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# "NEW INSIGHTS IN ELECTRON DENSITY AND ELECTRON SPIN DENSITY THROUGH TOPOLOGICAL DESCRIPTORS BASED ON BADER'S THEORY OF ATOMS IN MOLECULES" 

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## INTRODUCTION:

1900 could be considered as year of birth of quantum mechanics, in fact in that year Max Plank has published his well known work on the distribution of the blackbody radiation ${ }^{[1]}$. Since that work, during the following 25 years, a huge amount of discussions and comparisons were done; this challenge has involved almost all the most important scientist of the last century, shaking the foundation of classical physics. In fact in 1925 W. K. Heisenberg published a landmark paper on quantum mechanics ${ }^{[2]}$ and, in 1927, he proposed the uncertainty principle ${ }^{[3]}$. This led to a new microscopic science, also helped by the experimental techniques that were becoming available in that period. The birth of quantum mechanics originated because classical physics models were unable to explain the following phenomena:
i) The problem of blackbody radiation: the classical electromagnetic theory does not interpret the spectrum emitted by hot black bodies
ii) The problem of specific heat in solids: according to classical statistical mechanics, all the energetic levels in a molecular system should equally contribute to the specific heat of a crystal, but this leads to an incorrect behaviour of thermal capacity with temperature $(\mathrm{T})$ at low T .
iii) The problem of atomic spectra: experiment shows that the radiations emitted (or absorbed) by elements are restricted to well-defined frequencies, typical of each element. This is in contradiction with the classical model relying on continuous electron energies.

The introduction of a quantum approach in chemistry was performed by Heitler and London ${ }^{[4]}$, that showed how the use of Schroedinger equation could help to explain chemical bonding. In any case Schrodinger formalism is unable to translate the outcome of a calculation in the usual chemical language. For this reason chemical paradigms (as for example the Lewis theory of chemical bonding ${ }^{[5]}$ ) are customarily used and the problem remains of finding a link between them and the rigorous quantum physics. A huge amount of effort has been done in the last century to meet this goal. The most general and useful approach is the introduction of descriptors, i.e. theoretical tools and procedures which yield information close to the classical chemical language and at the same time ultimately relies on the wavefunction. An interesting subset of descriptors is represented by the ones based on the Electron Density (ED) distribution which represents the probability of finding an
electron at the position $\mathbf{r}$ regardless the position and the spin of the other electrons within the molecular system. Electron density can be obtained from the wavefunction by

$$
\rho(\mathbf{r})=\int \Psi^{*}\left(\boldsymbol{r}_{1}, \boldsymbol{r}_{2}, \ldots, \boldsymbol{r}_{N} ; R\right) \Psi\left(\boldsymbol{r}_{1}, \boldsymbol{r}_{2}, \ldots, \boldsymbol{r}_{N} ; R\right) d_{\boldsymbol{S}_{1}} d_{\boldsymbol{r}_{2}, d_{\boldsymbol{S}_{2}} d_{\boldsymbol{S}_{3} \ldots d} \boldsymbol{S}_{N}, d_{\boldsymbol{r}_{N}} \text { eq. l }}
$$

where $\Psi$ represents the wavefunction, $r_{\mathrm{i}}$ and $s_{\mathrm{i}}$ are the space and spin coordinates of the i-th electron and R collectively indicates the position of nuclei; it is important to stress that eq. 1 is valid in the well known Born-Oppenheimer approximation so that the nuclei are considered static with respect electrons, which move in the field created by nuclei in their fixed positions. ED is a physical observable defined in real space and thus very suited for the study of chemical phenomena. Furthermore, as showed by Hohenberg and Kohn, ${ }^{[6]}$ the external potential of a molecular system is uniquely determined by its $\rho(\mathbf{r})$, i.e. energy is a functional of $\operatorname{ED}(\mathrm{E}[\rho(\mathbf{r})])$; as a consequence, all the properties of a system can be determined in principle by the knowledge of its $\rho(\mathbf{r})$.

Chemical descriptors based on Quantum Theory of Atoms in Molecules (QTAIM ${ }^{[7]}$ ) are the most used in our research group as they present a very important advantage: they can be applied on the same grounds to experimental and theoretical ED's. In fact $\rho(\mathbf{r})$ is not only a quantum mechanical observable, but it is also a measurable quantity. In particular it is possible to obtain the electron density distribution of a physical system from X-ray diffraction experiments, which measure structure factors that are the Fourier transform of $\rho(\mathbf{r})$

$$
\mathrm{F}_{\mathrm{hkl}}=\int_{V}<\rho(r)>e^{2 \pi H \cdot r} d r e q .2
$$

In eq. $2 \mathrm{~h}, \mathrm{k}, 1$ are the Miller indices which define vectors $H$ in the reciprocal space ${ }^{[8] 1}$. There exist several approaches to obtain $\rho(\mathbf{r})$ from X-ray diffraction data ${ }^{[9]}$, the most used is the multipolar model approach. A very relevant and important aspect of QTAIM is the possibility of partition molecules (and crystals) into atomic regions. Of course QTAIM is not the only method of partitioning the real space belonging to the physical system into atomic contributions, but it is the only one leading to quantum objects, whose energy may be defined unequivocally. The atomic basins are defined in Bader's theory by

$$
\nabla \rho(\mathbf{r}) \cdot \mathrm{n}(\mathbf{r})=0 \quad \text { eq. } 3
$$

where $\nabla \rho(\mathbf{r})$ is the gradient of the electron density distribution and $n(\mathbf{r})$ is the vector normal to the basin surface. All the points that fulfill eq. 3 define a zero-flux surface which encloses all the

