

# Improving *Bowen-ratio* estimates of evaporation using a rejection criterion and multiple-point statistics

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## Abstract

The application of the Bowen ratio method to estimate evaporation is heavily affected by uncertainties on the measured quantities. Time series collected with a hydro-meteorological monitoring station often contain measurements for which a reliable estimate of evaporation cannot be computed. Such measurements can be identified with standard error propagation methods. However, simply discarding some values might introduce a bias in the cumulative evaporation for long time intervals, also depending on the threshold of acceptance. In this paper, we propose the use of multiple-point statistics simulation to integrate the time series of reliable evaporation estimates. A test conducted on a two-year-long time series of data collected with a hydro-meteorological station in the Po plain (Italy) shows that the usage of a rejection criteria in conjunction with multiple-point statistics simulation is a promising and useful tool for the reconstruction of reliable evaporation time series. In particular, it is shown that if the rejected values are not replaced by simulation, then the cumulative evaporation curves are estimated with a

bias comparable with estimates of cumulative annual evaporation. Moreover, the test gives some insights for the selection of the best rejection threshold.

*Keywords:* evaporation, Bowen ratio, multiple-point statistics, time series reconstruction, direct sampling

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## 1 Introduction

Evaporation and transpiration are key factors in the water balance at any temporal and spatial scale and their estimate is of paramount importance in several disciplines, from hydrology to soil science, climatology, etc. (Allen et al., 1998; Eagleson, 2003). Unfortunately, means of direct measurement of evaporation are not available; therefore, the estimate of such a quantity always relies on models of variable complexity or on parameterization.

Among physically-based methods, i.e., those which derive from basic physical principles, the *Bowen ratio* method (BRM, Bowen, 1926) uses quantities which can be measured with an hydro-meteorological monitoring station. However, the uncertainties on the measured quantities can affect the Bowen ratio ( $B$ ), namely the ratio between sensible and latent heat fluxes, in such a way as to yield an unrealistic value of real evaporation ( $E$ ).

Very often, sensible and latent heat fluxes are computed from quantities measured at two heights only. Therefore, some authors proposed to improve the estimation of  $B$  by increasing the spatial resolution of the measurements required to compute the aforementioned fluxes (Euser et al., 2014).

Another solution to cope with unrealistic  $E$  values is data rejection, and the literature contains a number of approaches to handle it. Some authors (Tanner et al., 1987; Ortega-Farias et al., 1996; Cellier and Olioso, 1993)

21 proposed to reject data on the basis of the value of  $B$ . Other authors, like  
22 for example Ohmura (1982) and Perez et al. (1999), proposed criteria for  
23 data rejection based on the analysis of the limits related to the instrument  
24 resolution and physical considerations. Many of the aforementioned works  
25 were summarized and integrated by Payero et al. (2003). A different approach  
26 was proposed by Romano and Giudici (2009), by taking into account the  
27 measurement errors and their propagation through the formula to estimate  
28 the evaporation with the BRM.

29 No matter which method is used to select the unreliable samples from  
30 a data set, the simplest approach of excluding the physically inconsistent  
31 data from the time series of evaporation introduces a bias in the estimate  
32 of cumulative evaporation. In fact, this can alter the results for long time  
33 periods, e.g., if the BRM is used to perform climatological analyses. It is  
34 therefore important to develop an approach to integrate the rejected data  
35 samples.

36 Some authors proposed to integrate the missing or rejected values of  $B$   
37 using estimates based on an exchange coefficient, computed from quantities  
38 like wind speed or temperature-variance (Savage et al., 2009). Here an alter-  
39 native approach is proposed, where the rejected values of  $E$  are replaced by  
40 a stochastic simulation method.

41 In this paper, the use of multiple-point statistic simulation (MPS) for the  
42 replacement of the rejected values of  $E$  is proposed and tested. Among the  
43 multiple-point simulation paradigms, the Direct Sampling (DS, Mariethoz  
44 et al., 2010) method is considered for its flexibility in handling the simu-  
45 lation of continuous variables and the possibility to incorporate secondary

46 information. Moreover, the DS was already tested with success for the re-  
47 construction of incomplete flow rate time-series in a karstic network by Oriani  
48 et al. (2016). In the present work, the methodology is tested on a real case  
49 study with a two-year-long time series of hydro-meteorological data, whose  
50 length can help to evidence particular features, strengths and weaknesses of  
51 the method. To our knowledge, this is the first time that this algorithm  
52 is tested on the reconstruction of evaporation, and in conjunction with a  
53 rejection criteria.

54 In particular, the following questions are addressed. As the method of  
55 Romano and Giudici (2009) requires to define a rejection threshold  $\varepsilon$ , what is  
56 the impact of the selection of  $\varepsilon$  on the cumulative evaporation? How much the  
57 estimates of cumulative evaporation are improved when the rejected values  
58 of  $E$  are replaced by the simulated ones? Is it possible to improve the DS  
59 simulation of the rejected values of  $E$  by including one or more measured  
60 quantities as covariates?

61 The field data used to demonstrate the proposed approach, the method  
62 used to compute the evaporation  $E$ , and the two main steps of the approach  
63 (rejection and simulation) are described in Section 2. Section 3 briefly reports  
64 the results, which are then discussed in detail in Section 4. The conclusion  
65 are reported in Section 5.

## 66 **2. Materials and Methods**

67 This section illustrates first the field data used to demonstrate the pro-  
68 posed approach. Then, the Bowen ratio method used to compute the evap-  
69 oration  $E$  is briefly recalled. Finally, the two main steps of the proposed

70 approach are described: (1) the criterion used to reject the estimates of  $E$   
71 that are not reliable, and (2) the direct sampling method, used to replace  
72 the rejected values of  $E$ .

73 [Table 1 about here.]

#### 74 *2.1. Field data*

75 The data set used to test the procedure proposed in this paper were  
76 acquired at an hydro-meteorological monitoring station installed in 2006 at  
77 Roncopascolo, in the valley of the Taro river, within the Po plain, at about  
78 6 km NW from the city of Parma (Italy).

79 The position of the station was chosen on the basis of some constraints:  
80 the ground has not being subject to human activities for a long time, the area  
81 is far from buildings or other obstructing bodies, the installed instruments  
82 are protected against thieve or damages.

