Millisecond $23/2^+$ isomers in the N = 79 isotones ¹³³Xe and ¹³⁵Ba

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smooth onset of isomeric $J^{\pi} = 23/2^+$ states along the N = 79 isotones and close a gap in the high-spin systematics towards the recently investigated $J^{\pi} = 23/2^+$ isomer in ¹³⁹Nd. The resulting systematics of M2 reduced transition probabilities is discussed within the framework of the nuclear shell model. Latest large-scale shell-model calculations employing the SN100PN, GCN50:82, SN100-KTH, and a realistic effective interaction reproduce the experimental findings generally well and give insight into the structure of the isomers.

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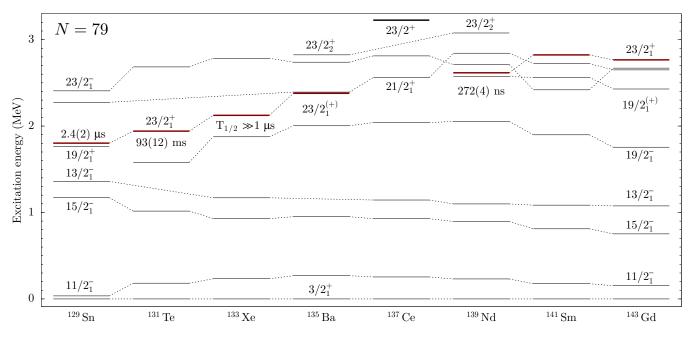


FIG. 1. Evolution of excited states along the N = 79 chain. Dashed lines connecting levels of same spin and parity are drawn to guide the eye. The $J^{\pi} = 23/2^+_1$ states in ¹²⁹Sn, ¹³¹Te, and ¹³⁹Nd are isomers. A candidate for a $J^{\pi} = 23/2^+$ isomer at $E_x = 2107 + x$ keV was reported in ¹³³Xe [5]. It is expected that a corresponding long-lived state is also present in ¹³⁵Ba. Data extracted from the ENSDF database [8] and Refs. [1,5–7].

I. INTRODUCTION

The N = 79 isotones ¹³³Xe and ¹³⁵Ba, only three neutrons away from the N = 82 shell closure, are located within the proton midshell between the Z = 50 shell and the Z = 64subshell closures. In this region, the evolution of nuclear collectivity competes with the excitation of single-particle states. Enabling high-*j* couplings, the intruder $h_{11/2}$ neutron orbital is pivotal for high-spin states in this region. ¹³³Xe and ¹³⁵Ba present an intriguing study ground for the predictive power of the shell model at both low and high spins in the vicinity of the N = 82 neutron closed shell. In particular, detailed knowledge of long-lived states—so-called isomers—provide a sensitive probe for the active quasiparticle configurations.

Figure 1 shows the evolution of several negative-, and positive-parity states along the N = 79 chain, ranging from semimagic ${}_{50}^{129}$ Sn up to ${}_{64}^{143}$ Gd. Isomeric $J^{\pi} = 11/2_1^-$ states with neutron-hole $vh_{11/2}^{-1}$ configurations were discovered in all odd-mass N = 79 isotones. Furthermore, several $J^{\pi} = 19/2^+$, $23/2^+$, and $27/2^-$ high-spin isomers above the $J^{\pi} = 11/2_1^-$ states were reported in the literature. These isomeric states are explained as high-spin members of the $v(h_{11/2}^{-2}d_{3/2}^{-1})$ and $v(h_{11/2}^{-n})$, seniority v = 3 multiplets [1–9].

Information on excited states in ¹²⁹Sn and ¹³¹Te were mainly obtained from β decay and actinide fission studies. In a previous experiment, the semimagic nucleus ¹²⁹Sn was populated via thermal neutron-induced fission and investigated by means of γ -ray and electron-conversion spectroscopy [1,9]. Two *L* conversion lines corresponding to transition energies of 41.0 and 19.7 keV were identified as the decay of $J^{\pi} =$ $23/2^+$ and $19/2^+$ states, respectively. Based on the decay curves of the two electron-conversion lines and corresponding γ -ray decays, half-lives of $T_{1/2} = 2.4(2) \ \mu s$ for the $J^{\pi} = 23/2^+$ state and $T_{1/2} = 3.6(2) \ \mu s$ for the $J^{\pi} = 19/2^+$ state were determined [1]. In ¹²⁹Sn the seniority v = 3 multiplet is completed by the $J^{\pi} = (27/2^-)$ state at $E_x = 2552 \text{ keV}$ $[T_{1/2} = 0.27(7) \ \mu s]$, identified by Lozeva *et al.* in 2008 [4].

¹³¹Te was populated in a pioneering 64 Ni + 130 Te multinucleon-transfer experiment at the GASP γ -ray spectrometer [10]. A delayed 361-564-833-keV triple- γ coincidence was identified to form the $(21/2^{-}) \rightarrow (19/2^{-}) \rightarrow$ $(15/2^{-}) \rightarrow 11/2^{-}$ yrast band. Referring to isotopic systematics, a $J^{\pi} = 23/2^+$ isomer is proposed that is located slightly above the $J^{\pi} = (21/2^{-})$ state at $E_x = 1941$ keV with a lower half-life limit of $T_{1/2} > 1 \ \mu$ s. However, no low-energy E1 transition was observed in this work. Soon after, ¹³¹Te was also populated after thermal fission of U isotopes at the OSIRIS mass separator by Fogelberg et al. [6]. In this work, a very long half-life of $T_{1/2} = 93(12)$ ms was determined. Based on conversion-electron measurements, the authors excluded a low-energy E1 transition hypothesis and the $E_x =$ 1941-keV state was revised to be a $J^{\pi} = (23/2^+)$ isomer. The 361-keV transition was proposed to be of E3 character, connecting the isomer with a $J^{\pi} = (17/2^{-})$ state. Finally, in a later fusion-fission experiment by Astier et al. [2] utilizing the EUROBALL array, the negative-parity band on top of the $J^{\pi} = (19/2^{-})$ state was extended to excitation energies of approximately 4.7 MeV and spin $J^{\pi} = (35/2^{-})$. The determined lower limit of the half-life of the $J^{\pi} = (23/2^+)$ state $(T_{1/2} \gg 10 \ \mu s)$ is in agreement with the previous experiment. The multipolarity of the 361-keV transition was reevaluated to be mainly of M2 character. Based on the OSIRIS result and the reevaluated M2 character, a reduced transition strength of $B(M2; 23/2^+_1 \rightarrow 19/2^-_1) = 2.0(3) \times 10^{-6}$ W.u. [2] was

deduced. Shell-model calculations predict a $\nu(h_{11/2}^{-2}d_{3/2}^{-1})$ configuration for the $J^{\pi} = (23/2^+)$ state and a predominant $(\nu h_{11/2}^{-1})(\pi g_{7/2}^2)$ configuration for the $J^{\pi} = (19/2^-)$ state. No feeding transitions for the $J^{\pi} = (23/2^+)$ isomer were yet discovered in ¹³¹Te.

Going to the proton midshell, a first search of high-spin isomers in ¹³⁷Ce was made using a ⁴He + ¹³⁸Ba reaction [11]. No evidence for a long-lived state was found in the off-beam range from 10–300 μ s with respect to the beam pulse. Later, a J = (31/2) state at $E_x = 4255$ keV was observed to be isomeric with a half-life of $T_{1/2} = 5(2)$ ns according to the time distribution of the depopulating 552-keV γ ray [12]. The level scheme of ¹³⁷Ce was extended up to highest spins via ¹⁸O + ¹²⁴Sn [13] and ¹³C + ¹³⁰Te [14] reactions. To date, only a $J^{\pi} = 23/2^+$ state above $E_x = 3$ MeV is reported. It is much higher in excitation energy than in the other N = 79 isotones and disrupts the systematics (c.f. Fig. 1).