[^0]electrons belonging to an atomic basin, the boundaries among atoms being defined by the zero-flux surfaces. The atomic regions so defined are non-overlapping and exhaustive and all the atomic basins built by eq. 3 are defined as proper quantum open systems. A very important consequence is that in a system all molecular properties (volume, charge, electrostatic moments, energy, etc.) can be partitioned into atomic contributions. One fundamental aspect of QTAIM is the study of $\rho(\mathbf{r})$ in terms of its scalar field topology. It is performed through the analysis of the critical points (CPs), i.e. those points where the gradient of the electron density vanishes. Critical points are labeled by two numbers $m$ and $n$, the rank ${ }^{2}$ of the CP and the algebraic sum of the signs of the curvatures. For topologically stable structures, $\mathrm{m}=3$; as consequence, for them it is possible to distinguish four types of CPs, each of which indicates univocally a structural feature of the system:

- (3,-3) are maxima in the $\rho(\mathbf{r})$ distribution, are (roughly) located at the position of nuclei (with a few exceptions ${ }^{3}$ ) and are thus associated to them. Since all the gradient lines terminate at these maxima, they are also called 3D attractors.
- $(3,-1)$ are saddle points called bond critical points (BCPs); this kind of CPs are particularly important because they are related to chemical interactions.
- $(3,+1)$ are saddle points which are found at the center of rings (ring critical points, RCP).
$\cdot(3,+3)$ are minima in ED, associated to cages and corresponding to the minimum ED values within them .

In QTAIM, the line formed by the juxtaposition of the two $\nabla \rho(\mathbf{r})$ trajectories connecting two $(3,-3)$ critical points is defined as bond path (BP). The bcp lies at the minimum ED along the bond path, along which $\rho(\mathbf{r})$ is maximally concentrated with respect to any other direction. In general in a molecular system all the chemical bonds supposed by a chemist are topologically described by a bond path but the inverse relationship not always holds In fact in many cases BPs are found among atomic basins whose interaction would be classified as repulsive by common chemical thinking (e.g. among anions in a crystal). ${ }^{[10]}$

This Ph.D. thesis is focused on the application of QTAIM based chemical descriptors to challenging chemical test-cases, as well as on the development of novel topological descriptors, like the Source Function for the spin density.

The thesis is organized as follows:
In chapter 1 the ED of a very unusual structural feature in a synthetic $\beta$-sultamic analogue (DTC) ${ }^{[11,12]}$, has been explored by both low-T single-crystal X-ray diffraction and quantum mechanical simulations to gain insights into the subtle interplay between structure, electron

[^1]delocalization and crystal field polarization effects. The core chemical moiety in DTC is an uncommon 4-membered thiazete-1,1-dioxide heterocycle, where the formally single $\mathrm{N}-\mathrm{C}$ bond is, on average, $0.018 \AA$ shorter than the formally double $\mathrm{N}=\mathrm{C}$ bond. Both local and non-local topological descriptors provided by QTAIM have been employed in the analysis of DTC in comparison with chemically related derivatives and possible implications from the viewpoint of the accurate in silico modelling of crystal structures are discussed. Particular attention is dedicated on such kind of issues in chemical and pharmaceutical industries, because the control of the crystal structure is really problematic in some cases; in fact different polymorphs of the same substance have different intensive physical properties, such as solubility, refraction index and conductivity and problems may arise in industrial processes related to the synthesis of chemicals and drugs on large scale ${ }^{[13]}$. Results of this part of work have been published in $\operatorname{Ref}$ [12, 14].

In chapter 2, we focused on the source function (SF) QTAIM based topological descriptor. The ED at any point r within a system may be regarded as consisting of a sum of Source Function (SF) contributions $\mathrm{S}(\mathrm{r} ; \Omega)^{[15]}$ representing a measure of how the various atomic basins or groups of atomic basins defined through QTAIM contribute to determine the $\rho(\mathrm{r})$ at r . Recently it was shown that the SF is able to reveal electron delocalization effects in planar electron conjugated systems, in terms of an increased capability of determining the ED along a given bond by the distant, though through-bonds connected, atomic basins and, at the same time, into a decreased ability to do so by the two atoms directly involved in the bond. Such an adjustment of sources then translates into a pictorial pattern of enhanced and reduced atomic SF contributions from, respectively, distant and nearby atoms, compared to the case of a partially or fully saturated network of bonds. ${ }^{[16,17]}$

In the present PhD thesis, we have extended such an analysis to the non planar conjugated systems, where the usual $\sigma / \pi$ electron separation does no longer apply. Being based on the total ED, the SF analysis may be safely applied also in these less conventional electron delocalized systems. The obtained results have been published in Ref. [18]. Then we have extended the SF reconstruction approach also to the electron density spin counterparts ${ }^{[19]}$ in vacuo. Such reconstruction was investigated both on simple (but chemically meaningful) spin-polarized molecular systems ${ }^{[19]}$ and on more complex single-molecule magnets ${ }^{[18,20]}$. This investigation has showed that the difference between the two spin counterparts of electron density distribution can be reconstructed with a sufficient accuracy, analogously to the case of the total $\mathrm{ED}^{[19]}$. Moreover, it was found that the SF for the electron spin density brings in precious chemical information, neatly distinguishing the quite different roles played by the unpaired electrons ED and the spin polarized ED due to the remaining electrons ${ }^{[19]}$. Furthermore, quantitative answers to questions related to the transferability of the spin density in alkyl radicals ${ }^{[18]}$ or to the transmission of spin information in metal(s)-ligand systems
were provided ${ }^{[20]}$. Understanding, from a real space perspective, by which mechanisms spin information transmits, might be of relevance to interpret the fundamental magnetic interactions present in complex materials, such as for example coordination polymers or Heussler and halfHeussler alloys ${ }^{[21]}$. As these interactions have a key role in spintronics, characterization of the chemical bond and interpretation of the electron spin density distributions in these systems through the SF analysis, could hopefully disclose structure-property relationships extremely useful for the design of materials with particular physical properties.