83 The meteorological sensors of the monitoring station are installed on a  
84 five-meter-tall pole. Two couples of humidity and temperature sensors are  
85 installed at 2 m ( $h_1$ ) and 4 m ( $h_2$ ) from the ground surface, a pressure sensor  
86 is installed in the box containing the data logger, an anemometer is installed  
87 at the top of the pole, i.e. 5 m above the ground, and a sensor of net radiation  
88 is installed at an height of about 2 m. Moreover, a rain gauge is installed  
89 at a distance of 2 m from the principal pole at an height of 1.5 m from the  
90 ground and a sensor to measure the heat flux is immersed in the soil, at a  
91 depth of few centimeters, a couple of meters far from the pole. All the data  
92 have been collected with a sampling interval of 20 minutes.

93 The data used in this work correspond to the period from June 2009 to  
94 July 2011, for which a rather complete series of data is available. Later, it

95 was not possible to perform a regular maintenance of the monitoring station,  
96 which has newly been working since spring 2016.

97 A preliminary accurate analysis of the recorded data already shows some  
98 anomalous measurements. In winter, negative values of net radiation, with  
99 high absolute values, have been measured and interpreted as an effect of  
100 intense snow, as supported from meteorological bulletins of the surrounding  
101 area. In those cases snow could cover the upper part of the net radiation  
102 sensor and filter out the direct solar radiation, whereas the high albedo of  
103 snow on the ground could enhance the reflected radiation, thus producing  
104 values as low as  $-150 \text{ W/m}^2$ . In summer and spring, some spikes appear in  
105 the time series of different quantities, but they seem to be due to interference  
106 of lighting with the instrumentation, again as confirmed by the inspection of  
107 meteorological bulletins of the surrounding area. These evident anomalous  
108 measurements were removed from the time series prior to the application of  
109 the proposed work-flow.

## 110 2.2. Bowen ratio method

111 Using the data collected at the hydro-meteorological station, evaporation  
112  $E$  can be computed using the BRM. The latter is based on the computation  
113 of the Bowen ratio, i.e., the ratio between sensible and latent heat flux, which  
114 is estimated from measurements of temperature and vapor partial pressure  
115 at two different heights as

$$B = \frac{C_a P_a}{0.622 \lambda_v} \frac{T_2 - T_1}{e_2 - e_1} \quad (1)$$

116 where  $C_a$  is the specific heat of air at constant pressure per unit mass,  $P_a$  is  
117 the atmospheric pressure,  $\lambda_v$  is the latent heat of evaporation per unit mass,

118  $T_i$  and  $e_i$ , with  $i = 1, 2$ , are, respectively, air temperature and vapor partial  
 119 pressure at two different heights  $h_i$  above the ground surface. Given the  
 120 air temperatures, the vapor partial pressures can be converted, using some  
 121 empirical relation (Dingman, 2015), into the corresponding relative humidity  
 122  $RH_1$  and  $RH_2$ .

123 The energy balance at the soil, by neglecting the advective contribution  
 124 and energy storage, yields the following expression for the evaporation  $E$ ,  
 125 i.e., the volume of liquid water evaporating from the surface per unit time  
 126 and unit surface:

$$E = \frac{R_n - G}{\rho_w \lambda_v (1 + B)} \quad (2)$$

127 where  $R_n$  is the net radiation,  $G$  is the geothermal heat flow and  $\rho_w$  is the  
 128 water density.

### 129 *2.3. Rejection of unreliable estimates of evaporation*

130 Equations (1) and (2) show that (i)  $B$  can be computed only if  $e_1 \neq e_2$  and  
 131 (ii)  $E$  can be computed with (2) only if  $B \neq -1$ . These conditions are not  
 132 always met when dealing with field monitoring data. Moreover, even if they  
 133 are satisfied, the propagation of measurement errors could yield unrealistic  
 134 values of  $E$ . For example, if  $e_2 - e_1 \rightarrow 0$ , i.e. the vapor partial pressure is  
 135 constant along the vertical, and  $B \neq 1$ , then  $E \rightarrow 0$ , namely the evaporation  
 136 is negligible. Instead, if  $e_2 \neq e_1$ , then  $B \rightarrow -1$  implies  $E \rightarrow \pm\infty$ . In other  
 137 words, when  $B$  is close to  $-1$ , the estimated evaporation rate would achieve  
 138 unrealistic values.

139 The criterion used to reject data is taken from Romano and Giudici (2009)  
 140 and operates according to the following procedure. For every physical quan-  
 141 tity appearing in equations (1) and (2) an estimate of its uncertainty is given,

142 based on the accuracy of the measurement instrument. From these estimates  
143 and the law of error propagation (Bevington and Robinson, 2003), the uncer-  
144 tainty on the estimate of the evaporation rate,  $\delta_E$ , is computed. If  $\delta_E/E > \varepsilon$ ,  
145 where  $\varepsilon$  is a prescribed threshold, then the value of  $E$  is considered to be  
146 unreliable and it is discarded. Romano and Giudici (2009) tested values of  
147  $\varepsilon \in [0.1, 50]$  for a data set collected in the suburbs of the city of Milan and  
148 suggest the value of 5 acceptable for relative errors of the cumulative evap-  
149 oration lower than 20%. In the following sections we report and discuss the  
150 results obtained with  $\varepsilon \in \{0.5, 1, 5, 10\}$ .

#### 151 *2.4. Reconstruction of rejected estimates of evaporation with MPS*

152 Starting from a time series of meteorological data, the procedure de-  
153 scribed in Section 2.2 and Section 2.3 can be applied. The values of evap-  
154 oration that were rejected because considered not reliable according to the  
155 criterion described in Section 2.3 should be replaced by reliable estimates. If  
156 these values are not replaced, then the cumulative evaporation assessed for  
157 a long time period could be strongly underestimated.

158 This problem can be limited with a proper simulation of the missing val-  
159 ues in the series of evaporation. In this paper, this is obtained with the  
160 application of MPS. In particular, a direct sampling (DS) algorithm (Mari-  
161 ethoz et al., 2010) is used. Our approach is similar to that applied by Oriani  
162 et al. (2014) to model rainfall time series and the flow rate of two karstic  
163 springs in the Jura Mountains, Swiss Alps (Oriani et al., 2016).

164 For our application, a training image (TI) is given by the time series of  
165 the acceptable values of  $E$  ( $E_{\text{TI}}$ ). The simulation grid (SG) is the array  
166 which contains the whole time series of  $E$ , including both the acceptable



167 values estimated from (2) and the values simulated with the DS algorithm to  
 168 replace the rejected ones. Hereinafter we briefly outline the working principle  
 169 of the DS, as applied to our case study.