First spectroscopic data on the elusive $J^{\pi} = 23/2^+$ isomer in ¹³⁹Nd were reported by Müller-Veggian et al. [15] employing a ¹⁴⁰Ce(α , 5n) reaction. The level scheme above the $J^{\pi} = 11/2^{-}_{1}$ isomer was extended to an excitation energy of approximately 4 MeV. Delayed γ rays deexciting the $J^{\pi} = 19/2^+_1$ state were observed in off-beam $\gamma \gamma$ -coincidence spectra. Based on the decay curve, a half-life limit of $T_{1/2}$ > 141 ns was deduced. Later, the isomer's excitation energy was constrained to be above the $J^{\pi} = 19/2^+_1$ state and a precise half-life of $T_{1/2} = 272(4)$ ns could be obtained [7]. However, the isomer could not unambiguously place in the level scheme. Finally, in 2013, a recoil-decay tagging experiment at the Jyväskylä accelerator facility confirmed the previous half-life measurement [3]. The authors observed feeding transitions from the decay of three higher-lying $J^{\pi} = (25/2^{-})$ states allowing for a placement of the isomeric $J^{\pi} = (23/2^+)$ state in the level scheme at $E_x = 2616$ keV, only 44 keV above the $J^{\pi} = 19/2^+$ state. However, that 44-keV transition is still unobserved. Towards the subshell closure at Z = 64, detailed high-spin structure information is available for ¹⁴¹Sm [16,17] and ¹⁴³Gd [17–19]; no high-lying isomeric states were observed.

The onset of isomerism as a function of the proton number along the N = 79 chain (see Fig. 1) motivates a refined investigation of isomeric $J^{\pi} = 23/2^+$ states in ¹³³Xe and ¹³⁵Ba. The available data on low-spin states in ¹³³Xe mainly originate from β -decay studies of ¹³³I [20]. The $J^{\pi} = 11/2_1^-$ isomer at 233 keV with a $\nu h_{11/2}^{-1}$ neutron-hole configuration has a half-life of 2.198(13) *d* [21]. First results on the high-spin structure were obtained by Lönnroth *et al.* [22] via α -induced reactions on ¹³⁰Te at beam energies of 14.1–18 MeV. Three γ rays with energies of 247.4, 947.8, and 695.2 keV were placed above the $J^{\pi} = 11/2_1^-$ isomer to form a $(23/2^-) \rightarrow$ $19/2_1^- \rightarrow 15/2_1^- \rightarrow 11/2_1^-$ cascade.

Recently, the high-spin regime of 133 Xe was extended via 136 Xe + 208 Pb and 136 Xe + 198 Pt multinucleon-transfer reactions employing the Advanced GAmma Tracking Array (AGATA) coupled to the magnetic spectrometer PRISMA and the GAMMASPHERE spectrometer in combination with the gas-filled detector array CHICO, respectively [5]. A 1253-468-465-keV prompt triple coincidence was observed to form

a band unconnected to any known states in ¹³³Xe. According to the time structure in the GAMMASPHERE data set, a long-lived isomer with $T_{1/2} \gg 1 \ \mu$ s was proposed at $E_x = 2107 + x$ keV.

High-spin states in ¹³⁵Ba above the $J^{\pi} = 11/2^{-}_{1}$ isomer $(T_{1/2} = 28.7 \text{ h} [23])$ were investigated by Che *et al.* [24]. Excited states were populated up to excitation energies of 5.8 MeV using a 130 Te(9 Be, 4n) 135 Ba reaction at 45 MeV. A 1184-254 keV cascade was observed to feed the $J^{\pi} = 15/2^{-1}_{1}$ state at $E_x = 950$ keV. The 2134-keV state was identified as the $J^{\pi} = 19/2^{-}_{2}$ state, while no spin assignment was given for the 2388-keV state. Moreover, no decay from higher-lying states into the 2388-keV state was observed. Later, a first tentative spin assignment of $J^{\pi} = 21/2^{(-)}$ was proposed for the 2388-keV state [25]. A high-spin investigation by Kumar *et al.* extended the level scheme with 20 new γ rays [26]. Directional correlation measurements confirmed the spin and parity assignments of the $J^{\pi} = 19/2_2^-$ state and indicated a tentative J = (23/2) spin assignment for the 2388-keV state. Even though detailed data are available up to highest spins and excitation energies, no feeding γ ray to the 2388-keV state was found to date. This observation corroborates the existence of a long-lived $J = 23/2^+_1$ isomer in ¹³⁵Ba.

In this paper, we report and discuss new results on isomeric $J^{\pi} = 23/2^+$ states in the N = 79 isotones ¹³³Xe and ¹³⁵Ba obtained in two different experiments. ¹³⁵Ba was populated in a 136 Xe + 208 Pb multinucleon-transfer (MNT) experiment employing the high-resolution position-sensitive Advanced GAmma Tracking Array (AGATA) [27] in combination with the magnetic mass spectrometer PRISMA [28-30]. In a fusion-evaporation experiment, both ¹³³Xe and ¹³⁵Ba were investigated with the HORUS γ -ray array [31] at the Institute of Nuclear Physics, University of Cologne, employing a pulsed 40-MeV ⁹Be beam impinging onto a ¹³⁰Te target. This paper is organized as follows: the experimental setup and data analysis of the two experiments are described in Sec. II, followed by the experimental results in Sec. III. A detailed comparison with shell-model calculations is presented in Sec. IV before the paper closes with a summary and conclusions.

II. EXPERIMENTAL PROCEDURE AND DATA ANALYSIS

A. ¹³⁶Xe + ²⁰⁸Pb multinucleon transfer

¹³⁵Ba was populated in a ¹³⁶Xe + ²⁰⁸Pb multinucleontransfer experiment at the Laboratori Nazionali di Legnaro, Italy. In this experiment, a 6.84 MeV/nucleon ¹³⁶Xe beam, accelerated by the PIAVE+ALPI accelerator complex, impinged onto a 1-mg/cm² ²⁰⁸Pb target. The Advanced GAmma Tracking Array (AGATA) [27] in a first demonstrator configuration [32] was placed at a distance of 18.8 cm from the target position to measure γ rays from excited states. The array consisted of nine large-volume electronically segmented high-purity Ge (HPGe) detectors in three triple cryostats [33]. An isotopic identification of the nuclei of interest was provided by the magnetic spectrometer PRISMA placed at the reaction's grazing angle of $\theta_{lab} = 42^{\circ}$. An event registered by the PRISMA focal-plane detector in coincidence with an AGATA event was taken as a trigger for the data acquisition. Pulse-shape analysis of the digitized detector signals was applied to determine the individual interaction points within the HPGe shell [34], enabling the Orsay forward-tracking algorithm [35] to reconstruct the individual emitted γ -ray energies, determine the first interaction point of the γ ray in the germanium and, thus, the emission angle. Together with the kinematic information from PRISMA, a precise Doppler correction was performed. Further details on the analysis can be found in Refs. [36,37].

B. ⁹Be + ¹³⁰Te fusion-evaporation reaction

In a second experiment, ¹³³Xe and ¹³⁵Ba were populated in a ¹³⁰Te + ⁹Be fusion-evaporation reaction. The FN Tandem accelerator of the Institute of Nuclear Physics, University of Cologne delivered pulsed 40-MeV ⁹Be beams with two different repetition rates onto an enriched ¹³⁰Te target with a thickness of 1.8 mg/cm² evaporated onto a 120-mg/cm² thick Bi backing plus a 132-mg/cm² thick Cu layer for heat dissipation. Approximately 95% of the reaction products were stable nuclei, stopped inside the Bi backing. The pulsing system was placed at the injection line of the FN Tandem accelerator and comprises five deflectors aligned parallel to the beam axis. The electric potential of one side of the deflectors was grounded, while the electrical potential of the opposite side was alternating between ground level and 1.3 kV.

The first pulsed beam had a pulse width of 75 ms and a repetition rate of 3.33 Hz. To exclude the background from β -decay channels and longer-lived isomers, a second pulsed beam was employed with a pulse width of 3.75 s and a repetition rate of 66.66 mHz. γ rays were measured using the HORUS array [31] comprising 14 HPGe detectors, six of them equipped with BGO Compton-suppression shields. The detectors were positioned on the eight corners and six faces of a cube. γ events were processed triggerless and recorded utilizing the synchronized 80-MHz XIATM Digital Gamma Finder (DGF) data-acquisition system. In addition, a reference signal given by the pulsing system was recorded.

