 0.3$. This analysis demonstrates the power of using N -body simulations to forward model galaxy surveys for cosmological inference. The data products and code necessary to reproduce the results of this analysis are available online (<https://github.com/darklight-cosmology/vipers-sham>).

Key words: galaxies: statistics – cosmology: observations – large-scale structure of Universe.

1 INTRODUCTION

The growth of structure over cosmic time is a fundamental observable that informs us about the expansion history and the physics of gravitational instability, both of which are key ingredients for interpreting cosmic acceleration (e.g. Huterer et al. 2015). Surveys that map the distribution of galaxies out to high redshift provide important measurements of the statistics of the matter field and its evolution. In the standard paradigm galaxies form inside massive dark matter clumps, and these clumps build up hierarchically (White & Frenk 1991). The formation of dark matter structures and their spatial statistics have been well investigated analytically and in N -body simulations (e.g. Bardeen et al. 1986; Springel et al. 2005).

However, the connection between the galaxies detected in surveys and the underlying matter distribution is complex (Baugh 2013; Wechsler & Tinker 2018). Observations show that the two-point clustering statistics depend strongly on the luminosity, colour, morphology, and other physical properties of the galaxy sample

(Davis & Geller 1976; Giovanelli, Haynes & Chincarini 1986; Guzzo et al. 1997; Norberg et al. 2002; Zehavi et al. 2005; Pollo et al. 2006; Marulli et al. 2013; Cappi et al. 2015; Di Porto et al. 2016), since these properties are tied to the density environments the galaxies are found in (Blanton & Berlind 2007; Davidzon et al. 2016; Cucciati et al. 2017). These dependencies are encoded in the galaxy bias b_g that relates the two-point clustering statistics of the galaxies to that of the underlying matter on large scales: $\xi_g(r, z) = b_g(z)^2 \xi(r, z)$ (Kaiser 1984). It is the usual practice to parametrize the bias function and marginalize over these parameters in a cosmological analysis since they depend on the galaxy sample and the peculiarities of the survey selection function (Alam et al. 2017; Rota et al. 2017). Other approaches have been developed to infer the biasing function using statistics of the galaxy distribution. Di Porto et al. (2016) constrain the bias by matching the galaxy density distribution measured in a galaxy survey with the distribution of dark matter in an N -body simulation assuming a one-to-one correspondence. We will follow a similar approach in this analysis using dark matter haloes.

The process of matching the dark matter haloes in a simulation to the distribution of galaxies selected by luminosity or stellar mass in a survey known as subhalo abundance matching (SHAM) provides a

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simple yet accurate prediction of galaxy bias (Vale & Ostriker 2004; Conroy, Wechsler & Kravtsov 2006; Behroozi, Conroy & Wechsler 2010; Moster et al. 2010; Trujillo-Gomez et al. 2011). The method requires an N -body simulation with sufficient resolution to identify and follow the substructure within dark matter haloes (Guo & White 2014). Reddick et al. (2013) demonstrate that a single halo property is sufficient to assign galaxies and that the implicit choice of this property primarily affects the clustering on small scales below $1 h^{-1}$ Mpc. Stochasticity or scatter in the relationship between the halo mass and the galaxy luminosity has been shown to be less important when the galaxy sample is sufficiently deep such that it is complete down to the characteristic flattening of the luminosity function (or stellar mass function; Conroy et al. 2006; Reddick et al. 2013).

At low redshift, spectroscopic surveys including the Two-degree Field Galaxy Redshift Survey (2dFGRS), the Sloan Digital Sky Survey (SDSS) Main Galaxy Sample, and the Galaxy And Mass Assembly (GAMA) survey have appropriately broad and deep selection functions. At higher redshift, the VIMOS Public Extragalactic Redshift Survey (VIPERS; Guzzo et al. 2014; Scodregio et al. 2018) is unique with a cosmologically representative volume.

The accuracy of SHAM to model galaxy clustering over cosmic time was first demonstrated by Conroy et al. (2006) who compiled galaxy clustering measurements to $z \sim 5$. Conroy et al. (2006) developed a SHAM model to assign galaxy luminosities to haloes using the equivalent of the halo property V_{peak} that we define below. No additional free parameters such as stochasticity or scatter in the assignment were used. The success of Conroy et al. (2006) has motivated the development of the SHAM model that we adopt to describe the clustering of galaxies in SDSS and VIPERS.

The application of SHAM without free parameters is attractive for making cosmological predictions. For example, He et al. (2018) extended SHAM to modified gravity models and tested the validity of these models against the standard Λ cold dark matter (Λ CDM) scenario using galaxy clustering statistics. To extend this technique more generally to constrain cosmological parameters requires a large number of simulations that span a range of cosmological models (Harker, Cole & Jenkins 2007). However, a practical shortcut can be taken to avoid this computational expense. It has been shown that a simulation runs in one model can be made to quantitatively look like a simulation runs in a different model by rescaling the time and spatial dimensions to match the expansion and growth histories (Angulo & White 2010; Mead & Peacock 2014a,b; Mead et al. 2015; Zennaro et al. 2019). This approach was implemented in a cosmological analysis pipeline by Simha & Cole (2013).

We apply the rescaling algorithm here in a simplified context in which we vary only the growth history quantified by σ_8 , the variance of the linear matter field on $8 h^{-1}$ Mpc scales. In practice, modifying the evolution of $\sigma_8(z)$ in a simulation requires only relabelling the redshift of the outputs. Using the MultiDark N -body simulation (Klypin et al. 2016), we employ a parameter-free SHAM model to predict the galaxy correlation function and directly constrain $\sigma_8(z)$ using measurements at redshift $z < 0.106$ in SDSS and at redshift $0.5 < z < 1$ in VIPERS. Harker et al. (2007) made a similar analysis on SDSS that employed semi-analytic models for galaxy formation to predict the amplitude of galaxy clustering. Simha & Cole (2013) carried out a full cosmological analysis using SDSS making use of rescaled simulations and SHAM. We present the preliminary application of these techniques to higher redshift.

The growth history $\sigma_8(z)$ may be parametrized by the growth index γ as (Wang & Steinhardt 1998)

$$\sigma_8(z) = \sigma_8(0) \exp \left[- \int_0^z \Omega_m(z')^\gamma d \ln(1+z') \right]. \quad (1)$$

The growth index in the standard model is $\gamma = 0.55$. Other parametrizations have been proposed more recently (e.g. Silvestri, Pogosian & Buniy 2013); however, the use of the growth index neatly separates the dependence on the expansion history given by $\Omega_m(z)$ from modifications to the gravity model (Linder 2005; Guzzo et al. 2008; Moresco & Marulli 2017).

In this paper, we first present a validation of the SHAM model over the redshift range $0 < z < 1$ using well-characterized galaxy samples from SDSS and VIPERS (Sections 2 and 3). To give an additional test of the underlying assumptions, we select galaxies by luminosity and stellar mass with matching number densities so that they share the same SHAM prediction. We study systematic errors arising from incompleteness and scatter in Section 4. After demonstrating the robustness of the SHAM model, we apply the rescaling algorithm to the MultiDark simulation and infer the cosmological growth of structure (Section 5). Section 6 concludes with a discussion of the results.