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## CHAPTER 1

## Single N-C bond becomes shorter than

 formally double $\mathrm{N}=\mathrm{C}$ bond in a thiazete-1,1dioxide crystal: an experimental and theoretical study of strong crystal field effects
### 1.1 Introduction

In modern theoretical and applied chemistry, electron localization and delocalization effects play an important role, providing an easy-to-grasp conceptual framework to forecast and rationalize molecular structure and reactivity. ${ }^{[1,2]}$ Furthermore, these effects are also rooted at the core of several relevant molecular properties, such as the well-known requirement of bond length alternation to prompt nonlinear optic responses. ${ }^{[3,4]}$ Translating the description of bonding (de)localization from the realm of quantum mechanics to the language of the electron density, $\rho(\mathbf{r})$, has been a major object of study during the past decades. ${ }^{[5,8]}$ In this sense one of the most popular density-based tool to explore the chemical bond in the real space is the Quantum Theory of Atoms in Molecules (QTAIM) developed by R. F. W. Bader ${ }^{[5]}$ and co-workers in early 90 s. ${ }^{[9]}$ Since $\rho(\mathbf{r})$ is a scalar field which is also a quantum-mechanical observable, it is accessible from both theoretical simulations and accurate single-crystal X-ray tests carried out at low temperature, ${ }^{[10]}$ as already pointed out in the introductory chapter of this thesis. In a physical perspective, the root of localization and delocalization effects actually consists in the correlated motion of electrons, that can be fully described by the two-electron (pair) density and by the consequent 'electron sharing indices' (ESI). ${ }^{[11]}$ Among the latter, localization, $\lambda(\mathrm{A}, \mathrm{A})$, and delocalization, $\delta(\mathrm{A}, \mathrm{B})$ indices are undoubtedly the most widely used ESI. ${ }^{[12]}$ When employed in the QTAIM framework, they provide a direct estimate of the number of electrons localized within the same QTAIM atomic basin A, and, respectively, of the number of electron pairs delocalized between a couple of atomic basins A and B, regardless their nuclei are connected by a bond path or not. Even though these pair density-based indices are not experimentally accessible, investigating non-local electronic effects is possible thanks to the Source Function (SF) descriptor. ${ }^{[13]}$ (For an introduction to the SF, see Chapter 2). Although SF lacks of any direct connection with pair density, it can provide indirect hints on the magnitude of electron delocalization within the system, revealing how the individual atomic basins influence both their close and far surroundings. ${ }^{[14]}$ Moreover, SF is easily computed from the charge density Laplacian, $\nabla^{2} \rho(\mathbf{r})$, and it allows to relate the electron density at every reference point $\mathbf{r}$ to the influence that each atomic basin has on determining the electron density at that point.

Electron delocalization features may be also deeply influenced by crystal packing: for example, the energy gain caused by electrostatic interactions among molecules in the crystal may strengthen the role of those molecular resonance forms leading to higher charge separation in the molecule. ${ }^{[15]}$ The result of this process is often a remarkable enhancement of the molecular dipole moment $\boldsymbol{\mu}$ in the crystal ${ }^{[15,16]}$ : as revealed by a ground-breaking work on urea crystal ${ }^{[15 a]}$, $|\boldsymbol{\mu}|$ increases in the crystal respectively by $37 \%$ and by $53 \%$ relative to the isolated molecules at crystal
or at in vacuo optimized geometry. The main cause of such large dipole moment enhancement in the bulk can be attributed to the significant magnitude increase of the charge transfer component $\mu_{\mathrm{CT}}$, which is a measure of charge separation among the atoms in the molecule.
More in detail the total molecular dipole is given by ${ }^{[45]}$

$$
\mu=\mu_{\mathrm{A}}+\mu_{\mathrm{CT}}
$$

where $\mu_{\mathrm{A}}$ is the atomic polarization term due to the atomic first moments $\mu_{\Omega}$ and it is evaluated as

$$
\begin{gathered}
\boldsymbol{\mu}_{\mathrm{A}}=\Sigma_{\Omega} \boldsymbol{\mu}_{\Omega} \\
\boldsymbol{\mu}_{\Omega}=-\int_{\Omega} \rho(\mathbf{r}) \mathbf{r}_{\Omega}
\end{gathered}
$$

with $\mathbf{r}_{\Omega}$ being the local atomic position vector $\mathbf{r}_{\Omega}=\mathbf{r}-\mathbf{X}_{\Omega}$, defined relative to its associated nucleus position $\mathbf{X}_{\Omega}$. The charge transfer (CT) component $\boldsymbol{\mu}_{\mathrm{CT}}$ is evaluated as

$$
\mu_{\mathrm{CT}}=\Sigma_{\Omega} \mathrm{q}_{\Omega} \mathbf{X}_{\Omega}
$$

where $\mathrm{q}_{\Omega}$ is the net charge of atom $\Omega$, obtained by

$$
\mathrm{q}_{\Omega}=\mathrm{Z}_{\Omega}-\mathrm{N}_{\Omega}
$$

$\mathrm{Z}_{\Omega}$ and $\mathrm{N}_{\Omega}$ being the nuclear charge and the atomic electron population of $\Omega$.
In this chapter, we're going to focus on the experimental and theoretical charge density distribution of 3-diethylamino-4-(4-methoxyphenyl)-1,1-dioxo-4H-1 $\lambda^{6}$,2-thiazete-4-carbonitrile, a synthetic thiazete-1,1-dioxide derivative (hereinafter DTC). As shown in Scheme 1 and Figure 1, DTC's core structure shows a significant similarity with 4 -membered $\beta$-sultam antibiotics. ${ }^{[17]}$ The central moiety of the title compound is a heavy functionalized four-membered 1,2-thiazete-1,1-dioxide ring bearing a N -bonded sulfonyl group.


Scheme 1


Fig. 1: Experimentally-derived asymmetric unit of DTC at $T=100(2) \mathrm{K}$, with the atom numbering scheme. Thermal ellipsoids are drawn at $50 \%$ probability level.