The data were sorted into (i) a two-dimensional $\gamma - \gamma$ matrix with a time gate of 250 ns between coincident γ events, (ii) a two-dimensional γ -t matrix to gate on different time windows relative to the reference pulse, and (iii) a total of three group matrices each corresponding to detector pairs with relative angles $\Theta = \{54.7^\circ, 70.4^\circ, 90^\circ\}$ for off-beam angularcorrelation measurements using the SOCO-V2 code [38]. In total, $7.1 \times 10^7 \gamma \gamma$ -coincidence events and $1.2 \times 10^9 \gamma$ -t events were collected.

Spins and parities of populated states in the HORUS experiment are investigated in the off-beam measurement with the $\gamma\gamma$ angular-correlation code CORLEONE [39,40] based on the phase convention by Krane, Steffen, and Wheeler [41,42]. Different hypotheses of involved spins J_1, J_2, J_3 and multipole-mixing ratios δ_1, δ_2 of two coincident γ rays in a cascade $J_1 \xrightarrow{\delta_1} J_2 \xrightarrow{\delta_2} J_3$ are evaluated by χ^2 fits of the correlation function $W(J_1, \delta_1, J_2, \delta_2, J_3, \Theta, \sigma)$ to experimental correlation intensities for the three angular-correlation groups. θ_1 and θ_2 are the angles between beam axis and detectors; $\Theta = \theta_1 - \theta_2$ denotes the relative angle of a detector

pair. A deorientation from the beam axis is taken into account by increasing the value of σ .

III. RESULTS

Partial level schemes of excited states in ¹³³Xe and ¹³⁵Ba, which are discussed in this paper, are displayed in Figs. 2(a) and 2(b). The determined half-lives of isomeric states in ^{132,133}Xe and ^{135,136}Ba are summarized in Table I.

The Doppler-corrected beamlike singles γ -ray spectrum gated on ¹³⁵Ba from the ¹³⁶Xe + ²⁰⁸Pb AGATA experiment is shown in Fig. 3(a). Random background is significantly suppressed by gating on the prompt peak in the time-difference distribution between AGATA and PRISMA. Prominent transitions are marked with labels. The decays of the $J^{\pi} = 19/2_1^{-1}$ and $15/2_1^-$ states at energies of 1052 and 682 keV are clearly visible as dominant peaks in the spectrum. Transitions in the positive-parity dipole band, on top of the $J^{\pi} = 21/2^+_2$ state at $E_x = 3083$ keV are observed well above the background. The highest excitation energy identified in the ¹³⁵Ba reaction channel corresponds to the $J^{\pi} = 31/2^+$ state at $E_x =$ 4696 keV. The insets Figs. 3(b) and 3(c) show magnifications into the measured γ -ray spectrum around the γ -ray energies of the expected decays of the $J^{\pi} = 23/2^+$ state at 254 keV and around the decay of the $J^{\pi} = 19/2^{-}_{2}$ state at 1184 keV, respectively. The 1184-keV transition is clearly visible in the prompt AGATA spectrum, however, the 254-keV feeding transition is absent. This observation suggests that the half-life of the 2388-keV state is significantly longer compared to the width of the prompt peak in the time-difference spectrum between PRISMA and AGATA, i.e., $\Delta t_{\text{PRISMA}-\text{AGATA}} \approx 16$ ns. Consequently, the observation of the 1184-keV transition accompanied by the absence of the 254 keV feeding transition, despite the observation of other high-spin bands, indicates an isomeric character of the $E_x = 2388$ keV state.

In the first part of the HORUS experiment, the beam pulse width was set to 75 ms, followed by a 225-ms time window for off-beam measurements. The recorded reference time at the beginning of the beam flash allows us to gate on different off- and in-beam time windows. In particular, gates within the time window between 75 and 300 ms with respect to the reference pulse restrict the γ -ray spectrum to the off-beam measurement. Figures 3(d) and 3(f) show γ -ray spectra obtained with different time windows. The γ -time matrices with the applied gates are shown in inset Figs. 3(e) and 3(g). In the matrix a distinct separation between in-beam and off-beam γ -ray spectrum is visible at 75 ms relative to the reference pulse.

In order to validate the experimental procedure, several well-known long-lived millisecond isomers were investigated. By gating on the time window $\Delta t = 80-90$ ms [Fig. 3(d)], delayed transitions at energies of 174, 538, 600, 668, and 773 keV, forming a cascade below the $J^{\pi} = 10^{+}_{1}$ isomer in ¹³²Xe, are clearly enhanced in the γ -ray spectrum. Furthermore, the spectrum exhibits the 1048-keV $4^{+}_{1} \rightarrow 2^{+}_{1}$ and 819-keV $2^{+}_{1} \rightarrow 0^{+}_{1}$ transitions originating from the $J^{\pi} = 7^{-}_{1}$ isomer in ¹³⁶Ba. The peaks at 231, 948, and 695 keV are mutually coincident and identified as the decay cascade of the $J^{\pi} = 23/2^{+}_{1}$ state in ¹³³Xe. A background-subtracted

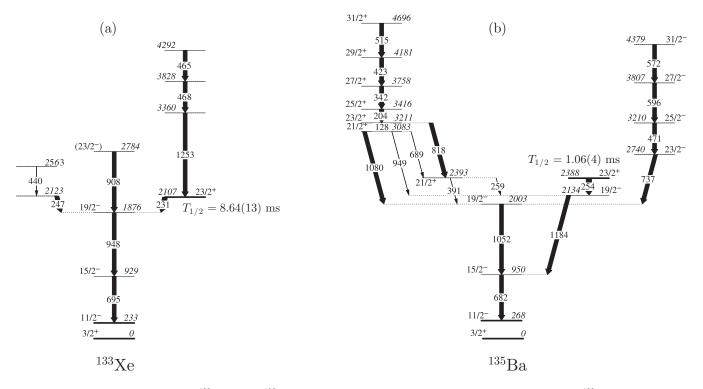


FIG. 2. Partial level schemes of (a) ¹³³Xe and (b) ¹³⁵Ba. The reduced transition strengths of the 231-keV transition in ¹³³Xe and the 254-keV transition in ¹³⁵Ba are subject of this paper. Dominating transitions in the HORUS fusion-evaporation experiment are presented with thicker arrows.

in-beam prompt $\gamma\gamma$ -coincidence spectrum with a gate on the 1253-keV transition in ¹³³Xe is shown in Fig. 4. Coincident transitions at energies of 465 and 468 keV are forming a 1253-468-465 keV cascade on top of the $J^{\pi} = 23/2^+$ isomer confirming the observation in Ref. [5]. Other lines at 197, 847, 1039, and 1239 keV originate from the ¹⁹F($n, n'\gamma$) reactions and the β decay of ⁵⁶Mn into ⁵⁶Fe.

The delayed transitions in ^{132,133}Xe and ¹³⁶Ba are also visible in the spectrum gated on the time window $\Delta t = 75$ -80 ms in Fig. 3(f). Based on the AGATA data set, a pronounced delayed 254-1184-682-keV γ -ray cascade in ¹³⁵Ba is expected. The observation of this cascade in the off-beam spectrum

in Fig. 3(f) clearly confirms the presence of an isomer in this nucleus. The absence of the cascade in the spectrum in Fig. 3(d) implies that the isomer in 133 Xe has a longer half-life compared to the similar state in 135 Ba.

Figures $5(a_{1,2})-5(c_{1,2})$ show fits of well-known halflives of isomeric states in ¹³⁶Ba and ¹³²Xe. The fit function of the time spectrum N(t) is chosen as $N(t) = a \exp[t \ln(2)/T_{1/2}] + b$ with *a* and *b* as free parameters. The decay chain deexciting the $J^{\pi} = 7^{-}$ isomer in ¹³⁶Ba is observed in the seconds-range pulsed-beam experiment. The corresponding background-subtracted time projection of the $2_1^+ \rightarrow 0_1^+$ transition at $E_{\gamma} = 819$ keV and the fitted decay

TABLE I. Measured half-lives of selected isomers observed in the ${}^{9}Be + {}^{130}Te$ experiment. The different columns indicate the nucleus, repetition rate of the pulsed beam, excitation energy, spin and parity of the isomeric state, the energy of the γ ray used to determine the half-life, the deduced weighted mean half-life, and previous results reported in the literature.