2 GALAXY REDSHIFT SURVEYS

2.1 SDSS Main Galaxy Sample at $z < 0.1$

The Sloan Digital Sky Survey (SDSS; York et al. 2000) Main Galaxy Sample (MGS; Strauss et al. 2002) provides a flux-limited census of galaxies in the low-redshift Universe. In this paper, we use the SDSS MGS Data Release 7 (DR7; Abazajian et al. 2009), which includes spectroscopy and photometry for 499 546 galaxies with Petrosian extinction-corrected r -band magnitude $r < 17.77$ at $z < 0.22$, over 7300 deg^2 .

We obtain the MGS data from the NYU Value Added Galaxy Catalog (NYU-VAGC;¹ Blanton et al. 2005), which provide K -corrections, absolute magnitudes, completeness weights, and the survey mask. We use the Data Release 7 (DR7) Large Scale Structure (LSS) catalogue, which employs a more restrictive r -band cut at $r < 17.6$ in order to ensure a homogeneous selection across the SDSS footprint. The absolute magnitudes in the $ugriz$ bands included in the LSS catalogue are K -corrected to $z_0 = 0.1$ using k -correct (Blanton et al. 2003). By blueshifting the rest frame to $z = 0.1$, the effect of the correction is minimized.

The NYU-VAGC provides all the elements needed to measure the SDSS correlation function, including survey mask, randoms, and galaxy weights. Following the procedure described in Favole et al. (2017), the NYU-VAGC randoms are corrected for the variation of completeness across the SDSS footprint. This correction is performed by down-sampling the random catalogue with equal surface density in a random fashion using the completeness as a probability function (see section 3 in Favole et al. 2017 for more details).

We apply two different galaxy weights to correct for angular incompleteness. The fibre collision weight, w_{fc} , accounts for the fact that fibres on the same tile cannot be placed closer than 55 arcsec. These weights correspond to the total number of neighbours within a 55-arcsec radius of each MGS galaxy for which redshift was not measured due to fibre collisions (i.e. $w_{\text{fc}} \geq 0$). The second weight, w_c , accounts for the redshift measurement success rate

¹<https://cosmo.nyu.edu/blanton/vagc/>

in the mask sector where each galaxy lies, so that $w_c \leq 1$. The average completeness of the MGS is ~ 80 per cent (see Montero-Dorta & Prada 2009). In the computation of the correlation function, each galaxy is counted as $(1 + w_{fc})w_c$ and each random as w_c since we previously diluted the random catalogue using the w_c measurement completeness.

We select a single sample in the redshift range $0.02 < z < 0.106$ by imposing an r -band absolute magnitude threshold $^{0.1}M_r < -20.0$. The uncertainty on the SDSS clustering measurement is estimated from the covariance matrix of 200 jackknife resamplings with constant galaxy number density (Favole et al. 2016b).

2.2 VIPERS at $0.5 < z < 1$

The VIMOS Public Extragalactic Redshift Survey (VIPERS; Guzzo et al. 2014; Scodreggio et al. 2018) provides high-fidelity maps of the galaxy field at higher redshift. The survey measured 90 000 galaxies with moderate-resolution spectroscopy using the Visible Multi-Object Spectrograph (VIMOS) at Very Large Telescope (VLT). Targets were selected to a limiting magnitude of $i_{AB} = 22.5$ in 24 deg^2 of the Canada–France–Hawaii Telescope Legacy Survey (CFHTLS) wide imaging survey. The low-redshift limit was imposed by a pre-selection based upon colour that effectively removed foreground galaxies while providing a robust flux-limited selection at $z > 0.5$.

The completeness of the VIPERS sample with respect to the parent flux-limited sample is well characterized in terms of the target sampling rate (TSR) and spectroscopic redshift measurement success rate (SSR; Scodreggio et al. 2018). Additionally, close pairs of galaxies could not be targeted due to slit placement constraints leading to a drop in the correlation function at very small scales $< 1 h^{-1} \text{ Mpc}$. We correct for this effect by up-weighting pairs according to their angular separation when computing the correlation function (see Pezzotta et al. 2017).

The VIPERS sample has photometric measurements from the ultraviolet to infrared that have been used to infer the luminosity and stellar masses of the galaxies (Davidzon et al. 2013, 2016 Fritz et al. 2014; Moutard et al. 2016). The absolute magnitudes are presented assuming a standard flat cosmological model with $\Omega_m = 0.3$ and $h = 1$, but note that we compute the number density of the samples in the MultiDark cosmology for the SHAM analysis. The distribution of the rest-frame magnitude M_B is shown in Fig. 1.

For the analysis we select four samples in overlapping bins of redshift with thresholds in M_B . These samples are labelled L1, L2, L3, and L4 and listed in Table 1. We impose an evolving luminosity limit to account for the luminosity trend for a passively evolving stellar population as applied in previous VIPERS analyses (e.g. Marulli et al. 2013). The selection threshold in a redshift bin $z_0 < z < z_1$ is specified as $M_{\text{limit}} = M_{z_1} + (z_1 - z)$. We also construct matching samples selected by stellar mass that have the same number density. These samples are labelled M1, M2, M3, and M4. The number density is computed as the weighted sum to correct for TSR and SSR. The completeness limits as a function of luminosity, stellar mass, and colour are shown in Fig. 2.

We make use of the VIPERS mock galaxy catalogues to estimate the covariance of the correlation function measurements. These catalogues were built from the Big MultiDark N -body simulation (Klypin et al. 2016). Galaxies were simulated using the halo occupation distribution (HOD) technique calibrated to reproduce the number density and projected correlation function of VIPERS galaxies in bins of luminosity and redshift (de la Torre et al. 2013, 2017). In total, 153 independent realizations of the full VIPERS survey are available.

For each VIPERS sample we select a comparable sample from the mock catalogues by setting a threshold in luminosity that gives the same number density. We confirm that the projected correlation function of these mock samples approximately matches the amplitude of the VIPERS measurements.

3 MATCHING WITH DARK MATTER HALOES

We use the MultiDark N -body numerical simulation (Klypin et al. 2016) to model the distribution and evolution of dark matter haloes. We choose the Small MultiDark Planck (SMDPL) box, of side length $400 h^{-1} \text{ Mpc}$, containing a total of 3840^3 particles. The simulation assumes a Λ CDM cosmology (Planck Collaboration XVI 2014), with parameters $h = 0.677$, $\Omega_m = 0.307$, $\Omega_\Lambda = 0.693$, $n_s = 0.96$, and $\sigma_8 = 0.823$. Dark matter haloes (including subhaloes) were identified using the ROCKSTAR code (Behroozi, Wechsler & Wu 2013).