- 170 1. Let  $\mathbf{t} = \{t_1, t_2, \dots, t_n\}$  be the array of the times for which the SG has  
 171 to be built, let  $\boldsymbol{\tau} = \{\tau_1, \tau_2, \dots, \tau_m\}$  be the array of the times for which  
 172 acceptable values of  $E$  were found and let  $\tilde{E}$  be the evaporation rate,  
 173 normalized with a linear scaling in such a way that it is comprised  
 174 between  $-1$  and  $1$ . This step is required to homogenize the distance  
 175 computations and the comparisons between variables and covariates.
- 176 2. Randomly select an empty cell of the SG, i.e. a time  $t_i$ . The set  $\boldsymbol{\tau}_i$  of  
 177 times  $\tau_j \in \boldsymbol{\tau}$ , such that  $|t_i - \tau_j| < R$ , where  $R$  is a prescribed search  
 178 radius, and such that the cardinality of  $\boldsymbol{\tau}_i$  is smaller than a prescribed  
 179 maximum number  $N$ , is used to define a data event, i.e., a set of couples  
 180 of time lags and corresponding values of  $\tilde{E}$  such that

$$\mathbf{d}_i = \{(t_i, \tilde{E}(\tau_j)) \text{ with } |\tau_j - t_i| < R, \tau_j \neq t_i, \text{card}(\boldsymbol{\tau}_j) \leq N\}. \quad (3)$$

181 The number of values  $\tau_j$  is limited by the user provided parameter  $N$ ,  
 182 that is the maximum number of nodes in the search neighborhood. This  
 183 parameter allows to dynamically define the radius  $R$  by considering only  
 184 the  $N$  values of  $\tau_j$  closest to  $t_i$ .

- 185 3. The TI is scanned until a data event, for time  $t_k \in \boldsymbol{\tau}$ , similar to  $\mathbf{d}_i$  is  
 186 found, i.e., when  $|\mathbf{d}_i - \mathbf{d}_k| < \sigma$ , where  $\sigma$  is a prescribed threshold of  
 187 acceptance.
- 188 4. The time  $t_i$  is added to  $\boldsymbol{\tau}$  and  $\tilde{E}(t_i) = \tilde{E}(t_k)$ . The procedure continues  
 189 from point 2 above, until the whole SG is filled with simulated values  
 190  $(E_{\text{sim}})$ .

191 If, for the time series, measurements of other variables supposedly cor-  
192 related with the simulated variable are available, then the approach can be  
193 extended in a straightforward manner to include them in a co-simulation  
194 framework, where the training image becomes a multi-variate training image  
195 and different thresholds and search radius can be defined, one for each vari-  
196 able. For more details refer to Mariethoz et al. (2010) and to Oriani et al.  
197 (2014, 2016).

198 When using the DS simulation technique, the choice of several simulation  
199 parameters can have an important impact on the final results. In this work,  
200 a number of preliminary tests were performed to select the suitable simula-  
201 tion parameters, also following the guidelines presented by Meerschman et al.  
202 (2013) and the parameterization adopted by Oriani et al. (2014, 2016). A  
203 good balance between CPU requirements (that anyhow remained below the  
204 order of few seconds per realization) and quality of the simulation were ob-  
205 tained with a search radius  $R$  of 28 days, a threshold  $\sigma = 0.001$ , and  $N = 20$ .  
206 To smooth the simulated values of  $E$ , the average over 10 equiprobable re-  
207 alization is considered. All the direct sampling simulations were performed  
208 with the `deesse` simulation code (Mariethoz et al., 2010; Straubhaar, 2017).

209 An important remark has to be made here: in a standard MPS simula-  
210 tion setting, TI and SG are separated entities which can have, in general, a  
211 different size and represent different time (or space) windows. In the simu-  
212 lation setting presented here, TI and SG share the same grid and the same  
213 time window. In fact, the TI is incomplete (rejected values of  $E$ ) and the  
214 simulation procedure aims at inserting the missing  $E$  values.

215 *2.5. Validation*

216 A validation step was performed to support the results obtained by the  
 217 reconstruction. In practice, a given percentage of the  $E$  values considered  
 218 reliable according to the adopted rejection criterion is randomly selected and  
 219 excluded both from the training and the conditioning data set, but is used for  
 220 cross-validation ( $E_{\text{val}}$ ). The validation is performed for different values of the  
 221 rejection threshold  $\varepsilon$  in terms of Q-Q plots, and also in terms of a coefficient  
 222 inspired by the Nash-Sutcliffe efficiency ( $NSE$ , Nash and Sutcliffe, 1970)

$$NSE = 1 - \frac{\sum_{t_i \in \tau_{\text{val}}} (E_{\text{val}}(t_i) - E_{\text{sim}}(t_i))^2}{\sum_{t_i \in \tau_{\text{val}}} (E_{\text{val}}(t_i) - \bar{E}_{\text{val}}(t_i))^2} \quad (4)$$

223 Here  $\tau_{\text{val}}$  contains the time steps  $t_i$  for which a validation value of  $E$  is se-  
 224 lected, and  $\bar{E}_{\text{val}}$  represents the average of these values over a given time win-  
 225 dow. In brief,  $NSE \simeq 1$  indicates that simulation has better performances if  
 226 compared to simple approaches where the average value of  $E$  is considered;  
 227  $NSE \simeq 0$  indicates that simulation and simple approaches are equivalent;  
 228  $NSE < 0$  indicates that simple approaches outperform simulation.

229 **3. Results**

230 First of all the deleterious effect of  $B$  is analyzed. By looking at Figure 1  
 231 it is clear that for values of  $B \simeq -1$   $|E|$  reaches completely unreliable values.

232 [Figure 1 about here.]

233 Then, in the two following section, the results obtained by investigating the  
 234 impact of a different rejection threshold  $\varepsilon$  and the usage of one or more  
 235 covariates in the DS simulation are briefly illustrated.

236 To illustrate the impact of the rejection threshold, the criterion proposed  
237 by Romano and Giudici (2009) was applied using four different thresholds to  
238 the evaporation computed with the Bowen-ratio method. The values of  $E$   
239 that were not rejected are used both as training image and as conditioning  
240 data in the DS simulation. For each value of  $\varepsilon$ , 10 DS realizations are per-  
241 formed and the rejected values of  $E$  are replaced by the arithmetic average  
242 of the 10 realizations. The results are compared in terms of Q-Q plots, visual  
243 inspection of time series, cumulative  $E$  curves, and also using diverse statis-  
244 tical indicators to average the realizations obtained for each  $\varepsilon$ . To further  
245 support the results, a validation test is performed by randomly selecting the  
246 25% of the non-rejected  $E$ . The validation values are then compared with  
247 values simulated for the same time steps using the 75% of the non-rejected  
248 data as training and conditioning data.