Isotope	Repetition rate (Hz)	E_i (keV)	$J^{\pi}_i(\hbar)$	E_{γ} (keV)	$T_{1/2}$		
					Present work	Literature	
¹³⁶ Ba	0.066	2031	7-	819	0.296(7) s	0.3084(19) s [43]	
						0.303(2) s [44] 0.37(5) s [45]	
¹³² Xe	3.33	2752	10^{+}	174, 538, 600, 668, and 773	8.37(8) ms	0.32(2) s [46] 8.39(11) ms [47]	
						8.4(8) ms [48] 8.2(6) ms [49,50]	
¹³³ Xe	3.33	2107	$23/2^+$	231, 695, and 948	8.64(13) ms	-	
¹³⁵ Ba	3.33	2388	$23/2^+$	254, 682, and 1184	1.06(4) ms	_	

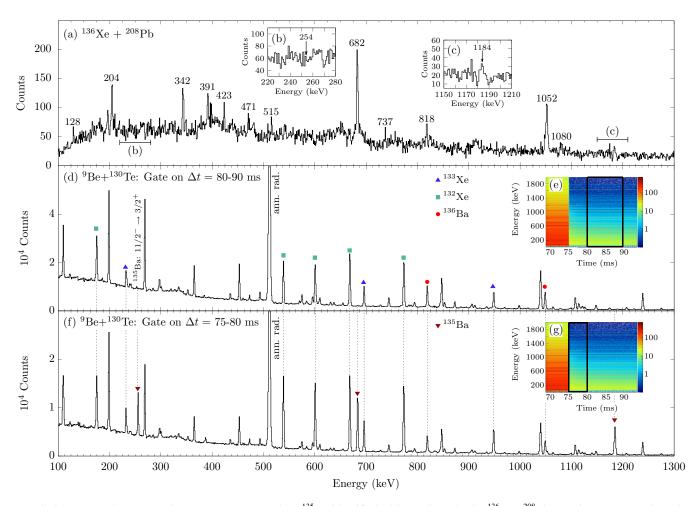


FIG. 3. (a) Doppler-corrected γ -ray spectrum gated on ¹³⁵Ba identified with PRISMA in the ¹³⁶Xe+²⁰⁸Pb experiment. Insets show the zoomed spectrum around the expected transitions at (b) 254-keV and (c) 1184-keV. (d) Projection of the γ -t matrix gated on a time window between 80 and 90 ms relative to the reference time at the beginning of the beam flash. (f) Similar data for a gate on a time window between 75 and 80 ms. Delayed transitions below the $J^{\pi} = 23/2_1^+$ isomers in ¹³³Xe, ¹³⁵Ba, and below the $J^{\pi} = 10_1^+$ isomer in ¹³²Xe are marked with symbols and dashed lines to guide the eye. Both insets (e) and (g) present the γ -t matrix relative to the reference time. The applied time gates are surrounded by black boxes.

curve are shown in Fig. $5(a_1)$. For the sake of completeness, a similar plot with a logarithmic scale is shown in the inset Fig. $5(a_2)$. The measured half-life of $T_{1/2} = 0.296(7)$ s is in good agreement with previously measured values [44–46]. The absolute fit residual, defined as difference between absolute experimental value and fit function, is presented in

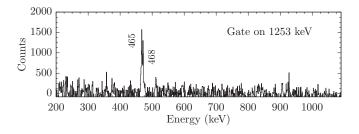


FIG. 4. Prompt in-beam $\gamma\gamma$ coincidence spectrum with a gate on the 1253-keV transition in ¹³³Xe above the $J^{\pi} = 23/2^+$ isomer. Coincidences at energies of 465 and 468 keV are visible.

Fig. 5(a₃). In addition, fits of the background-subtracted time projections of the 538-keV and 668-keV transitions, depopulating the $J^{\pi} = 10^+$ isomer in ¹³²Xe, are depicted in Fig. 5(b_{1,2}) and Fig. 5(c_{1,2}). A small constant background remains after background subtraction in the time distribution of the $2_1^+ \rightarrow 0_1^+$ 668 keV transition due to a weak feeding from β decays of ¹³²I and ¹³²Cs. Both independently determined half-lives are in excellent agreement with the previous values [47–50]. The consistency between the literature values and the current analysis demonstrates the reliability of the analysis.

The background-subtracted time distributions of the 231-, 947-, and 695-keV transitions in ¹³³Xe are presented in Figs. $5(c_{1,2})$, $5(d_{1,2})$, and $5(e_{1,2})$. Exponential fits of the slope components yield respective half-lives of 8.62(13), 8.60(9), and 8.68(8) ms. The constant random background is determined separately and incorporated into the fit. The independently determined half-lives utilizing the three different gate conditions show excellent agreement. Systematic errors from uncertainties in the determination of the background

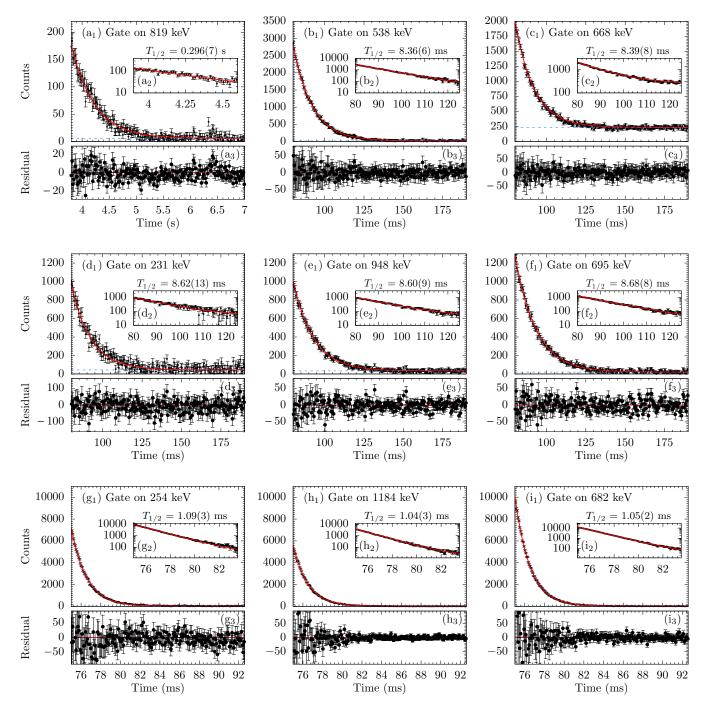


FIG. 5. Gates on background-subtracted γ -time matrices and half-life fits for the gating conditions (a₁₋₂) 819 keV in ¹³⁶Ba measured in the seconds-pulsing experiment, (b₁₋₂) 538 keV and (c₁₋₂) 668 keV in ¹³²Xe, (d₁₋₂) 231 keV, (e₁₋₂) 947 keV, and (f₁₋₂) 695 keV in ¹³³Xe, (g₁₋₂) 254 keV, (h₁₋₂) 1184 keV, and (i₁₋₂) 682 keV in ¹³⁵Ba obtained in the milliseconds-pulsing experiment. The corresponding residual, defined as difference between absolute value and fit function, is shown in panels (a₃), (b₃), (c₃), (d₃), (g₃), (f₃), (g₃), (h₃), and (i₃), respectively. Half-lives are determined from exponential fits of the delayed component. The fit is drawn with a solid red line. Random background is determined separately (dashed blue line) and incorporated into the fit model.

are taken into account. The final weighted mean value of $T_{1/2} = 8.64(13)$ ms is newly established for the $J^{\pi} = 23/2^+$ state in ¹³³Xe.

Background subtracted time spectra of transitions deexciting the state at $E_x = 2388$ keV in ¹³⁵Ba, fits, and corresponding residuals are presented in Figs. 5(f₁)-5(h₃). The fit for the 254-keV transition yields a half-life of 1.09(3) ms. Independently determined half-lives involving the 1184-keV [1.04(3) ms], and the 682-keV [1.05(2) ms] γ ray are in mutual agreement. The final weighted mean half-life of the $J^{\pi} = 23/2^+$ state in ¹³⁵Ba is measured to be $T_{1/2} = 1.06(4)$ ms taking into account systematic errors.