This system shows remarkable unusual features: out of the 632626 entries within the current release of the Cambridge Structural Database (CSD), ${ }^{[18]}$ just $16(0.03 \%)$ contain a 4-membered ring bearing a $\mathrm{N}-\mathrm{SO}_{2}$ system. Furthermore, most of them are 1,2-thiazetidine derivatives, i.e. their heterocyclic core is completely saturated. Just DTC ${ }^{[19]}$ (codes: LOZII, LOZII2) and one closely related compound ${ }^{[20]}$ (code: TAYCUR) display the unsaturated thiazete ring. At a structural level, a very unusual bonding feature was revealed by former room-temperature (RT) crystallographic investigation within the independent atom model (IAM) approximation ${ }^{[21]}$ on different DTC polymorphs ${ }^{[19]}$ and TAYCUR ${ }^{[20]}$ : in the $-\mathrm{N}-\mathrm{C}=\mathrm{N}-\mathrm{SO}_{2}-$ moiety (Scheme 1), the formally single $\mathrm{N}-$ C bond is indeed found to be, on average, $0.018(3) \AA$ shorter than the formally double $\mathrm{N}=\mathrm{C}$ bond. In the current CSD release just other two structures, ${ }^{[22]}$ markedly different from DTC, show a $\mathrm{R}_{2} \mathrm{~N}-$ $\mathrm{C}=\mathrm{N}-\mathrm{R}(\mathrm{R}=$ any substituent $)$ bond pattern where $d_{\mathrm{C}-\mathrm{N}}<d_{\mathrm{C}=\mathrm{N}}$, being $d$ the geometric bond length. Thus, a deep investigation of the DTC crystal seems to be particularly intriguing as it may shed light on the subtle interplay between electron delocalization and crystal field polarization effects. By comparing a series of in vacuo systems, including DTC molecule and DTC crystal, our analysis aims to clarify the peculiar properties of the uncommon conjugated $-\mathrm{N}-\mathrm{C}=\mathrm{N}-\mathrm{SO}_{2}-$ moiety and how crystal packing influences them. Considering the relevance of accurate estimates in describing the geometry of the conjugated bond patterns in DTC crystal and the electronic effects that cause them, we performed single-crystal X-ray diffraction experiments at low $T$ in order to deconvolute the thermal motion from the static electron density and to provide better estimates either of geometrical and electronic parameters.

### 1.2 Materials and Methods

### 1.2.1 X-ray diffraction

We performed X-ray data collections with graphite-monochromated Mo K $\alpha$ radiation ( $\lambda=0.71073$ Á) at a nominal source power of $50 \mathrm{kV} \times 30 \mathrm{~mA}$ on a three-circle Bruker SMART APEX II goniometer equipped with a CCD area detector and an Oxford Cryostream $\mathrm{N}_{2}$ gas blower; details of synthetic route to obtain title compound have been reported elsewhere. ${ }^{[19 a]}$ We employed the SAINT program package ${ }^{[23]}$ throughout to obtain data reductions and the final dataset results by merging diffraction data collected on two distinct crystals at $T=100(2) \mathrm{K}$. A detailed description of the experimental procedure can be found in the appendix A1; Table 1 summarizes the overall statistics of the data employed for the charge density analysis. ${ }^{[24]}$ Generally, the completeness was as large as $99.7 \%$, with an internal agreement factor $R_{\text {int }}$ as low as 0.0443 .

| Crystal data | $F_{\text {exp }}$ |
| :--- | :--- |
| $a(\AA)$ | $8.5421(26)$ |
| $b(\AA)$ | $13.2390(6)$ |
| $c(\AA)$ | $13.0443(40)$ |
| $\beta(\mathrm{deg})$ | $95.079(26)$ |
| $V\left(\AA^{3}\right)$ | $1469.37(35)$ |
| Density $\left(\mathrm{g} \cdot \mathrm{cm}^{-3}\right)$ | 1.389 |
| Crystal size $(\mathrm{mm})$ | $/ /$ |
| Data collection $\left(\sin \vartheta / \lambda_{\text {MAX }}\right)=0.65 \AA^{-1} / 0.90 \AA^{-1}$ |  |
| Measured reflections | $86720 / 157389$ |
| Unique reflections | $3375 / 8956$ |
| $I>2 \sigma(I)$ reflections | $3117 / 7688$ |
| Completeness $(\%)$ | $100.0 / 99.7$ |
| $R_{\text {int }}$ | $0.0397 / 0.0441$ |
| Refinement |  |
| $R(F)$, wR $\left(F^{2}\right)$, Goodness-of-fit ${ }^{4}$ | $0.0297,0.0798,0.999$ |
|  | $0.0168,0.0290,1.099$ |
| $\Delta \rho_{\text {min }}, \Delta \rho_{\text {max }}\left(\mathrm{e} \AA^{-3}\right)$, data-to-parameters ratio | $-0.341,+0.372,13.80$ |
| Experimental $\left(F_{\text {exp }}\right)$ spherical $\left(\zeta_{=}=\kappa \alpha\right)$ and | $-0.144,+0.151,13.37$ |
| deformation $\left(\zeta^{\prime}=\kappa^{\prime} \alpha^{\prime}\right)$ exponents | $\mathrm{S}: \zeta=4.306, \zeta^{\prime}=4.26(2), 4.54(1)$ |
|  | $\mathrm{O}: \zeta=4.345, \zeta^{\prime}=4.98(2)$ |
|  | $\mathrm{N}: \zeta=3.797, \zeta^{\prime}=3.28(1)$ |

Table 1: Data collection statistics and relevant refinement details of the ' A ' polymorph of DTC $\left(\mathrm{C}_{14} \mathrm{H}_{17} \mathrm{~N}_{3} \mathrm{O}_{3} \mathrm{~S}\right.$, molecular weight $307.37 \mathrm{~g} \mathrm{~mol}^{-1}$, space group $\mathrm{P}_{1} / \mathrm{n}, \mu=0.234 \mathrm{~mm}^{-1}, \mathrm{~F}_{\text {000 }}=648 e$ ).