249 Then, an intermediate value of  $\varepsilon = 5$  was selected to illustrate the effect  
250 of adding a covariate in the simulation process. Seven different covariates  
251 were selected and used in the DS to simulate the rejected  $E$  values, including  
252  $T_1$ ,  $RH_1$ ,  $P_a$ , precipitation,  $G$ ,  $R_n$ , and  $v$ .

### 253 *3.1. The impact of the rejection threshold $\varepsilon$*

254 The basic problem to be solved when applying the method by Romano  
255 and Giudici (2009) is the choice of the threshold  $\varepsilon$  for the rejection criterion.  
256 Here we investigate the effects that four different thresholds have on the  
257 reconstructed time series of  $E$  and the corresponding cumulative time series.  
258 The main impact is evident on the number of rejected values of  $E$ , which  
259 are reported in Table 2. The percentage of rejected values is also listed on  
260 a seasonal basis to illustrate its variability, for each of the investigated years

261 and for the complete time series.

262 [Table 2 about here.]

263 Another tool useful to compare the results obtained by changing the re-  
264 jection threshold  $\varepsilon$  is the Q-Q plot. In Figure 2 are reported, for different  
265 values of  $\varepsilon$ , the quantiles of the time series completed with the simulated data  
266 on abscissa, and the quantiles of the time series containing only the reliable  
267 (non-rejected) values of  $E$  on ordinate. The orange line represents the case  
268 when the quantiles computed for the simulation coincide with the training  
269 data.

270 [Figure 2 about here.]

271 Q-Q are not sufficient to discern if the missing values were correctly re-  
272 placed by the simulated ones. A visual inspection of the time series can reveal  
273 some details which are not put in evidence by the Q-Q plot. In Figure 3, for  
274 example, we compare the  $E$  time series obtained with  $\varepsilon = 1$  and  $\varepsilon = 10$  for a  
275 time window with a high density of simulated data (second half of January  
276 2011)

277 [Figure 3 about here.]

278 It is also important to check the impact of applying different rejection thresh-  
279 olds  $\varepsilon$  on the cumulative  $E$  curves (Figure 4).

280 [Figure 4 about here.]

281 One of the main goals of this research was to estimate the impact of  
282 neglecting the contribution of the rejected values of  $E$  on the cumulative

283 curves. This aspect is illustrated in Figure 5 for  $\varepsilon = 1$ , a parameter that  
284 provides a good balance between the number of rejected values of  $E$  and the  
285 reliability of the time series. In Figure 5 the cumulative  $E$  curves obtained by  
286 replacing the rejected data with simulated values of  $E$  (continuous line) are  
287 compared against the curves obtained without replacing the rejected values  
288 of  $E$  (dashed lines). Comparable results were obtained with the other values  
289 of  $\varepsilon$ , which are not shown here for the sake of brevity. Nevertheless, the  
290 differences between the cumulated  $E$  are reported for each year and for each  
291 value of  $\varepsilon$  in Table 3.

292 [Figure 5 about here.]

293 [Table 3 about here.]

294 As mentioned in Sect. 2.4, the simulated values of  $E$  are presented as  
295 the arithmetic mean over 10 DS realizations. Fig. 6 illustrates how the cu-  
296 mulative  $E$  curves behave when different statistical indicators are used to  
297 aggregate the 10 realizations. In particular, Fig. 6 reports, for year 2010  
298 and for the different values of the threshold  $\varepsilon$ , the cumulative  $E$  curves com-  
299 puted using the arithmetic mean (continuous blue line), the 1-st quartile ( $Q_1$ ,  
300 dashed orange line), the median ( $Q_2$ , dash-dotted green line), and the 3-rd  
301 quartile ( $Q_3$ , dashed red line).

302 [Figure 6 about here.]

303 Figure 7 illustrates the results of the validation step, where for the differ-  
304 ent values of  $\varepsilon$  considered in this work the 25% of the reliable  $E$  is randomly

305 selected and kept for validation purposes, and compared with the values sim-  
306 ulated for the same time step. The *NSE* for the corresponding value of  $\varepsilon$  is  
307 reported in the lower right corner of each sub-plot.

308 [Figure 7 about here.]

### 309 3.2. Simulating the rejected values of $E$ using a covariate

310 Another aspect explored by this research is the influence of considering a  
311 covariate in the simulation of the rejected values of  $E$ . Here the considered  
312 covariates are a number of quantities measured at the hydro-meteorological  
313 station of Roncopascolo including  $T_1$ ,  $RH_1$ ,  $P_a$ , precipitation,  $G$ ,  $R_n$ , and  
314 the wind speed  $v$ . All the parameters already used in Equations (1) and (2)  
315 for the computation of  $E$  are correlated with  $E$  itself. Nevertheless, for the  
316 time step where  $E$  is rejected, the aforementioned parameters have reliable  
317 values and therefore they can potentially improve the simulation of  $E$ . Here  
318 the impact of considering one covariate in the DS simulations is illustrated  
319 via Q-Q plots in Figure 9. Figure 9a illustrates the reference case when no  
320 covariates are used, while the remainders sub-plots (Figure 9b-h) represent  
321 the results obtained considering one of the aforementioned covariates. Also,  
322 the same results are presented in terms of cumulative  $E$  (Figure 8).

323 Only the results for the rejection threshold  $\varepsilon = 5$  are shown here, because  
324 they provide a situation where many  $E$  values are rejected and there is room  
325 for improving the estimates of the missing  $E$  values obtained without the use  
326 of a covariate.

327 [Figure 8 about here.]

328 [Figure 9 about here.]

329 **4. Discussion**

330 As anticipated in Section 2.3 and as expected from Equation (2), the re-  
331 sults show that when  $B$  is close to -1 the computed values of  $|E|$  become more  
332 and more high and unreliable (Figure 1). From Figure 1 it is evident that  
333 those  $E$  values can have a deleterious effect when considered in cumulative  
334  $E$  curves. It becomes therefore crucial to reject unreliable values of  $E$ .

335 With the rejection thresholds  $\varepsilon$  tested in this work, for the same time  
336 series the percentage of rejected values varies from 6.1 % to 70.6 % (Table 2).  
337 The percentages of rejected data regrouped by season (Table 2) suggest that  
338 spring is the season where most data are incorrectly determined, and this  
339 is thought to be related to the fact that this is the season with the highest  
340 atmospheric instability.