According to systematics and shell-model arguments, a direct single-step decay of the 2107 + *x*-keV band head of the 465-468-1253-keV cascade in ¹³³Xe via a 231-keV transition was slightly favored in the previous work [5]. However, a decay via an unobserved low-energy transition similar to ¹²⁹Sn and ¹³⁹Nd could not be ruled out. Internal conversion coefficients and angular-correlation measurements were carried out to clarify the decay patterns in ¹³³Xe and ¹³⁵Ba. Since conversion electrons are not directly detected, the internal conversion coefficient α_T is determined via the intensity-balance method described in Ref. [52]. In the off-beam measurement the isomer in ¹³³Xe decays via the 231-948-695 cascade towards the $J^{\pi} = 11/2^{-}$ state. Therefore, the intensities of the 231 and 948-keV transitions, corrected for detector efficiency and internal conversion, are equal in the delayed γ -ray spectrum:

$$I_{\gamma_1}(1 + \alpha_{\gamma_1}) = I_{\gamma_2}(1 + \alpha_{\gamma_2}), \tag{1}$$

where $I_{\gamma_{1,2}}$ are the efficiency-corrected γ -ray intensities and $\alpha_{\gamma_{1,2}}$ are the total internal-conversion coefficients (ICCs). The off-beam intensities $I_{948 \text{ keV}}$ and $I_{231 \text{ keV}}$ are extracted from the γ -ray spectra of the 14 HPGe detectors by gating on the offbeam time window with a time gap of 100 ns from the in-beam part to exclude possible feeding from short-lived components. Using the weighted arithmetic mean of the 14 measurements and the well-established E2 character of the 948 keV transition ($\alpha_{948} = 0.00182$ [51]), a value of $\alpha_{231} = 0.49(9)$ is obtained for the 231-keV transition. Based on a comparison with theoretical α_T values [51], presented in Fig. 6(a), the multipolarity of the 231-keV transition can be restricted to an M2 or E3 character. Applying the same method to the 254-1184-keV cascade in ¹³⁵Ba, a value of $\alpha_{254} = 0.32(7)$ for the 254 keV transition is computed. Again, a comparison with theoretical values shown in Fig. 6(b) yields a good agreement with M2 or E3 multipolarities for the 254-keV γ ray.

Angular-correlation measurements provide a complementary approach to the internal conversion coefficient measurement. Figures 6(c)-6(e) show comparisons of theoretical angular-correlation functions $W(J_1, \delta_1, J_2, \delta_2, J_3, \Theta, \sigma)$ (colored lines) with experimentally obtained relative intensities in three different correlation groups. A fit of the $2^+_2 \rightarrow 2^+_1$ 1120keV transition in ²¹⁴Po, measured in the energy calibration run with a ²²⁶Ra source, is shown in Fig. 6(c). The determined multipole-mixing ratio of $\delta = 0.19(6)$ agrees well with the evaluated multipole-mixing ratio of $\delta_{\text{lit.}} = 0.18(2)$ [53]. The corresponding angular-correlation fit of the 231-keV transition, gated on the 948-keV transition in ¹³³Xe, is presented in Fig. 6(d). The multipolarity of the 948-keV γ ray is fixed to be an E2 transition, while different spin hypotheses of the 2107keV state are tested. Combined with the internal conversion coefficient measurement, a spin assignment of $J^{\pi} = 23/2^+$ and a multipole-mixing ratio of $\delta_{23/2^+ \rightarrow 19/2^-} = -0.021(10)$ is most likely for the 2107-keV state. The small value of the multipole-mixing ratio indicates a dominant M2 contribution and a small E3 admixture in the $\Delta J = 2$ transition.

Spin hypotheses for the 2388-keV state in ¹³⁵Ba are tested by employing the same angular-correlation method. In Fig. 6(e) experimentally determined intensities of the 254-keV γ ray in the different correlation groups, gated on the 1184-keV transition, are compared to theoretical intensities.

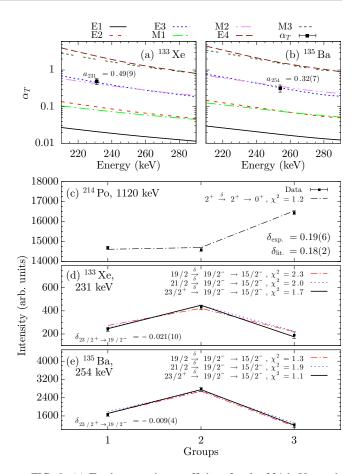


FIG. 6. (a) Total conversion coefficient for the 231-keV transition in ¹³³Xe compared with predicted values from the BrIcc v2.3 database [51]. (b) Similar comparison for the 254-keV transition in ¹³⁵Ba. The multipolarity of the 231 and 254-keV transition can be restricted to M2/E3 character. $\gamma\gamma$ off-beam angular correlations for (c) the known 1120-609-keV cascade in ²¹⁴Po, (d) the 231-948-keV cascade in ¹³³Xe, and (e) the 254-1184-keV cascade in ¹³⁵Ba. Experimental values (black points) are compared to calculated angular-correlation functions $W(J_1, \delta_1, J_2, \delta_2, J_3, \Theta, \sigma)$ (lines) for three correlation groups.

Again, the $23/2^+ \stackrel{\delta}{\rightarrow} 19/2^- \rightarrow 15/2^-$ hypothesis (solid line) with $\delta_{23/2^+ \rightarrow 19/2^-} = -0.009(4)$ yields the best agreement. The small multipole-mixing ratio indicates a dominating *M*2 character of the 254-keV transition. Nevertheless, based on the fit results of this work, a spin assignment of J = 19/2 $(\chi^2 = 1.9)$ or 21/2 $(\chi^2 = 1.3)$ cannot be excluded either. However, the internal conversion coefficient measurement shown in Fig. 6(b) suggests a $J^{\pi} = 23/2^+$ spin assignment. This argument is further supported by the previous results of Ref. [26], where both spin assignments J = 19/2 and J = 21/2 are excluded.

Internal-conversion coefficients are calculated employing the newly determined multiple-mixing ratios δ via the following expression [54]:

$$\alpha_T = \frac{\alpha_T(M2) + \delta^2 \alpha_T(E3)}{1 + \delta^2}, \qquad (2)$$

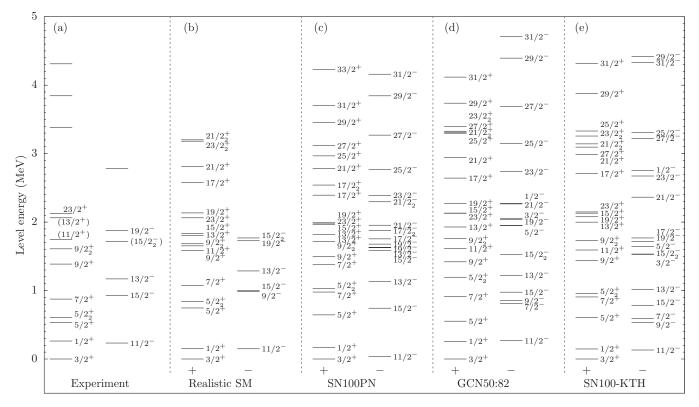


FIG. 7. Comparison of experimental energy spectra of 133 Xe [left panel, (a)] with the results of shell-model calculations employing the (b) Realistic SM, (c) SN100PN, (d) GCN50:82, and (e) SN100-KTH interaction. Note that the states are separated into columns for the negative- and the positive-parity states.

where $\alpha_T(M2)$ and $\alpha_T(E3)$ are theoretical ICC values. The calculated values $\alpha_T = 0.421(6)$ for ¹³³Xe and $\alpha_T = 0.364(5)$ for ¹³⁵Ba are in good agreement with the independently measured ICC values, showing the complementarity between both approaches.

IV. DISCUSSION

The experimentally obtained isomer excitation energies, half-lives and corresponding reduced transition probabilities in 133 Xe and 135 Ba are compared to shell-model theory. All shell-model calculations were carried out in an untruncated *gdsh* valence space outside doubly magic 100 Sn, employing the shell-model code NUSHELLX@MSU [55], the massive-parallelization code KSHELL [56] and the ANTOINE shell-model code [57].