We make the connection between galaxies measured in VIPERS or SDSS and haloes from the SMDPL snapshots with SHAM (Vale & Ostriker 2004). The link to the simulated haloes is made using the peak maximum circular velocity of the particles in the halo over its formation history (V_{peak}). The V_{peak} property characterizes

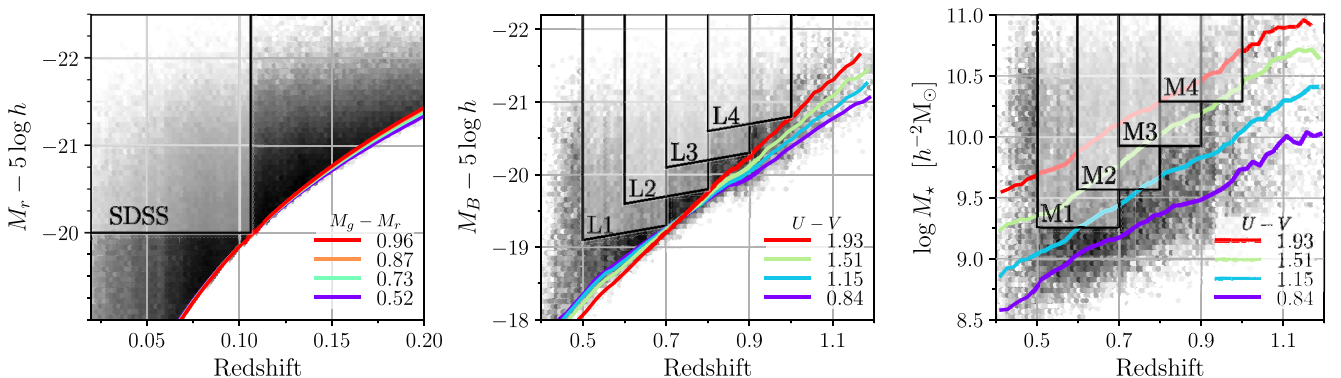
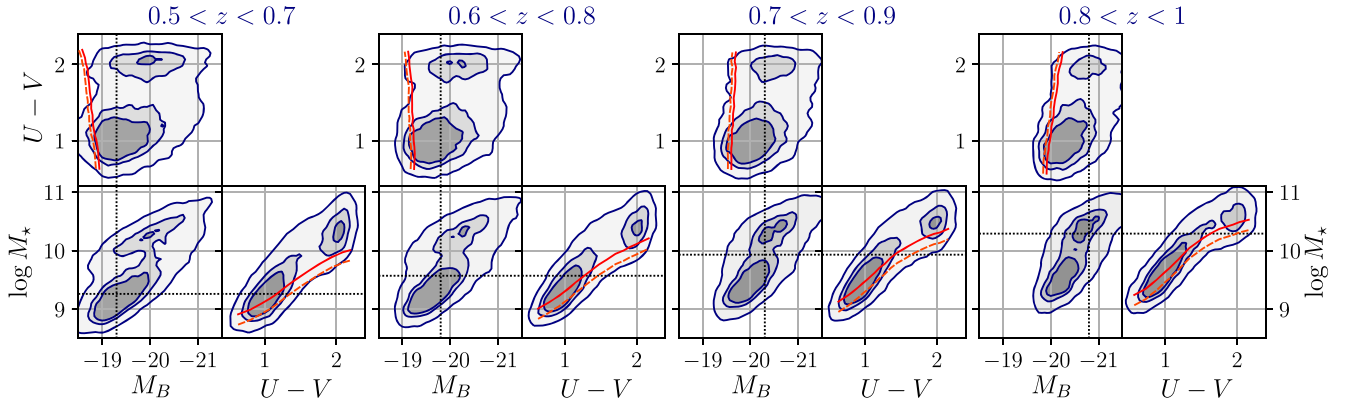


Figure 1. The SDSS and VIPERS samples used in this study. Left: the selection of the SDSS sample on the absolute magnitude in the r band, M_r . Middle: the selection of the VIPERS luminosity samples on M_B with an evolution trend. Right: the selection of the VIPERS stellar mass samples. In each panel the 90 per cent completeness limits are indicated by the lines as a function of the galaxy colour from blue to red (the colour is $M_g - M_r$ for SDSS and $U - V$ for VIPERS).

Table 1. The galaxy samples used in this study. The number density is weighted to correct for survey incompleteness.

Sample	Redshift	Mean z	Threshold	Count	Volume ($10^6 h^{-3} \text{Mpc}^3$)	Density ($10^{-3} h^3 \text{Mpc}^{-3}$)
SDSS	$0.020 < z < 0.106$	0.063	$M_r < -20.0$	117 959	21.90	5.85
L1	$0.5 < z < 0.7$	0.61	$M_B < -19.3 + (0.7 - z)$	23 352	4.93	11.8
M1	$0.5 < z < 0.7$	0.61	$\log M_\star > 9.26 h^{-2} M_\odot$	22 508	4.93	11.8
L2	$0.6 < z < 0.8$	0.70	$M_B < -19.8 + (0.8 - z)$	20 579	5.98	8.57
M2	$0.6 < z < 0.8$	0.70	$\log M_\star > 9.57 h^{-2} M_\odot$	19 577	5.98	8.57
L3	$0.7 < z < 0.9$	0.80	$M_B < -20.3 + (0.9 - z)$	13 046	6.96	4.79
M3	$0.7 < z < 0.9$	0.80	$\log M_\star > 9.93 h^{-2} M_\odot$	12 270	6.96	4.79
L4	$0.8 < z < 1.0$	0.90	$M_B < -20.8 + (1.0 - z)$	6305	7.86	2.13
M4	$0.8 < z < 1.0$	0.89	$\log M_\star > 10.29 h^{-2} M_\odot$	5881	7.86	2.13

**Figure 2.** The distribution of the VIPERS sample as a function of $U - V$ colour, absolute magnitude M_B , and stellar mass for the four redshift bins. The contours contain 25, 50, and 90 per cent of the sample. The horizontal and vertical dotted lines mark the stellar mass and absolute magnitude thresholds, respectively, of the subsamples used in the analysis. The solid and dashed curves indicate the 90 and 50 per cent completeness limits in stellar mass and absolute magnitude as a function of colour. The red sequence is above the stellar mass completeness limit in each redshift bin.

the halo mass before disruption processes occur and it has been demonstrated that this is important for modelling the distribution of satellite galaxies. Velocity is used instead of virial mass because it is more robustly defined in simulations. For further details we refer the reader to Conroy et al. (2006), Trujillo-Gomez et al. (2011), Reddick et al. (2013), and Campbell et al. (2018).

We select galaxies based upon a stellar mass (or luminosity) threshold. Then, within a single simulation snapshot we select haloes by setting a threshold in V_{peak} that results in an equal number density. These haloes become the mock galaxies for the analysis. In Section 4, we test the impact of scatter or stochasticity in the relationship between the halo and galaxy properties. However, our main results are derived without scatter and in this case the SHAM model is determined solely by the densities of the samples listed in Table 1.

Fig. 3 shows the distributions of haloes at $z = 0$ and $z = 1$ as a function of virial mass M_{vir} and V_{peak} . Two V_{peak} threshold selections are indicated that give number densities 10^{-2} and $10^{-3} h^3 \text{Mpc}^{-3}$. The median halo mass of the higher density selection is $M_{\text{vir}} \sim 7.5 \times 10^{11} h^{-1} M_\odot$ at $z = 1$ that corresponds to 7500 simulation particles and guarantees that the haloes selected for the SHAM analysis are robustly defined (Guo & White 2014).

The clustering amplitude of the galaxy field can be inferred from measurements of the projected correlation function without being strongly impacted by the redshift-space distortion signal

caused by peculiar velocities (Davis & Peebles 1983). The projected correlation function w_p depends on the perpendicular separation r_p and is computed by integrating along the line of sight (π direction):

$$w_p(r_p) = 2 \int_0^{\pi_{\text{max}}} \xi_g(r_p, \pi') d\pi'. \quad (2)$$

We set the integration limit to $\pi_{\text{max}} = 50 h^{-1} \text{Mpc}$.