341 Q-Q plots and visual inspection of the time series were used to evaluate  
342 the reconstructed time series (Figure 2). From the Q-Q plots,  $\varepsilon = 1$  appears  
343 to provide the best results. At the same time, a restrictive value of  $\varepsilon$  (i.e.  
344  $\varepsilon = 1$  or  $\varepsilon = 0.5$ ) reduces considerably the number of data and the number of  
345 extreme events in the incomplete data series that are used as training data in  
346 the DS. This has a clear impact on the reconstructed time series variability  
347 (Figure 2). A visual inspection of the time series integrates the results of  
348 the Q-Q plots, showing that a quite restrictive rejection threshold ( $\varepsilon = 1$ )  
349 provides a reliable temporal variability of  $E$  (Figure 3a) and filters out some  
350 spikes that instead appear for less restrictive  $\varepsilon$  ( $\varepsilon = 10$ , Figure 3b). Note  
351 that in Figure 3 we deliberately selected a time window where many values  
352 of  $E$  were rejected to illustrate the DS simulation capabilities.

353 Figure 4 illustrates the impact of different rejection thresholds  $\varepsilon$  on the



354 cumulated  $E$ , when the rejected values of  $E$  are replaced with simulated  
355 values, for years 2009, 2010 and 2011. The features of the cumulated  $E$   
356 curves are useful for the selection of the optimal  $\varepsilon$ . For example, for years  
357 2010 and 2011 (Figure 4b and Figure 4c), only with the values  $\varepsilon = 0.5$   
358 or  $\varepsilon = 1$  the anomalous features of the cumulative curves around March  
359 2010 and March-May 2011 are filtered out. Also, the difference between the  
360 growth rates of the curves for  $\varepsilon = 0.5$  and  $\varepsilon = 1$  show that the two rejection  
361 thresholds have a different impact depending on the sign of the rejected  $E$   
362 values. As a consequence, the rejection procedure has a different impact  
363 depending on the season and on the prevailing physical process. However,  
364 if we exclude year 2011, the final plateau reached by using diverse values  
365 of  $\varepsilon$  has an impact of few tenths of millimeters on the yearly cumulated  $E$ .  
366 The values of the cumulated precipitation reported on the top of each figure  
367 (Fig. 4) are also useful to check the reliability of the cumulative  $E$  curves  
368 computed with different  $\varepsilon$ . Note also that while for year 2010 a more complete  
369 data set is available, years 2009 and 2011 are incomplete for a rather different  
370 time period. This justified the noticeable differences between the cumulative  
371  $E$  curves (Fig. 4).

372 Probably, the most important result is illustrated in Figure 5. When  
373 the rejected values of  $E$  are not replaced by simulation, the cumulative  $E$   
374 obtained from instantaneous values which were not rejected is strongly un-  
375 derestimated (dashed lines, Figure 5). The cumulative  $E$  could be somehow  
376 corrected by considering the percentage of rejected values. However, here it  
377 is possible to provide a more precise estimate: the yearly cumulative  $E$  gen-  
378 erally is underestimated by an amount that has its same order of magnitude.

379 For example, in our case, for years 2009 and 2010 the yearly cumulative  $E$   
380 is underestimated by more than 100 mm (Figure 5a and Figure 5b), while  
381 (for the available period) of the 2011 by more than 300 mm (Figure 5c). The  
382 numerical values of the differences are reported in Table 3. Here it is impor-  
383 tant to remark that for years 2009 and 2010 the differences decrease with the  
384 increase of  $\varepsilon$ , whereas for year 2011 the trend is quite peculiar, with a peak  
385 of difference for the value of  $\varepsilon = 1$ .

386 Figure 6 illustrates the impact of the statistical indicator used to aggre-  
387 gate the results of the simulation over many realizations on the cumulative  
388  $E$ . With a relative low rejection threshold ( $\varepsilon = 0.5$ , Fig. 6a), many values are  
389 rejected, many are simulated and few conditioning data are kept; this has a  
390 clear effect on the spreading of the cumulated  $E$ , and implies that arithmetic  
391 mean and median ( $Q_2$ ) at the end of the year accumulate more than 50 mm  
392 of difference. Nevertheless, it is sufficient to rise the rejection threshold above  
393 1 to reduce the cumulated difference between mean and median to few mil-  
394 limeters per year (Fig. 6b, c, and d). In addition, the curves reported for  $Q_1$   
395 and  $Q_3$  show not only the uncertainty on the simulated cumulative  $E$ , but  
396 also the effectiveness of the arithmetic mean in smoothing extreme values for  
397 high values of  $\varepsilon$ , when the number of rejected and simulated values of  $E$  is  
398 small.

399 To further support the results, one depletion test for each rejection thresh-  
400 old was performed (Fig. 7). When many values of  $E$  are rejected, the statis-  
401 tics of the simulated values are coherent with those of the validation data  
402 (Fig. 7a and b). Nevertheless, the slight deterioration of the statistics when  
403 many data are rejected (Fig. 7a) suggests that a too high fraction of rejected

404 data entails a pauperization of the training data. Differently, and in par-  
405 ticular when many unreliable values are kept, the statistics of the simulated  
406 values (Fig. 7d) depart from the validation data, for example for  $E < 0$  mm/h  
407 and  $E > 0.6$  mm/h. The  $NSE$  indices reported in Fig. 7 illustrate the effi-  
408 ciency of the proposed work-flow against a naive approach where the missing  
409 values are reconstructed using the weekly averaged values of  $E$ . Also, its  
410 variability against  $\varepsilon$  provides a useful guide for the selection of this rejection  
411 threshold.

412 Another interesting aspect investigated here is the influence of a covariate  
413 in the simulation of the rejected  $E$  values. The Q-Q plots (Figure 9) already  
414 reveal that the impact is much less evident than changes in the value of  
415 the rejection threshold  $\varepsilon$  (Figure 2). Nevertheless, some variables provide a  
416 better representation of the quantiles. This is for example the case of relative  
417 humidity ( $RH_1$ , Figure 9c), atmospheric pressure ( $P_a$ , Figure 9d), and wind  
418 speed ( $v$ , Figure 9h), where the scattered quantiles (blue dots) are closer to  
419 the ideal case (orange line) than the results obtained without the use of any  
420 covariate in the DS simulation (Figure 9a). For the covariates that provide a  
421 better representation of the data in terms of Q-Q plots, the visual inspection  
422 of the  $E$  time series (not shown here) reveals a smoothed and spike-free trend  
423 if compared to the  $E$  time series simulated without a covariate. Clearly,  
424 taking into account a covariate in the simulation of the rejected  $E$  has an  
425 impact on the cumulative  $E$  curves (Figure 8). For the considered years,  
426 the difference between the reference black curve with markers (simulation  
427 without covariate) and the colored curves (simulation with one covariate),  
428 has a maximum of about 30 mm. One interesting aspect is that the sign

429 of this impact depends, for the time period investigated, not only on the  
430 considered covariate but also on the time window considered. For year 2009,  
431 for example, all the cumulative curves obtained using a covariate are above  
432 the one obtained with no covariate (Figure 8a), while for years 2010 and 2011  
433 diverse covariates have a diverse impact on the cumulative curves (Figure 8b  
434 and Figure 8c).