The first calculation is conducted in the framework of the realistic shell model [58,59], denoted as realistic SM. Singleparticle energies and two-body effective interaction are determined from the established CD-Bonn free nucleon-nucleon potential using the $V_{\text{low-}k}$ approach with a cutoff momentum of $\Lambda = 2.6 \text{ fm}^{-1}$, plus the Coulomb force for protons. The effective shell-model Hamiltonian is derived iteratively by means of the many-body perturbation theory in the \hat{Q} -box folded diagram expansion, including all diagrams up to third order in the interaction.

Another calculation is carried out with the jj55pn Hamiltonian (referred to as the SN100PN interaction) [60]. The Hamiltonian consists of four terms covering the neutronneutron, neutron-proton, proton-proton, and Coulomb repulsion between the protons individually. A renormalized *G* matrix derived from the CD-Bonn interaction [61] was employed to construct the realistic two-body residual interaction. The proton and neutron single-particle energies are based upon the energy levels in ¹³³Sb and ¹³¹Sn.

A third calculation is performed utilizing the effective interaction GCN50:82 [62,63]. Similar to the SN100PN interaction, the interaction is derived from a realistic *G* matrix based on the CD-Bonn potential. Empirical monopole corrections to the original *G* matrix are introduced by fitting different combinations of two-body matrix elements to sets of experimental excitation energies from even-even and even-odd semimagic nuclei.

The last calculation, hereinafter referred to as SN100-KTH, leverages the realistic CD-Bonn interaction as well. The T = 1 part of the monopole interaction was corrected via the Monte Carlo global optimization approach by fitting several low-lying yrast states in Sn isotopes. A renormalization was performed by a perturbative *G* matrix approach to include core-polarization effects. It was shown that the calculations reproduce well the excitation energies and *E*2 transition probabilities in even-even Te isotopes [64,65].

A comparison of [Fig. 7(a)] experimental energy spectrum of 133 Xe with the results of [Fig. 7(b)] realistic SM, [Fig. 7(c)] SN100PN, [Fig. 7(d)] GCN50:82, and [Fig. 7(e)] SN100-KTH shell-model calculations is shown in Fig. 7. The states are separated into columns for the negative- and the positive-parity states. All four calculations reproduce the spin

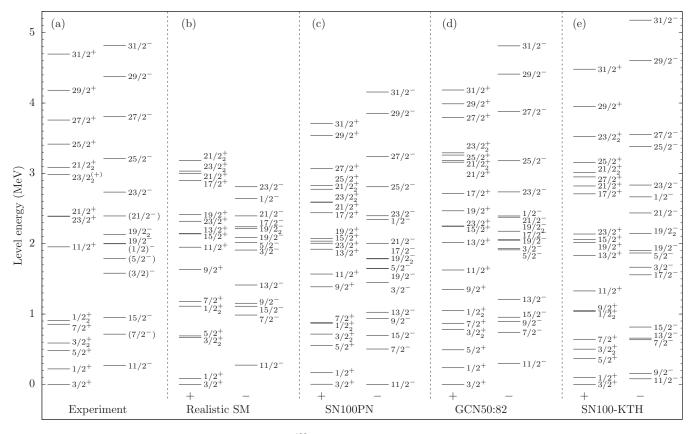


FIG. 8. Comparison of experimental energy spectra of 135 Ba [left panel, (a)] with the results of shell-model calculations employing the (b) Realistic SM, (c) SN100PN, (d) GCN50:82, and (e) SN100-KTH interactions. The arrangement of the states mirrors the layout in Fig. 7.

of the $J^{\pi} = 3/2^+$ ground state. The GCN50:82 interaction slightly overpredicts the $E_x = 233$ -keV $J^{\pi} = 11/2_1^-$ state by 37 keV while the realistic SM, SN100PN, and SN100-KTH interactions place the $J^{\pi} = 11/2_1^-$ state 84, 198, and 102 keV too low in excitation energy, respectively. All interactions show a good agreement for the low-spin positive-parity states below 1 MeV.

The 948-, and 695-keV γ -ray transitions, forming the $19/2_1^- \rightarrow 15/2_1^- \rightarrow 11/2_1^-$ cascade, are calculated as 726 and 852 keV using realistic SM, 883 and 707 keV using SN100PN, 977 and 706 keV using GCN50:82, and as 939 and 649 keV using SN100-KTH, respectively. The calculated excitation energy of the isomeric $J^{\pi} = 23/2_1^+$ state is in excellent agreement with the experimental value exhibiting deviations of only 45 (realistic SM), 134 (SN100PN), 5 (GCN50:82), and 24 keV (SN100-KTH). Additionally, the $23/2_1^+ \rightarrow 19/2_1^-$ transition is computed as $E_{\gamma} = 335$ keV (realistic SM), $E_{\gamma} = 348$ keV (SN100-KTH), compared to the observed 231-keV γ -ray transition in the experiment.

The level structure of the +2p isotone ¹³⁵Ba is more intricate. A comparison of [Fig. 8(a)] experimental energy spectra of ¹³⁵Ba with the shell-model results of [Fig. 8(b)] realistic SM, [Fig. 8(c)] SN100PN, [Fig. 8(d)] GCN50:82, and [Fig. 8(e)] SN100-KTH calculations are presented in Fig. 8. Again, the states are separated into columns for negative- and positive-parity states. The $J^{\pi} = 3/2_1^+$ ground state is well reproduced by the realistic SM, GCN50:82 and SN100-KTH interactions. However, the SN100PN interaction locates the $J^{\pi} = 3/2_1^+$ state 3 keV above the $J^{\pi} = 11/2_1^-$ state. The other three interactions compute the $J^{\pi} = 11/2_1^-$ state ($E_x = 268 \text{ keV}$) to have excitation energies of 274 (realistic SM), 297 (GCN50:82), and 79 keV (SN100-KTH). The interactions yield a good reproduction of the experimentally determined positive low-spin regime below 1 MeV excitation energy.

The interactions reproduce the $19/2_1^- \rightarrow 15/2_1^- \rightarrow 11/2_1^$ cascade with γ -ray energies of 1052 and 682 keV very well. Deviations amount to 73 and 155 keV (Realistic SM), 105 and 16 keV (SN100PN), 43 and 26 keV (GCN50:82), as well as 37 and 54 keV (SN100-KTH). In the experiment the energy difference between the first and second excited $J^{\pi} = 19/2^{-1}$ states is 131 keV, compared to the calculations of 123 (realistic SM), 139 (SN100PN), 128 (GCN50:82), and 243 keV (SN100-KTH). The calculated excitation energies for the first and second excited $J^{\pi} = 23/2^+$ states of 2320/3032 (realistic SM), 2007/2668 (SN100PN), 2252/3260 (GCN50:82), and 2138/3523 keV (SN100-KTH) are in good agreement with the experimentally determined $E_x = 2388/2985$ keV. Additionally, the $23/2_1^+ \rightarrow 19/2_2^-$ transition is computed as $E_{\gamma} = 126$ keV (realistic SM), $E_{\gamma} = 223$ keV (SN100PN), and $E_{\gamma} = 74$ keV (GCN50:82), compared to the observed 254-keV γ -ray transition in the experiment. Nonetheless, the SN100-KTH interaction is the only interaction, which computes the $J^{\pi} = 19/2_2^-$ state slightly above the $J^{\pi} = 23/2_1^+$ state.

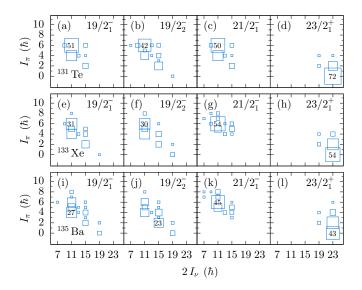


FIG. 9. Decomposition of the total angular momentum $I = I_{\pi} \otimes I_{\nu}$ into its proton and neutron components for the $J^{\pi} = 19/2_{1}^{-}$, $19/2_{2}^{-}$, $21/2_{1}^{-}$, and $23/2_{1}^{-}$ states in (a)–(d) ¹³¹Te, (e)–(h) ¹³³Xe, and (i)–(l) ¹³⁵Ba calculated with the GCN50:82 interaction. Strongest components are labeled with corresponding percentages.