We compute the redshift-space correlation function $\xi(r_p, \pi)$ for the galaxy surveys using the Landy–Szalay estimator (Landy & Szalay 1993). We employ two correlation function code implementations that of Favole et al. (2017) and CUTE (Alonso 2012). The correlation functions of the MultiDark SHAM samples are computed in the plane-parallel approximation taking advantage of the periodic boundaries of the cubic simulation box. The residual redshift-space distortion signal in the projected correlation function is present both in the galaxy and halo measurements, so we do not make any additional corrections.

We compute the projected correlation functions for the SHAM models at the redshifts of the MultiDark snapshots, $w_p^{\text{halo}}(r_p, z|n)$, where n is the number density of the galaxy sample. To compute the model between the simulation snapshots at an arbitrary redshift we build a linear interpolation function that is based on the principal component decomposition using the first two eigenvectors.

Fig. 4 shows the measured correlation function for each galaxy sample and the corresponding SHAM model at the sample redshift.

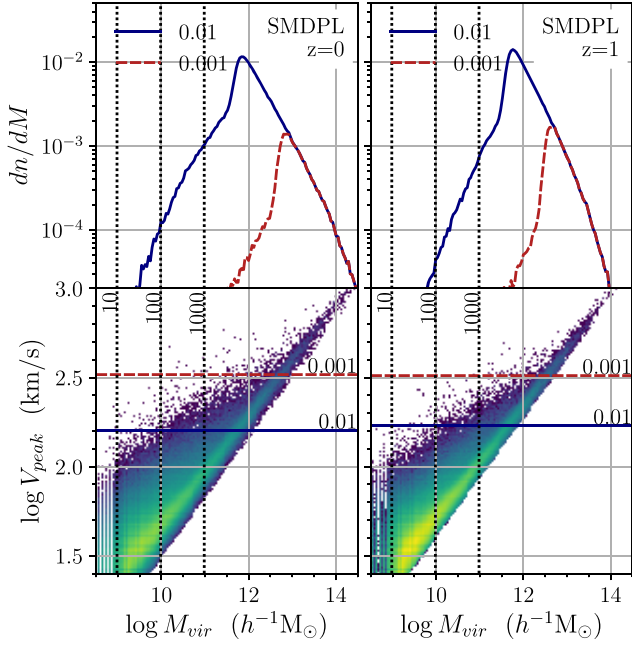


Figure 3. The distribution of V_{peak} and M_{vir} halo properties in SMDPL at $z = 0$ (left-hand panels) and $z = 1$ (right-hand panels). The horizontal solid and dashed lines in the bottom panels indicate thresholds in V_{peak} that give number densities of 10^{-2} and $10^{-3} h^3 \text{Mpc}^{-3}$. The M_{vir} distributions after applying these selections are shown in the top panels (solid and dashed histograms). The vertical dotted lines indicate the virial mass corresponding to 10, 100, and 1000 simulation particles.

There is good agreement between the SHAM model and the SDSS measurements. This confirms previous studies that developed and tested the SHAM model on the SDSS galaxy correlation function (e.g. Reddick et al. 2013).

We find that the VIPERS luminosity-selected samples have a clustering amplitude that is systematically lower than the stellar-mass-selected samples. This discrepancy is more significant at smaller scales $r_p < 1 h^{-1} \text{Mpc}$ and in the highest redshift bin. In each redshift bin the luminosity- and stellar-mass-selected samples were constructed to share the same SHAM prediction, thus we find that the SHAM model better reproduces the clustering of the stellar-mass-selected sample.

The systematic difference in clustering amplitude between the luminosity- and stellar-mass-selected samples is not unexpected since hydrodynamic simulations have demonstrated that galaxy stellar mass is a better indicator for the host halo mass (Chaves-Montero et al. 2016). We would expect the choice to be less important when selecting galaxies based upon the rest-frame luminosity in a redder band that is more tightly correlated to the stellar mass (Bell & de Jong 2001). This can explain the agreement with SHAM seen in SDSS projected correlation functions for both M_r - and mass-selected samples² (Reddick et al. 2013). On the other hand, the bluer rest-frame band used in VIPERS (that is closest to the observed i selection band) is more sensitive to recent star formation activity and hence is less informative of the total mass of the galaxy. The consequence is that in VIPERS, the correlation function of galaxies

²He et al. (2018) point out that the correlation functions of luminosity- and stellar-mass-selected samples are not similar in redshift space and stellar mass should be preferred.

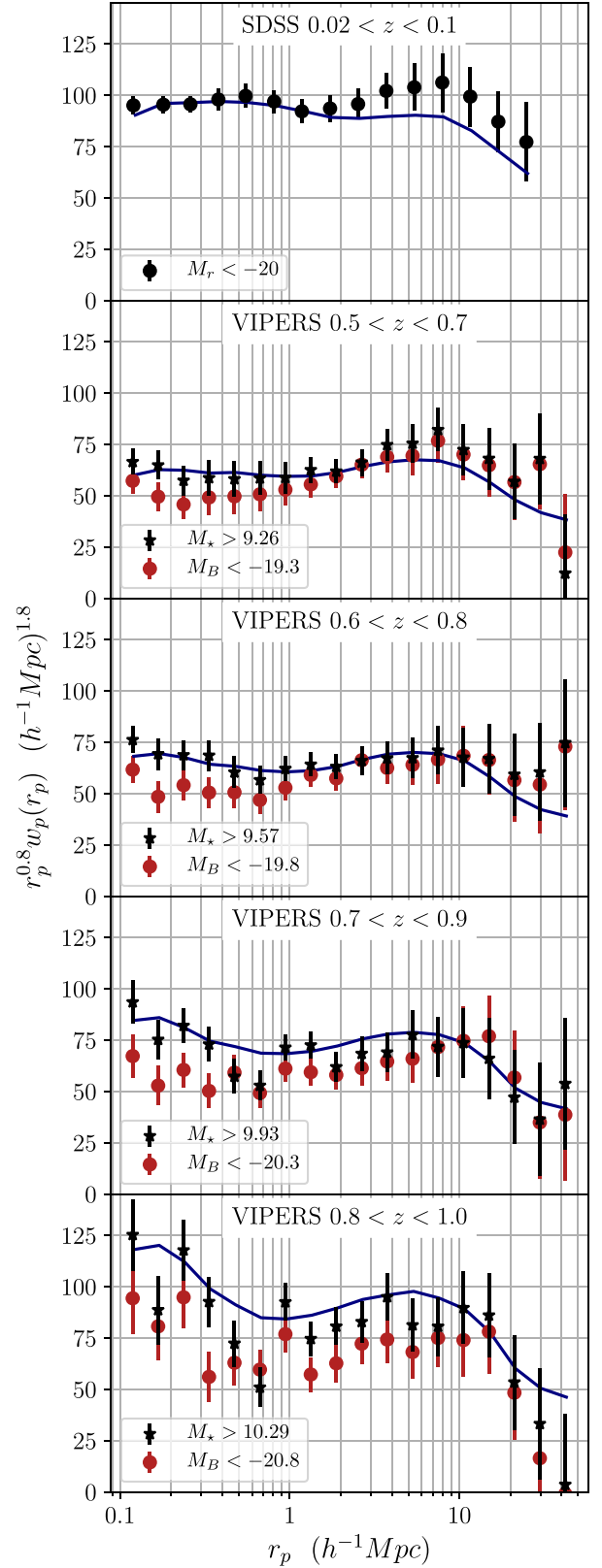


Figure 4. The projected correlation function measured in SDSS (top panel) and VIPERS (bottom four panels) in luminosity- and stellar-mass-selected samples. The matched samples have the same number density and thus share the same SHAM model (solid curve).