[^2]
### 1.2.2 In vacuo quantum mechanical calculations

For the in vacuo simulations we employed the Gaussian09 program. ${ }^{[25]}$ The non-local hybrid DFT B3LYP Hamiltonian, ${ }^{[26]}$ in conjunction with a $6-311 \mathrm{G}(\mathrm{p}, \mathrm{d})$ basis set ${ }^{[27]}$ was selected. Full geometry optimizations were performed on (i) DTC, (ii) the two independent molecules in the asymmetric unit of TAYCUR ${ }^{[20]}$ and (iii) a series of appropriate model systems for investigating the covalent bonding properties of the $\mathrm{N}-\mathrm{C}-\mathrm{N}-\mathrm{SO}_{2}$ atom sequence. To guarantee that a true energy minimum has been effectively reached, we performed full vibration mode analyses. We also performed a single-point calculation on the DTC molecule in vacuo, keeping frozen the atomic coordinates to those determined by the X-ray diffraction experiment at $T=100 \mathrm{~K}$. In all this chapter, $\rho_{\mathrm{VQm}}$ and $\rho_{\text {VQM-FROZEN }}$ label, respectively, the charge density distributions corresponding to the in vacuo relaxed and frozen geometries. An analysis of charge density topologies was carried out by a modified version of the PROAIM program package. ${ }^{[28]}$

### 1.2.3 Solid-state quantum mechanical calculations

We employed the same B3LYP ${ }^{[26]}$ Hamiltonian and $6-311 \mathrm{G}(\mathrm{p}, \mathrm{d})$ basis set ${ }^{[27]}$ used for in vacuo calculations, for the single-point periodic wavefunction calculation of DTC corresponding to the experimentally determined crystal structure at $T=100 \mathrm{~K}$ using the CRYSTAL09 program. ${ }^{[29]}$ The Fourier transform of the periodic wavefunction was employed to compute a set of $\approx 9000$ theoretical structure factor amplitudes, $F_{\text {theo }}$, within the same $0.9 \AA^{-1}$ resolution in $\sin \vartheta / \lambda$ as the experimental dataset. Then, these synthetic data have been employed to obtain a multipoleprojected charge density distribution, hereinafter referred to as $\rho_{\mathrm{MM}-\mathrm{PQM}}(\mathrm{MM}=$ Multipole Model; PQM= Periodic Quantum Mechanical), while its related primary density, i.e. before the multipole model projection, is referred to as $\rho_{\mathrm{PQM}}$.

### 1.3 Multipole analysis

In order to extract the static charge density ( $\rho_{\mathrm{EXP}}$ ) from the observed squared structure factor amplitudes ( $F^{2}$ exp $)$ at $T=100 \mathrm{~K}$ we employed the Hansen-Coppens multipole formalism ${ }^{[30]}$ as implemented in the XD2006 software package ${ }^{[31]}$. The multipole-projected density $\rho_{\text {MM-PQM }}$ was instead refined against $F_{\text {theo }}$ (see Section 5.3). See Table 1 for global refinement parameters, while a full desciption on the multipole refinement can be found in the appendix A1 along with a full assessment of the final least-squares model from the statistical and physical viewpoints ${ }^{[32]}$. The final
model employed a multipole expansion up to $l=4$ for $\mathrm{S}, l=3$ for $\mathrm{C}, \mathrm{O}, \mathrm{N}$ and $l=2$ for H . The description of thermal motion of hydrogen atoms as anisotropic was performed by means of the SHADE2 server. ${ }^{[33]}$

### 1.4 Results and discussion

### 1.4.1 Bond conjugation effects in the thiazete ring: gas-phase results

For as we know, 1,2-thiazetidine or 1,2-thiazete rings have never been investigated before in terms of a charge density analysis. Thus, quantum-mechanical calculations on a series of chemically related derivatives, i.e. methanimidamide, 1-(methylsulfonyl)-methanimidamide and 3-amino-1,1-dioxo-4H-1 $\lambda^{6}, 2$-thiazete-(Scheme 2, structures $1-3$ ) were performed in order to understand the basic conjugation effects in the DTC heterocycle.



4


5


6

Scheme 2
Moreover, we considered the minimum geometries of isolated DTC (Scheme 2, structure 4) and of both the symmetry-independent molecules of TAYCUR (Scheme 2, structure 5). ${ }^{[20]}$ Since the latter show a marked similarity in terms of chemical bonding descriptors, ${ }^{[34]}$ in the following discussion
we shall consider the related average values. The analogue fully saturated 3 -amino-1,1-dioxothiazetidine cycle (Scheme 2, compound 6) was also employed as a proper unconjugated reference. A further examination of those individual local and non-local topological descriptors for the thiazete cycle not openly discussed in the text have been reported in the appendix A1 as well as the delocalization indices and integrated Source Function.