## 435 5. Conclusions

436 In this technical note, a straightforward work-flow to improve the relia-  
437 bility of cumulative time series of evaporation  $E$  is presented. The work-flow  
438 is made of two main steps: firstly, the values of  $E$  that are deemed unre-  
439 liable according to a threshold defined by error propagation techniques are  
440 rejected; then, the rejected values are replaced by multiple-point statistics  
441 simulation using a direct sampling algorithm. The applicability of the work-  
442 flow is demonstrated on a data-set collected by a hydro-meteorological station  
443 located in the Po plain (Italy), from May 2009 to July 2011. This data-set  
444 allows to test the work-flow on values of  $E$  estimated with the Bowen ratio  
445 method. However, the proposed work-flow has a general validity and can  
446 be applied in different contexts, like for example where  $E$  is estimated from  
447 eddy covariance measurements.

448 It is shown that the proposed work-flow can be used to integrate incom-  
449 plete time series in a straightforward way. In particular, when applied to  
450 the reconstruction of evaporation time series, the results demonstrate that  
451 if the rejected values of  $E$  are not replaced by simulated values, then the  
452 cumulative  $E$  can be underestimated by quantities comparable to its total

453 per annum. Focusing on the data set considered in this study, the annual  
454 underestimation of  $E$  can easily exceed 100 mm/year.

455 Unfortunately, direct measurements of  $E$  are not available for the same  
456 time period and region. However, although a direct comparison with ref-  
457 erence values cannot be performed, the cumulative  $E$  time series obtained  
458 integrating the rejected values with simulated values allows to quantify the  
459 approximation made when the missing values are not properly replaced.

460 In addition, this study provides useful insights for the selection of  $\varepsilon$ , the  
461 threshold used to reject unreliable values of  $E$  based on the error propagation  
462 theory. Here, simple tools like Q-Q plots and visual inspection of time series  
463 allowed to select the value of  $\varepsilon$  that provided a good compromise between  
464 number of rejected samples and a reliable reconstruction of the  $E$  time series.

465 Another aspect investigated in this research is the potential improvement  
466 of the simulation results provided by the usage of covariates. This study  
467 shows that including a covariate in the simulation process has an impact on  
468 the final results, which of course depends on the covariate considered, but  
469 also on the part of the considered year. Further research is required to in-  
470 vestigate the effects of taking into account, in the simulation process, of the  
471 combination of two or more covariates. Besides different parameterizations  
472 of the direct sampling algorithm, other covariates derived from the variables  
473 measured at the hydro-meteorological station can be considered, like for ex-  
474 ample a moving average of the temperature, that could provide a seasonal  
475 trend useful to improve the simulation.

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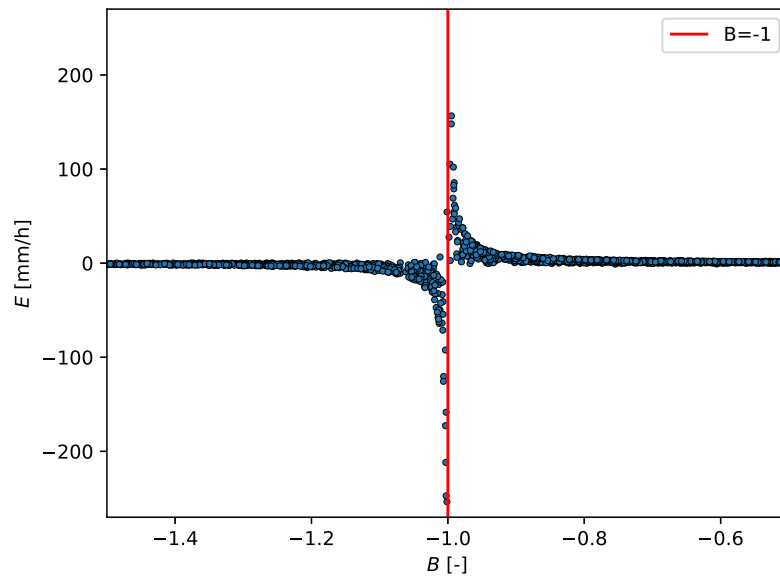


Figure 1: Scatter plot of evaporation  $E$  vs Bowen ratio  $B$

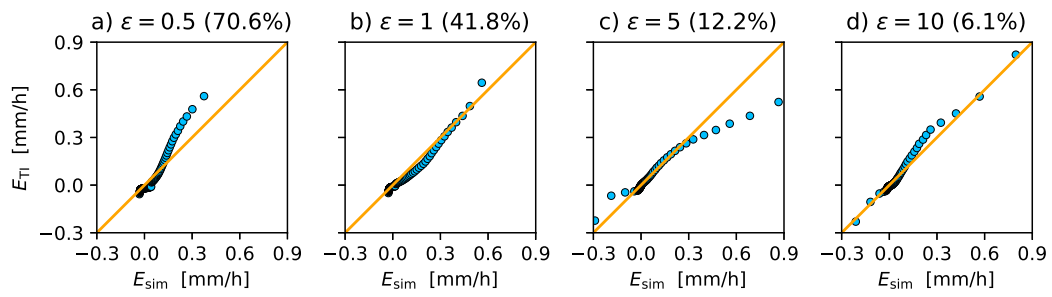


Figure 2: Q-Q plots of simulated  $E$  vs training  $E$  for different values of rejection threshold  $\varepsilon$ . For each value of  $\varepsilon$  it is also reported the percentage of rejected values (in brackets)