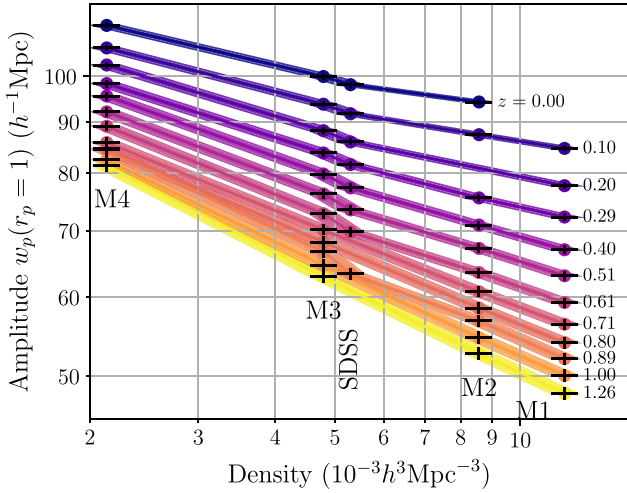


Figure 5. The correlation function amplitude at $r = 1 h^{-1} \text{Mpc}$ versus galaxy number density of all SHAM samples used in our analysis. The error bars correspond to 5 per cent variations in number density, which is representative of the VIPERS sample variance. In order to change the amplitude by 10 per cent requires a change of number density of 50 per cent at $z = 0$ and 30 per cent at $z = 1$.

selected in M_B is lower than for those selected by stellar mass. This effect should become more important at higher redshift as the rest frame for a fixed bandpass shifts to the blue and star formation activity becomes more prevalent (Haines et al. 2017).

4 SYSTEMATICS

We have found that the SHAM model can predict the galaxy clustering signal to redshift 1; however, it is important to make note of the assumptions that have been made and consider how extensions to the SHAM recipe would affect our results. On the observational side, uncertainty in the number density due to sample variance or incompleteness propagates to the SHAM model as a systematic error. Fig. 5 summarizes the SHAM models that we constructed for this work and demonstrates the power-law relationship between the clustering amplitude at $r = 1 h^{-1} \text{Mpc}$ and number density. The horizontal error bars on this plot indicate 5 per cent variations in number density that is representative of the sample variance in the VIPERS samples. The vertical error bar propagates this error to the amplitude of the correlation function and is at the per cent level. In order to change the amplitude of the correlation function by 10 per cent requires varying the number density by 50 per cent at $z = 0$ and 30 per cent at $z = 1$. These conclusions follow from the SHAM model that imposes that the clustering amplitude is determined only by stellar mass (or other halo mass proxy). This is not precisely true since galaxy colour correlates with the density of the environment at fixed stellar mass (e.g. Davidzon et al. 2016).

We also see from Fig. 5 that the SHAM prediction becomes less sensitive to redshift at lower number density. Therefore, to improve the constraining power requires higher density samples that at high redshift becomes observationally challenging.

The SHAM procedure can be extended to improve the precision of the predictions. Scatter can be introduced to account for the fact that galaxies of a specific stellar mass are associated with a greater variety of halo properties than the SHAM dictates. This may be due to stochastic processes or error in the host halo assignment due to missing physical ingredients. Investigations with hydrodynamic

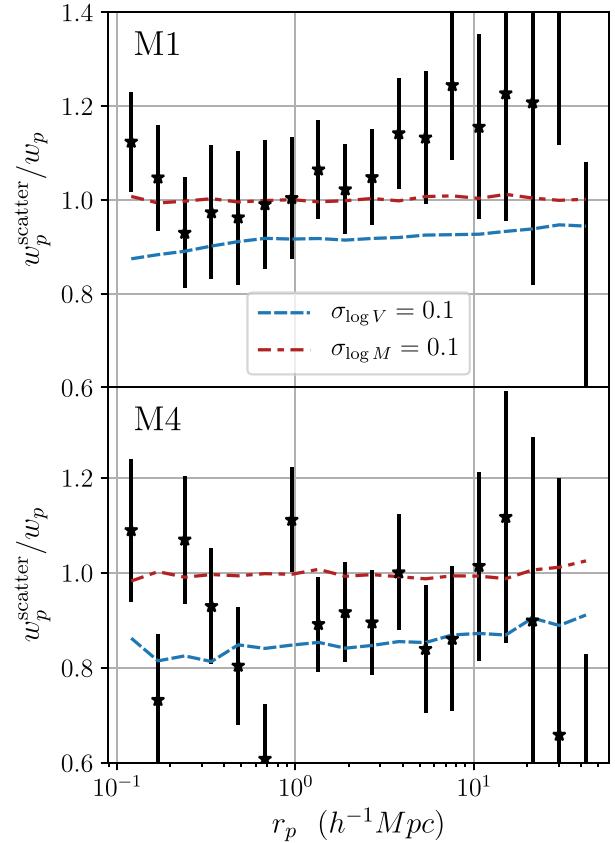


Figure 6. The relative change in the correlation function after introducing scatter in the SHAM procedure is shown for two mass-selected samples in VIPERS M1 $0.5 < z < 0.7$ (top) and M4 $0.8 < z < 1.0$ (bottom). A Gaussian scatter of 0.1 dex was applied to M_* (dash-dotted curve) or V_{peak} (dashed curve).

simulations indicate that the relationship between galaxy stellar mass and halo V_{peak} is approximately 0.1 dex (Chaves-Montero et al. 2016).

Fig. 6 shows the effect of scatter following two approaches. First, we consider scatter applied to the stellar mass (Behroozi et al. 2010, see also Trujillo-Gomez et al. 2011 who apply scatter to luminosity). From the observational perspective, this scatter cannot be too large otherwise the intrinsic (deconvolved) stellar mass function would be inconsistent with observations. A large scatter also requires extrapolating the stellar mass function to low masses below observational limits. We thus test scatter in stellar mass of 0.1 dex. We find that scatter of $\sigma_{\log M} = 0.1$ dex has no effect on the measured correlation function at the per cent level for the number densities of the VIPERS samples. This is due to the fact that the stellar mass function is flattening at the selection threshold (Reddick et al. 2013).

Next we consider a dispersion in V_{peak} . This implies that V_{peak} is not a perfect proxy for galaxy assignment. The advantage of applying scatter to V_{peak} is that a large scatter may be introduced without modifying the stellar mass function of galaxies. We find that the scatter of $\sigma_{\log V} = 0.1$ dex does modify the amplitude of the correlation function by 10–20 per cent in the VIPERS samples. The scatter can improve the match of the VIPERS data at high redshift but is not required given the statistical error. However, scatter at the same level applied at lower redshift is ruled out. The introduction

of free parameters to account for redshift-dependent scatter would greatly limit the cosmological interpretation.