### 1.4.2 Bond lengths and charge density at the bcp

Considering conjugated systems, the measure of individual bond lengths through adjacent bonds allows to provide a first indication of remarkable electron localization or delocalization effects. ${ }^{[3]}$ Differently with the solid-state X-ray results, all the evaluated gas-phase systems show the bond length alternation pattern predicted by the supposedly dominant resonance structure $a$ (or $a^{\text {') }}$ displayed in Scheme 3, ${ }^{[35]}$ as $d_{\mathrm{C}=\mathrm{N}}$ invariably results to be shorter than $d_{\mathrm{C}-\mathrm{N}}$ in all the conjugated structures 1-5 (see tab. 2).
(i)

( $\left.a^{\prime}\right) \quad\left(b^{\prime}\right) \quad\left(c^{\prime}\right)$
(ii)



Scheme 3
Regarding the not-conjugated structure $\mathbf{6}$, a bond alternation scheme more similar to the X-ray one, with the exocyclic $\mathrm{C} 9-\mathrm{N} 1$ bond shorter than the in-cycle $\mathrm{C} 9-\mathrm{N} 2$ bond was instead retrieved. The possible influence of the electron correlation on the refined geometrical parameters was also checked: we employed the same $6-311 \mathrm{G}(\mathrm{p}, \mathrm{d})$ triple zeta basis set to perform geometry optimizations on the isolated DTC molecule at the PBE0, ${ }^{[36]}$ M06 ${ }^{[37]}$ and MP2 ${ }^{[38]}$ levels of theory, resulting in the geometrical results reported in appendix A1. However, all the levels of theory adopted provided the same $d_{\mathrm{C}=\mathrm{N}}<d_{\mathrm{C}-\mathrm{N}}$ result, suggesting that crystal field effects may be
essentially the cause of the bond length inversion in crystalline DTC. In the following discussion we will always refer - if not otherwise specified - to the B3LYP results and we will investigate the variation of the bond lengths and the related charge density properties within the core $\mathrm{N}-\mathrm{C}=\mathrm{N}$ moiety, as its degree of similarity with the title compound increases (see figure 2). Table 2 and Figure 2a (red triangles) show that, on shifting from system $\mathbf{1}$ to $\mathbf{5}$, the $\mathrm{C} 9=\mathrm{N} 2$ bond distance undergoes a monotonic lengthening (up to $\approx+3.9 \%$ ), while its conjugated $\mathrm{C} 9-\mathrm{N} 1$ bond (red circles) similarly shortens by almost the same amount ( $\approx-3.4 \%$ ). Defining a 'bond length difference parameter', BDP , as $d_{\mathrm{C} 9-\mathrm{N} 1}-d_{\mathrm{C} 9=\mathrm{N} 2}$, i.e. as the distance between the red curves in Figure 2a, the latter amounts to $0.11 \AA$ in the conjugated methanimidamide $\mathbf{1}$, but reduces to $\approx 0.02-0.01 \AA$ in DTC and TAYCUR. The nature of the substituents at C8 has a minor influence on the thiazete properties since generally, all the geometric and topological point descriptors for compounds 4 and 5 are quite similar. The formally single and formally double C-N bond distances show respectively the largest decrease $(-0.037 \AA)$ and the largest increase $(+0.018 \AA)$ going from 1 to $\mathbf{2}$, upon insertion of the electron-attractor sulfonyl group. This may be clearly related to the attained availability of resonance forms $c-e$ (and $g-h$, Scheme 3) after introducing such group, while the different S-N distances in systems 2-5 (see tab. 2) may match to different relative weight of the resonance structures $a, b, c-d, e, g-h$ in such compounds.

|  | $1^{1}$ | $2^{2}$ | $3^{3}$ | $4^{4}$ | $5^{5}$ | $6^{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bonds |  |  |  |  |  |  |
| S1-N2 | $/ /$ | 1.6916 | 1.7277 | 1.7013 | 1.6963 | 1.7149 |
| N2=C9 | 1.2721 | 1.2896 | 1.3048 | 1.3159 | 1.3212 | 1.5109 |
| C9-N1 | 1.3799 | 1.3434 | 1.3401 | 1.3330 | 1.3327 | 1.4312 |
| C9-C8 | $/ /$ | $/ /$ | 1.5125 | 1.5407 | 1.5349 | 1.5486 |
| S1-C8 | $/ /$ | 1.7992 | 1.8577 | 1.9686 | 1.9465 | 1.8251 |
| Angles |  |  |  |  |  |  |
| S1-N2-C9 | $/ /$ | 115.2 | 91.9 | 95.0 | 94.5 | 93.8 |
| N2-C9-N1 | 129.3 | 121.8 | 125.8 | 125.0 | 124.1 | 116.4 |
| N2-C9-C8 | $/ /$ | $/ /$ | 108.2 | 108.5 | 108.1 | 94.9 |
| N2-S1-C8 | $/ /$ | 100.2 | 79.1 | 78.1 | 78.6 | 79.1 |
| Torsions |  |  |  |  |  |  |
| S1-N2-C9-C8 | $/ /$ | $/ /$ | 0.0 | -2.5 | 2.1 | 16.4 |
| S1-N2-C9-N1 | $/ /$ | -177.6 | 180.0 | 177.8 | -176.1 | 136.5 |
|  |  |  |  |  |  |  |

Table 2: Bond length and angles estimates ( $\AA$, deg) as retrieved from the gas-phase quantum-mechanical optimizations of compounds $1-6$ at the B3LYP $6-311 \mathrm{G}(\mathrm{p}, \mathrm{d})$ theory level. See Figure 1 and Scheme 2 for the atom numbering.

[^3]As expected, ${ }^{[5,8,9]}$ at the bond critical point (bcp), a contravariant correspondence occurs between the changes in bond distances and the adjustments of the electron density $\rho_{\mathrm{bcp}}$ : the shorter the bond, the greater the electron density value at the related critical point (dashed lines in Figure 2a), so that the $\rho_{\text {bcp }}$ values prove to be remarkably more similar in the substitutes thiazete eterocycles than in the linear compounds $\mathbf{1}$ and 2.