The nuclear structures along the N = 79 isotones closely resemble each other. Figures 9(a)-9(1) show the decomposition of the total angular momentum $I = I_{\pi} \otimes I_{\nu}$ into its proton and neutron components for selected states using the GCN50:82 interaction. The decompositions are very similar to those computed by the SN100PN and SN100-KTH interactions. Although being more fragmented going from ¹³¹Te to ¹³⁵Ba, the spin decompositions of the high-spin states above the $J^{\pi} = 11/2_1^-$ state are similar. In ¹³¹Te and ¹³³Xe, the $J^{\pi} = 23/2_1^+$ state decays into the yrast $J^{\pi} = 19/2_1^-$ state, while in ¹³⁵Ba it decays into another yrare $J^{\pi} = 19/2^-$ state. Nevertheless, the spin decomposition of the first and second excited $J^{\pi} = 19/2^-$ states are almost identical.

The interaction predicts the $J^{\pi} = 23/2_1^+$ state to predominantly have (54% ¹³³Xe; 43% ¹³⁵Ba) $\nu 23/2^+ \otimes \pi 0^+$ and (32%; 37%) $\nu 23/2^+ \otimes \pi 2^+$ stretched neutron spin configurations. On the other hand, the $J^{\pi} = 19/2^-$ states in both ¹³³Xe and ¹³⁵Ba are mostly assigned to configurations with neutron spin $I_{\nu} = 11/2$ coupled to proton spins of $I_{\pi} = 4$ and $I_{\pi} = 6$. These configuration differences provide a microscopic reason of the long-lived $J^{\pi} = 23/2^+$ states; their decays require a considerable reordering of angular momentum for protons and neutrons, which strongly hinders a transition between both states.

The isomeric character is also scrutinized via a detailed decomposition of the $J^{\pi} = 19/2^{-}$, and $23/2^{+}$ states of the N = 79 isotones ¹³¹Te, ¹³³Xe, and ¹³⁵Ba into their proton and neutron configurations computed by the GCN50:82 interaction, presented in Figs. 10(a)–10(f). The wave functions of the $J^{\pi} = 23/2_{1}^{+}$ states are dominated by the neutron $v(h_{11/2}^{-2}d_{3/2}^{-1})$ configuration with probabilities of 81.3% (¹³¹Te), 60.3% (¹³³Xe), and 44.0% (¹³⁵Ba). Also the SN100PN and SN100-KTH calculations yield a dominant $v(h_{11/2}^{-2}d_{3/2}^{-1})$ neutron configuration.

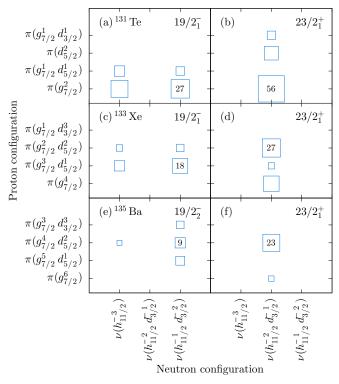


FIG. 10. Decomposition of the $J^{\pi} = 19/2^{-}$ and $23/2^{+}$ states of (a),(b) ¹³¹Te, (c),(d) ¹³³Xe, and (e),(f) ¹³⁵Ba into their proton and neutron configurations computed by the GCN50:82 interaction. Strongest components are labeled with corresponding percentages.

In contrary, with GCN50:82, the leading neutron configurations of the final $J^{\pi} = 19/2^{-}$ state are $vh_{11/2}^{-3}$ and $v(h_{11/2}^{-1}d_{3/2}^{-2})$ contributing with probabilities of 31.4% and 34.3% in ¹³¹Te, 13.7% and 24.8% in ¹³³Xe, as well as 4.9% and 20.3% in ¹³⁵Ba. The $v(h_{11/2}^{-2}d_{3/2}^{-1})$ configuration nearly vanishes in the decomposition of the $J^{\pi} = 19/2^{-}$ states. The dominant components of the $J^{\pi} = 19/2^{-}$ and 23/2⁺ states can be connected by a *M*2 transition operator, however, the hindrance of the *M*2 transition can be traced back mainly due to the change of the neutron content of the states.

Finally, reduced transition probabilities for the $23/2^+ \rightarrow 19/2^-$ transitions in ¹³¹Te, ¹³³Xe and ¹³⁵Ba are calculated with the realistic SM, SN100PN, GCN50:82, and SN100-KTH interactions. Modified g factors of $g_l = g_{l_{free}}$ and $g_s = 0.68g_{s_{free}}$ for protons and neutrons are used for the SN100PN, GCN50:82, and SN100-KTH interactions. The obtained quenching factor of 0.68 is tuned to reproduce the magnetic moments of the $J^{\pi} = 11/2^-_1$ states in ¹²⁹Sn ($\mu = -1.297(5)\mu_n$ [66]) and ¹³¹Te ($\mu = -1.123(7)\mu_n$ [67]). In the realistic SM calculation nuclear g factors of $g_l = 1.2$, $g_s = 3.91$ for protons and $g_l = 0.2$, $g_s = -2.678$ for neutrons are employed.

The effective charges for protons and neutrons are selected to reproduce the *E*2 transition strengths of the first excited $J^{\pi} = 2^+$ state in the Z = 50 isotope ¹²⁸Sn (*B*(*E*2; 2⁺ \rightarrow 0⁺) = 4.2(3) W.u. [68]) and of the 19/2⁻ \rightarrow 15/2⁻ decay (*B*(*E*2; 19/2⁻ \rightarrow 15/2⁻) = 2.56(14) W.u. [69]) in ¹³³Te using the SN100PN, GCN50:82, and SN100-KTH interactions.

Isotope	$J^{\pi}_i ightarrow J^{\pi}_f$	E_i (keV)	$T_{1/2}$ (ms)	σλ	$B(\sigma\lambda)\downarrow$ (W.u.)				
					Experiment	nent Theory			
						Realistic SM	SN100PN	GCN50:82	SN100-KTH
	$27/2_1^- \rightarrow 23/2_1^-$	2552	$0.27(7) \times 10^{-3}$	<i>E</i> 2	0.79(36)	_	0.72	0.72	0.72
¹²⁹ Sn	$23/2^+_1 \rightarrow 19/2^+_1$	1802	$2.4(2) \times 10^{-3}$	E2	1.24(10)	_	1.45	0.71	1.44
	$19/2^+_1 \rightarrow 15/2^+_1$	1761	$3.6(2) \times 10^{-3}$	E2	1.37(8)	_	2.11	1.78	2.14
¹³¹ Te	$19/2^1 \to 15/2^1$	1581	$71(20) \times 10^{-9}$	E2	3.5(10)	_	4.9	2.9	3.5
le	$23/2^+_1 \rightarrow 19/2^1$	1941	93(12)	M2	$2.0(3) \times 10^{-6}$	_	404×10^{-6}	197×10^{-6}	305×10^{-6}
¹³³ Xe	$23/2^+_1 \rightarrow 19/2^1$	2107	8.64(13)	М2	$0.209(3) \times 10^{-3}$	1.163×10^{-3}	1.613×10^{-3}	0.668×10^{-3}	1.691×10^{-3}
				E3	0.0017(16)	0.476	0.124	0.021	0.221
¹³⁵ Ba	$23/2^+_1 \rightarrow 19/2^2$	2388	1.06(4)	M2 E3	$1.053(40) \times 10^{-3}$ 0.0012(11)	4.12×10^{-3} 1.161	2.440×10^{-3} 0.144	3.878×10^{-3} 0.119	2.283×10^{-3} 0.164

TABLE II. Summary of experimental and theoretical results for *E*2, *M*2, and *E*3 reduced transition strengths of the N = 79 isotones ¹²⁹Sn, ¹³¹Te, ¹³³Xe, and ¹³⁵Ba. Transition strengths are given in Weisskopf units. Experimental values of ¹²⁹Sn and ¹³¹Te are taken from Refs. [1,4,6].

The adopted effective charges are $e_{\nu} = 0.81e$ and $e_{\pi} = 1.52e$. Selected values are in excellent agreement with the effective charges used in a recent study of the N = 81 isotonic chain [70] and the previous study of ¹³⁶Ba [71]. In the realistic SM calculation effective charges of $e_{\nu} = 0.7e$ and $e_{\pi} = 1.7e$ are used.