5 GROWTH OF STRUCTURE

We now adopt the SHAM model without scatter to constrain the growth of structure. For each galaxy sample, we construct a halo sample with matching number density for each one of 12 simulation outputs with snapshot redshifts $0 < z_{\text{snap}} < 1.3$. The correlation functions of the halo samples from each snapshot are overplotted in the panels of Fig. 7.

The best-fitting snapshot redshift was found for each sample by minimizing the χ^2 statistic over redshift:

$$\chi^2 = \sum_{i,j} (w_i^{\text{obs}} - w_i^{\text{halo}}(z)) C_{ij}^{-1} (w_j^{\text{obs}} - w_j^{\text{halo}}(z)), \quad (3)$$

where i and j index the r_p bins of the projected correlation function. The analysis was made on scales greater than $r_{\text{min}} = 1 h^{-1} \text{Mpc}$ to avoid systematic uncertainties in both the observations and simulations. The covariance matrices were inverted using the singular-value decomposition algorithm with a threshold of 0.1 on the relative size of the eigenvalues. Fig. 8 shows the χ^2 values and best-fitting redshifts. The uncertainty of the determinations was estimated with the threshold $\Delta\chi^2 = 1$.

The evolution of σ_8 is shown in Fig. 8 for alternative gravity models parametrized by the growth index γ . The mapping is defined using the growth equation $\sigma_8(z)$ (equation 1). Considering the growth history in the MultiDark cosmology $\sigma_8^{\text{MD}}(z)$ and an alternative model $\sigma_8'(z|\gamma)$, we determine the snapshot redshift z_{MD} that satisfies $\sigma_8^{\text{MD}}(z_{\text{MD}}) = \sigma_8'(z|\gamma)$.

In order to test models with high values of σ_8 we would need simulation outputs at scale factors $a > 1$ ($z < 0$). Since these are not available in MultiDark, we linearly interpolate the correlation function to emulate these outputs. We also extrapolate to higher redshift that is required to test models with low $\sigma_8(z)$.

We computed the joint likelihood defined by the χ^2 in equation (3) of each correlation function measurement as a function of σ_8 and γ . All other cosmological parameters were implicitly held fixed at the fiducial values of the MultiDark simulation. The likelihood surface is shown in Fig. 9. Some regions of the parameter space require extrapolation of the model well beyond the simulation snapshots. The limits requiring extrapolation to $z < -0.3$ and $z > 1.5$ are indicated by the dotted curves in the figure but they are not excluded from the likelihood analysis. The marginalized constraints are $\gamma = 0.2^{+0.4}_{-0.3}$ and $\sigma_8 = 0.87 \pm 0.07$. By fixing the value of σ_8 today to the MultiDark value $\sigma_8 = 0.82$ we find the growth index $\gamma = 0.6^{+0.3}_{-0.2}$. Considering the standard model with $\gamma = 0.55$ gives $\sigma_8 = 0.85 \pm 0.04$.

6 DISCUSSION AND CONCLUSIONS

At low redshift the distribution of haloes has been shown to be a good proxy for the distribution of galaxies and the SHAM recipe has been a success for modelling galaxy clustering. This is particularly true for galaxy samples that are complete to the characteristic luminosity L_* . At higher redshift VIPERS uniquely provides a data set to complement low-redshift studies. Here, we have found that the standard SHAM model without free parameters reproduces the amplitude of the projected correlation function over redshift range $0 < z < 1$ spanning SDSS and VIPERS.

We tested both luminosity and stellar mass selected samples in VIPERS constructed to have the same SHAM model. The

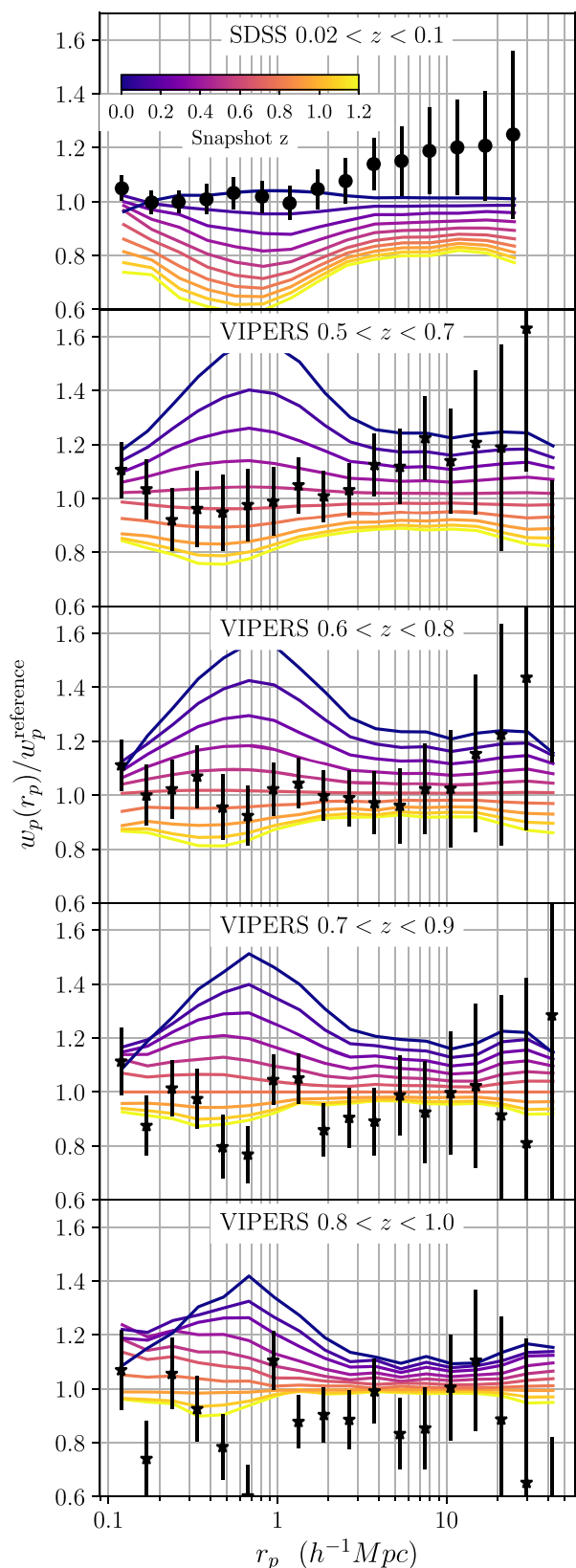


Figure 7. The SHAM model projected correlation functions computed over a range of simulation redshifts $0 < z < 1.2$. In each panel the correlation function has been divided by the SHAM model at the sample redshift. The data points indicate the SDSS sample (top panel) and VIPERS stellar-mass-selected samples (bottom four panels).