### 1.4.3 Charge density Laplacian and bond ellipticities

Looking for further details, we shall consider the electron density Laplacian at the bond critical point, $\nabla^{2} \rho_{\mathrm{bcp}}$, and the related bond ellipticity, $\varepsilon$ (Figure 2b). It is defined as $\varepsilon=\left(\lambda_{1} / \lambda_{2}-1\right)$, with $\lambda_{1}$ and $\lambda_{2}$ being the two negative curvatures of the $\rho(\mathbf{r})$ distribution at the bcp, and it measures the electron density accumulation in the plane orthogonal to the bond path. ${ }^{[5,6]}$ Specifically, the eigenvector related to $\lambda_{2}$ describes the major axis of the elliptical contour of the electron density about the bond path. Homopolar conjugated and aromatic systems show adjacent bonds with $\varepsilon>0$ and major axes tend to be parallel to each other. ${ }^{[6,39]}$


Figure 2: Point topological descriptors for the $\mathrm{N}-\mathrm{C}=\mathrm{N}$ bond pattern in gas-phase optimized molecules $\mathbf{1 - 5}$ (Scheme 2). Quantities referring to the $\mathrm{C} 9=\mathrm{N} 2$ bond are marked as triangles, those referring to $\mathrm{C} 9-\mathrm{N} 1$ as circles. (a) bond length (full red lines, left scale) and electron density at the bcp (dotted blue lines, right scale); (b) bond ellipticity (full red lines, left scale) and electron density Laplacian at the bcp (dotted blue lines, right scale).

On the contrary, bond ellipticity has a less straightforward interpretation in heteropolar bonds ${ }^{[40-42]}$ as the bcp usually falls in the valence shell charge concentration (VSCC) ${ }^{[5]}$ of the less
electronegative atom, expected therefore to rule the direction of the major bond axis. ${ }^{[4]]}$ The overlap of major axes of neighbouring bonds in the $-\mathrm{N}-\mathrm{C}=\mathrm{N}(\mathbf{1})$ or $-\mathrm{N}-\mathrm{C}=\mathrm{N}-\mathrm{S}(\mathbf{2 - 5})$ moieties was very close to one (>0.9985 at least) for all 1-5 compounds. Moreover, ellipticities retrieved in all of these bonds are significant in absolute value. On the other hand, the $\mathrm{p}-\pi$ system in the sulphonyl group shows no remarkable overlap (<0.3) with the $\pi$ system in the $-\mathrm{N}-\mathrm{C}=\mathrm{N}-\mathrm{S}$ moiety. Hence, the two systems are substantially decoupled, as for the resonance effects. Considering figure 2 b , the two $\mathrm{C}-$ N bonds clearly display quite a different behaviour through the series of compounds $\mathbf{1 - 5}$. In the formally single C9-N1 bond a neat increase of the magnitude of the electron density Laplacian occurs at the bcp (Figure 2b, open blue circles), while for the double $\mathrm{C} 9=\mathrm{N} 2$ bond (open blue triangles) $\nabla^{2} \rho_{\mathrm{bcp}}$ tends to oscillate; eventually, the title compound (4) and TAYCUR (5) have quite similar $\nabla^{2} \rho_{\mathrm{bcp}}$ values with respect to the reference methanimidamide $\mathbf{1}$. Such trends are reflected in bond ellipticities, since $\varepsilon_{\mathrm{C} 9-\mathrm{N} 1}$ (full red circles) almost monotonically grows to values very similar to those shown by the double bond $\mathrm{C} 9=\mathrm{N} 2$ in compounds 4 and $\mathbf{5}$, while $\varepsilon_{\mathrm{C} 9=\mathrm{N} 2}$ (red full triangles) displays a clear ellipticity minimum connected to the lower Laplacian magnitude in $\mathbf{2}$ and then grows again stabilizing at a value slightly smaller than that in 1 , namely at $\approx 0.20-0.22$. For both $\varepsilon$ and $\nabla^{2} \rho_{\mathrm{bcp}}$, the most abrupt and off-trend variations clearly concern the $\mathrm{C} 9=\mathrm{N} 2$ bond upon insertion of the electron-attractor sulfonyl group at the N 2 atom ( $\mathbf{1}$ to $\mathbf{2}$ transition). On the contrary, once the 4 -membered cycle is formed ( $\mathbf{2}$ to $\mathbf{3}$ transition), the N2-S1 bond weakens, as it lengthens by 0.0361 $\AA$ (Table 2), while the $\nabla^{2} \rho_{\mathrm{bcp}}$ value for the adjacent $\mathrm{C} 9=\mathrm{N} 2$ bond turns out to be even more negative than in methanimidamide 1 . However, the related $\rho_{\mathrm{bcp}}(\mathrm{C} 9=\mathrm{N} 2)$ grows only by $0.01 \mathrm{e} \cdot \AA^{-3}$ while $d_{\mathrm{C} 9=\mathrm{N} 2}$ increases its length even further (Figure 2a). Looking for the possible origin of such apparently inconsistent behaviour we have to consider the mutual interplay of several factors: (i) the electronic factors originated by the insertion of the $\mathrm{SO}_{2}$ group; (ii) the ring strain, revealing itself in the general weakening of the bonds of the cycle relative to the analogue linear compounds, and (iii) the sensitivity of the electron density (ED) Laplacian to the position of the bcp along the internuclear vector in polar bonds, as $\nabla^{2} \rho(\mathbf{r})$ is a fast varying function of the position of the point considered in those VSCC zones lying close to the core depletion region.


1


3


$4 \rho_{\text {vqM-FROZEN }}$


Figure 3: Location of $-\nabla^{2} \rho(\mathbf{r})$ non-bonded maxima around N1 (purple dots, see text), together with relevant bond lengths ( $\AA$ ) and QTAIM integrated charges (electrons) for case systems $\mathbf{1 - 4}$ (see Scheme 2 and the text for the meaning of the various labels). 'Et' stands for ethyl group.