The newly established half-lives are converted into M2 and E3 reduced transition probabilities using the equations [72,73]:

$$B(M2) = \frac{5.12 \times 10^{-8}}{T_{1/2} E_{\gamma}^5} \frac{1}{1 + \delta_{\frac{E3}{M2}}^2} \mu_N^2 \text{fm}^2$$
(3)

and

$$B(E3) = \frac{1.21 \times 10^{-3}}{T_{1/2} E_{\gamma}^7} \frac{\delta_{E3}^2}{1 + \delta_{E3}^2} e^2 \text{fm}^6, \qquad (4)$$

where $T_{1/2}$, E_{γ} and $\delta_{\frac{E_3}{M_2}}$ correspond to the measured half-life of the initial state in seconds, the γ -ray energy in MeV and the multipole-mixing ratio of the γ ray. The experimentally deduced $B(\sigma\lambda)$ values and the results of the shell-model calculations are summarized in Table II.

To benchmark shell-model calculations, several previously known B(E2) values of ¹²⁹Sn and ¹³¹Te are added. The experimental E2 reduced transition strengths of the decay of the seniority v = 3 multiplet states $J^{\pi} = 19/2^+$, $23/2^+$, and $27/2^-$ [1,4] in ¹²⁹Sn are well described within the three shell-model calculations. The discrepancy between the three calculations stays below 50% for the $B(E2; 23/2^+ \rightarrow 19/2^+)$ value in ¹²⁹Sn. Moreover, the calculated B(E2) transition probability of the $19/2^- \rightarrow 15/2^-$ decay in ¹³¹Te agrees well with the experiment.

Assuming a pure M2 transition, the experimental $B(M2; 23/2^+ \rightarrow 19/2^-)$ value of the $E_{\gamma} = 360$ -keV transition in ¹³¹Te is $2.0(3) \times 10^{-6}$ W.u. [2]. This value is overpredicted by at least two orders of magnitudes by the shell-model calculations. The single-particle Weisskopf estimate for the half-life of the $E_{\gamma} = 231$ keV transition in ¹³³Xe is 1.8 μ s for an M2 and 32 ms for an E3 transition. In ¹³⁵Ba the half-life

corresponding to one Weisskopf unit is 1.1 μ s for an *M*2 and 16 ms for an *E*3 transition. Assuming a pure *M*2 transition, the Weisskopf hindrance factors of the $J^{\pi} = 23/2^+$ isomers are $F_W = T_{1/2}^{\text{exp}}/T_{1/2}^{\text{W}} = 4800$ in ¹³³Xe and $F_W = 964$ in ¹³⁵Ba, compared to values of $F_W = 0.27$ and $F_W = 0.066$ for pure *E*3 transitions, respectively.

The experimental B(M2) and B(E3) values of the $23/2^+_1 \rightarrow 19/2^-_1$ decay in ¹³³Xe are $209(3) \times 10^{-6}$ and $1.7(16) \times 10^{-3}$ W.u., respectively. Calculations with the four interactions yield B(M2) values, which overpredict the experimental result by factors of 3.2–8.1. The measured *E3* admixture of the 231-keV transition is predicted at least one to two orders of magnitude too high. Only the B(E3) value computed by the GCN50:82 interaction is in reasonable agreement with the measured one.

The calculations for ¹³⁵Ba yield 2.2–3.9 times larger M2 transition strengths compared to the experimental M2 transition strength $B(M2; 23/2^+ \rightarrow 19/2^-) = 1.053(40) \times 10^{-3}$ W.u. Moreover, the transition strength to the first excited $J^{\pi} = 19/2^-$ state is computed to be 2.277 × 10⁻³, 1.607 × 10⁻³, and 2.627 × 10⁻³ W.u. by the GCN50:82, SN100-KTH, and SN100PN interactions, respectively. The B(E3) value of the 254-keV transition is overestimated by two orders of magnitude.

The calculated B(M2) values depend on the choice of proton and neutron *g* factors. Calculations employing $g_l(\pi) = 1.13$, $g_s(\pi) = 4.04$, $g_l(\nu) = 0.02$, and $g_s(\nu) = -2.65$, taking into account core polarization and meson-exchange currents [74,75], change the $B(M2; 23/2^+ \rightarrow 19/2^-)$ values slightly to 1.679×10^{-3} W.u (SN100PN), 0.693×10^{-3} W.u (GCN50:82), and 1.771×10^{-3} W.u (SN100-KTH) in ¹³³Xe and similar values of 2.559×10^{-3} W.u (SN100PN), 4.029×10^{-3} W.u (GCN50:82), and 2.406×10^{-3} W.u (SN100-KTH) in ¹³⁵Ba.

The fact that the M2 transition operator is mainly assigned to a change in neutron configuration (cf. Fig 10) is also reflected in the proton A_p and neutron A_n amplitudes which serve as weighting factors for the proton and neutron contribution to the M2 matrix elements. For the GCN50:82 interaction, the A_p and A_n amplitudes are 0.032 and 0.251 in ¹³³Xe and 0.057, 0.463 in ¹³⁵Ba, respectively.

The shell-model calculations support a dominating M2 character for the $23/2^+ \rightarrow 19/2^-$ transitions. Calculating the ratio B(M2)/B(E3) by using Eqs. (3) and (4) and solving for $|\delta|$ yields multipole-mixing ratios of 0.230, 0.068 (realistic SM), 0.098, 0.055 (SN100PN), 0.032, 0.013 (GCN50:82), and 0.158, 0.003 (SN100-KTH) for ¹³³Xe and ¹³⁵Ba, respectively. The values derived from the shell-model results are very similar to the experimentally determined $|\delta|$ values of 0.021(10) and 0.009(4). Moreover, the results support the smaller E3 admixture in ¹³⁵Ba compared to ¹³³Xe.

V. CONCLUSIONS

In summary, a detailed study of isomeric $J = 23/2^+$ states was performed in ¹³³Xe and in ¹³⁵Ba. Their half-lives of $T_{1/2} = 8.64(13)$ ms in ¹³³Xe and $T_{1/2} = 1.06(4)$ ms in ¹³⁵Ba close a gap along the N = 79 isotones. Measurements of the multipole-mixing ratio and internal-conversion coefficient of the 231-keV transition in 133 Xe and the 254-keV transition in 135 Ba yield a dominant M2 character. The experimentally determined B(M2) and B(E3) transition strengths are compared to the results of large-scale shell-model calculations employing the realistic SM, GCN50:82, SN100PN, and SN100-KTH interactions. In particular, interactions with improved and corrected monopole parts, i.e., GCN50:82, show a good agreement with the experimental findings. A detailed inspection of the evolution of proton and neutron decompositions along the N = 79 chain provide insight into the changing nuclear structure. The neutron configuration $v(h_{11/2}^{-2}d_{3/2}^{-1})$ is responsible for the isomeric character of the $23/2^+$ states. The different shell-model calculations follow the measured B(M2) systematics as function of proton filling in the gdsh orbitals along the N = 79 isotones. In particular, the agreement between calculated and experimental B(M2)values improves with increasing proton number.

However, the systematics of the N = 79 isotonic chain still lacks some information. In 2013 a recoil-decay tagging

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experiment reported on three feeding transitions decaying into the isomeric $J^{\pi} = (23/2^+)$ state at $E_x = 2616$ keV in ¹³⁹Nd [3]. So far, there are no states observed that populate the $J^{\pi} = 23/2^+$ isomers in ¹³¹Te and ¹³⁵Ba. In future, a similar measurement in both nuclei is of high interest to resolve those feeding patterns. There is a large disagreement between shell-model theory and experiment for the transition strength of the $23/2_1^+ \rightarrow 19/2_1^-$ decay in ¹³¹Te, motivating new refined experiments.

Furthermore, despite a detailed knowledge of the high-spin regime in ¹³⁷Ce, no $J^{\pi} = 23/2_1^+$ isomer was reported to date. The hitherto known $23/2^+$ state disrupts the isotonic systematics and is unlikely an isomer. However, the 2490-keV state, decaying into the $19/2_2^-$ state, is a possible candidate for the expected isomer [14]. Further experiments should be performed to elucidate a possible onset of $J^{\pi} = 23/2_1^+$ isomerism in ¹³⁷Ce.

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