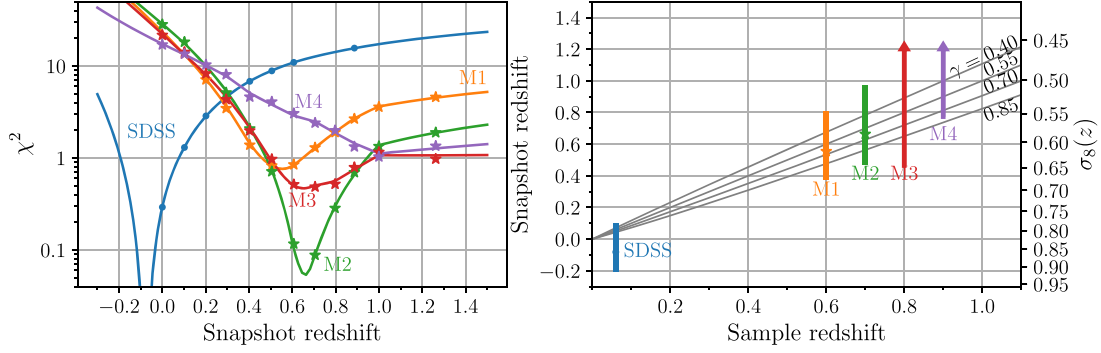


Figure 8. Left: the χ^2 statistics for each galaxy sample (SDSS, M1, M2, M3, M4) as a function of redshift. The markers indicate the SHAM models computed from the simulation snapshots, while the curves were derived by linear interpolation of the models. Negative snapshot redshifts (scale factor >1) corresponds to running the simulation into the future. Right: the best-fitting SHAM model as a function of its simulation snapshot is plotted for each galaxy sample shown on the left. The rightmost scale indicates the value of $\sigma_8(z)$ of the simulation snapshots. Three alternative growth histories are overlotted with growth index $\gamma = 0.4, 0.7$, and 0.85 that give different mappings between the simulation redshift and the sample redshift.

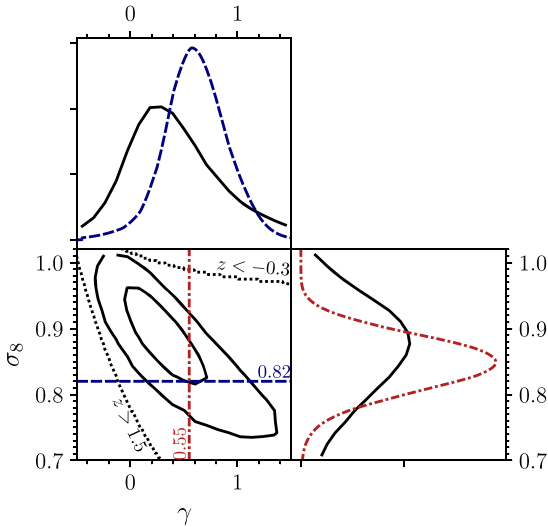


Figure 9. The likelihood degeneracy between the model parameters γ and σ_8 today. The contours mark the 1σ and 2σ levels. The broken curves show the constraints on γ with fixed $\sigma_8 = 0.82$ and on σ_8 with fixed $\gamma = 0.55$. The dotted curves indicate the borders of regions requiring extrapolation well beyond the simulation snapshots at $z < -0.3$ or $z > 1.5$.

luminosity-selected samples were found to have a lower clustering amplitude. This supports the claim that stellar mass is a better proxy for the host halo mass. We expect that luminosity becomes less informative at higher redshift due to the greater influence of star formation activity particularly in bluer rest-frame photometry.

Observational scatter in the relationship between stellar mass and the halo V_{peak} property cannot significantly impact the correlation function. We tested scatter in stellar mass at the level of 0.1 dex and found no change in the correlation function and greater levels of scatter is not consistent with the observed shape of the stellar mass function. However, scatter applied to V_{peak} at the level of 0.1 dex does modify the amplitude of the correlation function.

After demonstrating that SHAM can be successfully used to model the VIPERS sample, we apply the rescaling algorithm proposed by Angulo & White (2010) to test the history of structure formation. The growth history provides direct constraints on

alternative cosmological models with modifications to gravity. We estimate the growth index γ to be $\gamma = 0.6 \pm 0.3$ considering SDSS and the VIPERS stellar-mass-selected samples. The constraint was derived by fixing the value of σ_8 today. Allowing σ_8 to vary significantly reduces the constraining power of the data we consider. The sensitivity of the SHAM prediction depends on number density and we expect that the precision measurements from upcoming photometric and spectroscopic surveys at redshift ~ 1 will allow robust constraints on both the normalization and the redshift dependence of $\sigma_8(z)$.

The constraints we find may be compared to those from previous studies based on galaxy peculiar velocities and redshift-space distortions (Guzzo et al. 2008; Song & Percival 2009; Blake et al. 2011, 2013; Beutler et al. 2012; Johnson et al. 2014; Alam et al. 2017). Galaxy velocities on large scales are sensitive to the derivative of the growth factor $f = -d \log \sigma_8(z) / d \log(1+z) = \Omega_m(z)^\gamma$. Using VIPERS data, de la Torre et al. (2017) presented a 20 per cent measurement on $f\sigma_8$ in two redshift bins at $z = 0.60$ and 0.86 . Transforming these constraints to γ we find $\gamma = 0.57^{+0.3}_{-0.4}$. Hudson & Turnbull (2012) compiled measurements from peculiar velocity and redshift-space distortion surveys and reported the joint constraint $\gamma = 0.619 \pm 0.054$. Using the Baryon Oscillation Spectroscopic Survey (BOSS) and extended-BOSS (eBOSS), Zhao et al. (2019) found $\gamma = 0.469 \pm 0.148$. By convention redshift-space distortion analyses fix the amplitude of clustering at high redshift where it is constrained by measurements of the cosmic microwave background. In contrast, our method is sensitive to the integrated growth over a period at late time from redshift 1 to 0.

We investigated the effect of systematic uncertainties that would impact the SHAM prediction through the dependence on number density. The sample variance present in the VIPERS sample propagates to the correlation function amplitude at the per cent level, and so cannot make a significant contribution to the error. Incompleteness at the 30 per cent level would change the correlation function amplitude by 10 per cent, but we have no evidence for the existence of such a population of missing galaxies. Fig. 2 shows that the sample is incomplete in stellar mass only for the reddest galaxies at high redshift. A significant population of missing red galaxies could affect the clustering amplitude and alter the trend with density shown in Fig. 5; however, we do not expect our results to be significantly biased considering the level of

precision of the VIPERS measurements at high redshift. Upcoming surveys such as ESA *Euclid* will target galaxies in the near-infrared and may shed additional light on the importance of stellar mass incompleteness.

The SHAM recipe may be extended in future work to improve the precision of the analysis. Scatter was not needed to fit the VIPERS data, but a degree of intrinsic scatter is expected in the relationship between galaxy and halo properties. More flexible SHAM models can also be used to model samples that suffer from incompleteness (Favole et al. 2016a, 2017) or completeness corrections can be inferred from deeper samples. Secondary dependencies that are a signature of assembly bias such as the halo formation time can also improve the precision of the SHAM model (Hearin & Watson 2013; Lin et al. 2016; Miyatake et al. 2016; Montero-Dorta et al. 2017; Niemiec et al. 2018). The additional parameters in these models may be degenerate with the cosmological information we are attempting to extract, but there is a clear way forward if they can be constrained from observations such as weak lensing measurements (Favole et al. 2016a).