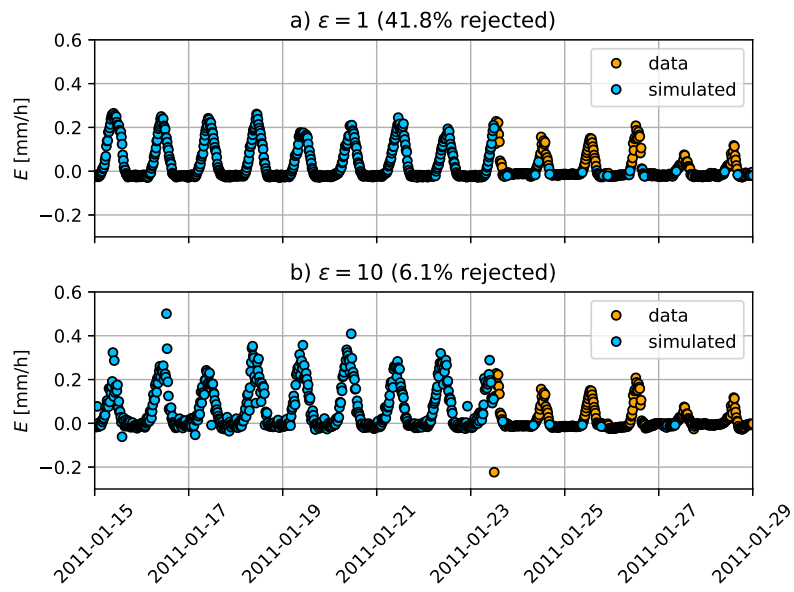


Figure 3: Comparison of two  $E$  time series obtained using two different values of rejection threshold  $\varepsilon$  for a heavily simulated time period (second half of January 2011)

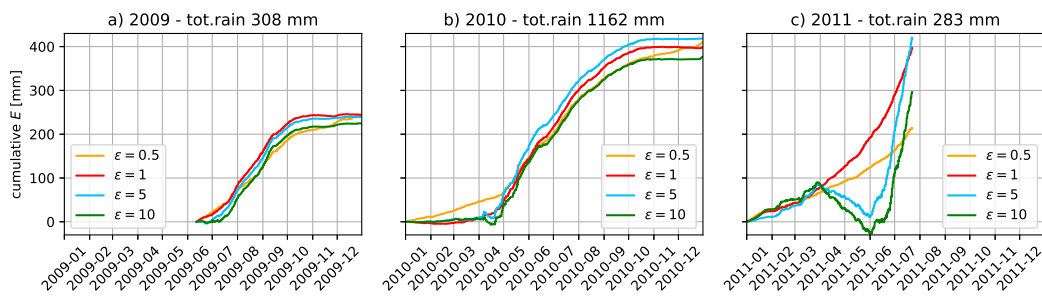


Figure 4: Cumulative  $E$  computed with the BRM for years a) 2009, b) 2010 and c) 2011. The different colors correspond to a different value of the rejection threshold  $\epsilon$ . Here the rejected values are replaced by DS simulation

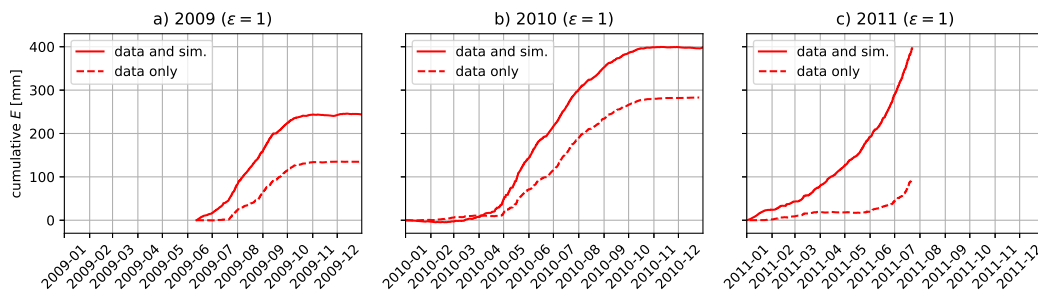


Figure 5: Cumulative  $E$  computed with the BRM for years a) 2009, b) 2010 and c) 2011. The continuous lines correspond to time series where the rejected values are replaced by DS simulation (data and sim.), while the dashed lines corresponds to time series where the rejected values are not replaced (data only)

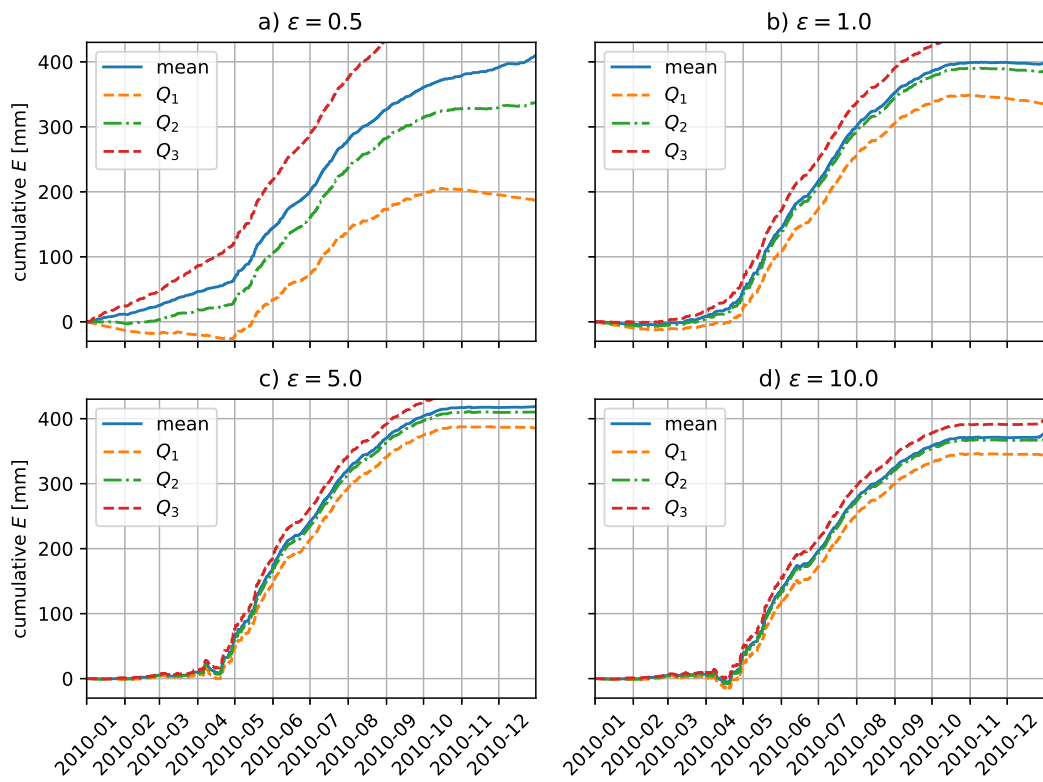


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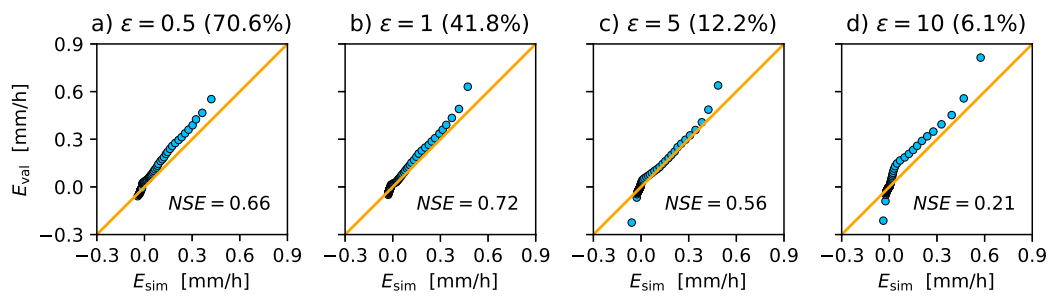