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REFERENCES

Abazajian K. N. et al., 2009, *ApJS*, 182, 543
 Alam S. et al., 2017, *MNRAS*, 470, 2617
 Alonso D., 2012, preprint (arXiv:1210.1833)
 Angulo R. E., White S. D. M., 2010, *MNRAS*, 405, 143
 Bardeen J. M., Bond J. R., Kaiser N., Szalay A. S., 1986, *ApJ*, 304, 15
 Baugh C. M., 2013, *Publ. Astron. Soc. Aust.*, 30, e030
 Behroozi P. S., Conroy C., Wechsler R. H., 2010, *ApJ*, 717, 379
 Behroozi P. S., Wechsler R. H., Wu H.-Y., 2013, *ApJ*, 762, 109
 Bell E. F., de Jong R. S., 2001, *ApJ*, 550, 212
 Beutler F. et al., 2012, *MNRAS*, 423, 3430
 Blake C. et al., 2011, *MNRAS*, 415, 2876
 Blake C. et al., 2013, *MNRAS*, 436, 3089
 Blanton M. R., Berlind A. A., 2007, *ApJ*, 664, 791
 Blanton M. R. et al., 2003, *AJ*, 125, 2348
 Blanton M. R. et al., 2005, *AJ*, 129, 2562
 Campbell D., van den Bosch F. C., Padmanabhan N., Mao Y.-Y., Zentner A. R., Lange J. U., Jiang F., Villarreal A., 2018, *MNRAS*, 477, 359
 Cappi A. et al., 2015, *A&A*, 579, A70

Chaves-Montero J., Angulo R. E., Schaye J., Schaller M., Crain R. A., Furlong M., Theuns T., 2016, *MNRAS*, 460, 3100
 Conroy C., Wechsler R. H., Kravtsov A. V., 2006, *ApJ*, 647, 201
 Cucciati O. et al., 2017, *A&A*, 602, A15
 Davidzon I. et al., 2013, *A&A*, 558, A23
 Davidzon I. et al., 2016, *A&A*, 586, A23
 Davis M., Geller M. J., 1976, *ApJ*, 208, 13
 Davis M., Peebles P. J. E., 1983, *ApJ*, 267, 465
 de la Torre S. et al., 2013, *A&A*, 557, A54
 de la Torre S. et al., 2017, *A&A*, 608, A44
 Di Porto C. et al., 2016, *A&A*, 594, A62
 Favole G. et al., 2016a, *MNRAS*, 461, 3421
 Favole G., McBride C. K., Eisenstein D. J., Prada F., Swanson M. E., Chuang C.-H., Schneider D. P., 2016b, *MNRAS*, 462, 2218
 Favole G., Rodríguez-Torres S. A., Comparat J., Prada F., Guo H., Klypin A., Montero-Dorta A. D., 2017, *MNRAS*, 472, 550
 Fritz A. et al., 2014, *A&A*, 563, A92
 Giovanelli R., Haynes M. P., Chincarini G. L., 1986, *ApJ*, 300, 77
 Guo Q., White S., 2014, *MNRAS*, 437, 3228
 Guzzo L., Strauss M. A., Fisher K. B., Giovanelli R., Haynes M. P., 1997, *ApJ*, 489, 37
 Guzzo L. et al., 2008, *Nature*, 451, 541
 Guzzo L. et al., 2014, *A&A*, 566, A108
 Haines C. P. et al., 2017, *A&A*, 605, A4
 Harker G., Cole S., Jenkins A., 2007, *MNRAS*, 382, 1503
 He J.-h., Guzzo L., Li B., Baugh C. M., 2018, *Nat. Astron.*, 2, 967
 Hearin A. P., Watson D. F., 2013, *MNRAS*, 435, 1313
 Hudson M. J., Turnbull S. J., 2012, *ApJ*, 751, L30
 Huterer D. et al., 2015, *Astropart. Phys.*, 63, 23
 Johnson A. et al., 2014, *MNRAS*, 444, 3926
 Kaiser N., 1984, *ApJ*, 284, L9
 Klypin A., Yepes G., Gottlöber S., Prada F., Heß S., 2016, *MNRAS*, 457, 4340
 Landy S. D., Szalay A. S., 1993, *ApJ*, 412, 64
 Lin Y.-T., Mandelbaum R., Huang Y.-H., Huang H.-J., Dalal N., Diemer B., Jian H.-Y., Kravtsov A., 2016, *ApJ*, 819, 119
 Linder E. V., 2005, *Phys. Rev. D*, 72, 043529
 Marulli F. et al., 2013, *A&A*, 557, A17
 Mead A. J., Peacock J. A., 2014a, *MNRAS*, 440, 1233
 Mead A. J., Peacock J. A., 2014b, *MNRAS*, 445, 3453
 Mead A. J., Peacock J. A., Lombriser L., Li B., 2015, *MNRAS*, 452, 4203
 Miyatake H., More S., Takada M., Spergel D. N., Mandelbaum R., Rykoff E. S., Rozo E., 2016, *Phys. Rev. Lett.*, 116, 041301
 Montero-Dorta A. D., Prada F., 2009, *MNRAS*, 399, 1106
 Montero-Dorta A. D. et al., 2017, *ApJ*, 848, L2
 Moresco M., Marulli F., 2017, *MNRAS*, 471, L82
 Moster B. P., Somerville R. S., Maubetsch C., van den Bosch F. C., Macciò A. V., Naab T., Oser L., 2010, *ApJ*, 710, 903
 Moutard T. et al., 2016, *A&A*, 590, A102
 Niemiec A. et al., 2018, *MNRAS*, 477, L1
 Norberg P. et al., 2002, *MNRAS*, 332, 827
 Pezzotta A. et al., 2017, *A&A*, 604, A33
 Planck Collaboration XVI, 2014, *A&A*, 571, A16
 Pollo A. et al., 2006, *A&A*, 451, 409
 Reddick R. M., Wechsler R. H., Tinker J. L., Behroozi P. S., 2013, *ApJ*, 771, 30
 Rodríguez-Torres S. A. et al., 2017, *MNRAS*, 468, 728
 Rota S. et al., 2017, *A&A*, 601, A144
 Scodreggio M. et al., 2018, *A&A*, 609, A84
 Silvestri A., Pogosian L., Buniy R. V., 2013, *Phys. Rev. D*, 87, 104015
 Simha V., Cole S., 2013, *MNRAS*, 436, 1142
 Song Y.-S., Percival W. J., 2009, *J. Cosmol. Astropart. Phys.*, 10, 004
 Springel V. et al., 2005, *Nature*, 435, 629
 Strauss M. A. et al., 2002, *AJ*, 124, 1810
 Trujillo-Gomez S., Klypin A., Primack J., Romanowsky A. J., 2011, *ApJ*, 742, 16

Vale A., Ostriker J. P., 2004, *MNRAS*, 353, 189
Wang L., Steinhardt P. J., 1998, *ApJ*, 508, 483
Wechsler R. H., Tinker J. L., 2018, *ARA&A*, 56, 435
White S. D. M., Frenk C. S., 1991, *ApJ*, 379, 52
York D. G. et al., 2000, *AJ*, 120, 1579
Zehavi I. et al., 2005, *ApJ*, 630, 1

Zennaro M., Angulo R. E., Aricò G., Contreras S., Pellejero-Ibáñez M.,
2019, preprint ([arXiv:1905.08696](https://arxiv.org/abs/1905.08696))
Zhao G.-B. et al., 2019, *MNRAS*, 482, 3497

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