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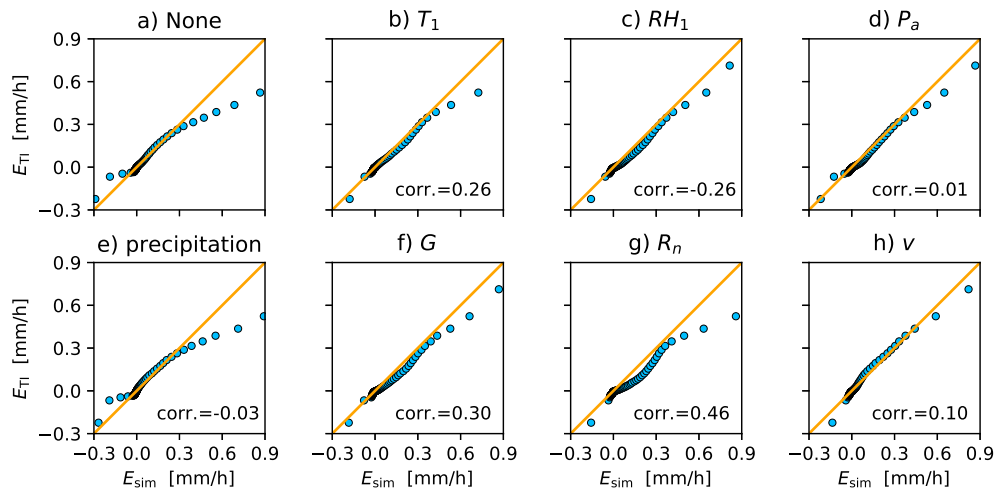


Figure 8: Q-Q plots of simulated  $E$  vs training  $E$  using different covariates. On the lower right corner Pearson's correlation coefficients

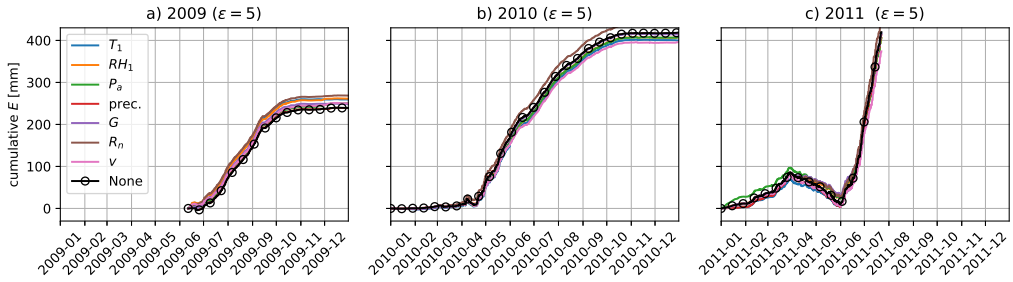


Figure 9: Cumulative  $E$  computed with the BRM for years a) 2009, b) 2010 and c) 2011. Unreliable values of  $E$  are rejected using a threshold  $\varepsilon = 5$ . The different colors represent a different covariate used in the DS simulation of the rejected values of  $E$ ; the black curve with markers represents the time series simulated taking into account for the variable  $E$  only

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Table 1: List of symbols and variables.  $i \in \{1, 2\}$ . For symbols related to the DS please refer to the text

symbol	units	description
$B$	–	Bowen ratio (computed)
$E$	mm/h	evaporation rate (computed/simulated)
$\varepsilon$	–	rejection threshold (user defined)
$h_i$	m	height above the ground of the sensor
$T_i$	K	temperature at $h_i$ (measured)
$RH_i$	%	relative humidity at $h_i$ (measured)
$P_a$	Pa	atm. pressure (measured)
$v$	m/s	wind speed (measured)
$R_n$	W/m <sup>2</sup>	net radiation (measured)
$G$	W/m <sup>2</sup>	soil heat flux (measured)
$C_a$	J/kgK	specific heat of air at constant pressure per unit mass
$\lambda_v$	J/kg	latent heat of evaporation per unit mass
$e_i$	Pa	vapor partial pressure at $h_i$ (derived from $RH_i$ )
$\rho_w$	kg/m <sup>3</sup>	water density
$\delta_E$	mm/h	uncertainty on $E$ (computed)
$E_{\text{sim}}$	mm/h	simulated values of $E$
$E_{\text{TI}}$	mm/h	training values of $E$
$E_{\text{val}}$	mm/h	values of $E$ kept for validation
$NSE$	–	Nash-Sutcliffe efficiency coefficient (computed)

Table 2: Percentage of data rejected for each season of the time series

		$\varepsilon$			
		0.5	1	5	10
Summer	2009	89.9 %	52.8 %	15.5 %	8.7 %
Autumn	2009	63.2 %	31.2 %	7.2 %	3.5 %
Winter	2009/2010	75.8 %	54.4 %	15.5 %	7.6 %
Spring	2010	74.7 %	46.8 %	14.0 %	7.4 %
Summer	2010	69.1 %	26.4 %	6.4 %	3.2 %
Autumn	2010	61.3 %	33.9 %	8.4 %	3.9 %
Winter	2010/2011	68.1 %	48.6 %	16.0 %	7.5 %
Spring	2011	70.4 %	46.8 %	15.8 %	7.7 %
Summer	2011	61.4 %	38.5 %	13.9 %	6.8 %
Total	2009	75.7 %	42.7 %	11.7 %	6.0 %
Total	2010	70.0 %	40.5 %	11.3 %	5.8 %
Total	2011	66.3 %	43.4 %	14.6 %	7.0 %
Total	2009, 2010, 2011	70.6 %	41.8 %	12.2 %	6.1 %

Table 3: Differences between the cumulated  $E$  computed by replacing the rejected data with the DS simulation and without replacing the rejected data. Units are in mm.

$\varepsilon$	2009	2010	2011
0.5	176	244	192
1.0	109	117	301
5.0	31	66	144
10.0	14	23	72