By inspecting resonance forms in Scheme 3 and analysing the VSCC non bonded maxima (nbms), it is possible to see how the abrupt reduction of the $\mathrm{C}=\mathrm{N}$ ellipticity and Laplacian magnitude from $\mathbf{1}$ to 2 are triggered by the increased availability of resonance forms like $c-e$, as confirmed and pictorially visible by a corresponding abrupt variation, from $s p^{3}$ to $s p^{2}$ hybridization of the N involved in the formally single $\mathrm{C}-\mathrm{N}$ bond. Figure 3 displays the remarkable pyramidalization this N atom acquires in $\mathbf{1}$, with a $\mathrm{N}-\mathrm{H}-\mathrm{C}-\mathrm{H}^{\prime}$ torsion of about $20^{\circ}$, having just one non bonded maximum (nbm) in its VSCC and forming a nbm-N-C angle, hereinafter referred to as $\alpha$ angle, of about $97^{\circ}$. The corresponding N atom in 2 shows a significant pyramidalization decrease, in reason of the N -$\mathrm{H}-\mathrm{C}-\mathrm{H}$ ' torsion lowered to $3^{\circ}$. Two nbms now appear above and below the N atom, almost perpendicular to the H-N-C plane. Since the two nbms form, respectively, an $\alpha$ and an $\alpha^{\prime}$ angle of $84.8^{\circ}$ and $77.0^{\circ}$, they are not equivalent in placement. The enhanced double bond character of $\mathrm{C}-\mathrm{N}$ and the consequent decrease of such character for $\mathrm{C}=\mathrm{N}$ is directly suggested by the evident decrease of the $\alpha$ angle from 1 to $\mathbf{2}$. Then, once the 4 -membered cycle is formed on passing from 2 to 3 , the

N pyramidalization gets completely lost. The $\alpha$ and $\alpha^{\prime}$ angles turn to be almost equivalent and progressively lower along the series $\mathbf{2 - 4}$, conforming with the $\mathrm{C}-\mathrm{N}$ bond length monotonic decrease. In details, such angles further decrease to about $79.5^{\circ}$ as the DTC molecule is constrained to the crystal geometry and to about $76.3^{\circ}$ as in the crystal the DTC molecule is surrounded by other DTC molecules. Note once more how the $\alpha$ and $\alpha$ 'angle decrease mirrors the $\mathrm{C}-\mathrm{N}$ bond length diminishing, and its remarkable change upon crystallization and single/double CN bond length inversion. ${ }^{[43]}$ As previously stated, the N-S bond weakens from 2 to $\mathbf{3}$ because of the insertion of the 4-membered ring constraint, but then it systematically strengthens and decreases in length along the cyclic series, from $1.723 \AA$ in $\mathbf{3}$, to $1.701 \AA$ in 4 and further down to $1.654 \AA$ in the DTC crystal. Again, a possible interpretation of this evidence may be given in terms of resonance structures $c-e$ increasing their impact, which is validated (Figure 3), for the DTC system, by the progressive, large increase in the global negative charge of the oxygen atoms, namely from $2.427 e$ in the geometry optimized molecule up to $2.596 e$ in the crystal. Since charge separation does not necessarily imply bond lengthening for heteropolar bonds, also structures $g$ - $h$ may be significant players in this process. Inspection of trends in bond polarization and in delocalization indices and integrated Source Function non-local descriptors of the charge density, provide other interesting hints on the changes occurring in the $\mathrm{N} 1-\mathrm{C} 9=\mathrm{N} 2-\mathrm{S} 1$ conjugation pattern. They are all reported in appendix A1.

### 1.5 Crystal field effects

### 1.5.1 Crystal packing

Concerning solid DTC, we can not recognize noteworthy directional atom-atom intermolecular extended patterns because of the lacking of strong hydrogen bond (HB) donors in this system. Actually, close contacts involving the backbone thiazete atoms are discouraged due to the presence of cumbersome substituents. The most significant HB contact at $\mathrm{T}=100 \mathrm{~K}$ is C5-H5 $\cdots \mathrm{N} 2\left(d_{\mathrm{H} \cdots \mathrm{N}}=\right.$ $\left.2.54 \AA, \alpha_{\mathrm{C} 5-\mathrm{H} 5-\mathrm{N} 2} \approx 164 \mathrm{deg}\right)$., which involves a phenyl CH group and the N 2 nitrogen in the thiazete cycle. In general, phenyl C-H donors always trigger the most favourable interactions in terms of geometrical descriptors in this system. Interestingly, an acceptor for weak $\mathrm{CH} \cdots \pi$ interaction is also the localized $\pi$-system of the cyano group, whereas the methoxy oxygen O1 accepts a couple of very weak HB's from the dangling ethyl groups of a translationally-related
molecule. In contrast, atom N1 is excluded from any intermolecular HB, while, as expected, the sulphonyl oxygen atoms O 2 and O 3 can also act as weaker $\mathrm{CH} \cdots \mathrm{O}$ HB acceptors.

### 1.5.2 Thiazete geometry.

In the $\mathrm{N}-\mathrm{C}=\mathrm{N}$ system, the uncommon bond length alternation pattern manifests clearly within the DTC and TAYCUR crystal structures (Table 5), where the previously defined bond length difference parameter (BDP) is always negative. Considering individual structures, however, the low- $T$ DTC structure is the only one where the sign of BDP is statistically significant, with $\mathrm{BDP}=$ $-0.0181(7) \AA$, whereas it is poorly relevant, in terms of the corresponding estimated standard deviations (esd's), at room temperature ( $-0.009(4) \AA$ ). Generally, the comparison among the geometrical parameters reported in Tables 2 and 3 implies that remarkable structural changes on the bond lengths and angles within the thiazete cycle are due to crystal field. On the contrary, upon crystallization no important variations in the torsion angles occur. The main conformational adjustments involve the exocyclic substituents, especially the methoxy group orientation. The thiazete cycle is not rigidly distorted, as the minor and the major diagonals, $\mathrm{C} 9 \cdots \mathrm{~S} 1$ and $\mathrm{C} 8 \cdots \mathrm{~N} 2$, undergo a significant but asymmetric reduction in length [C9 $\cdots$ S1: from 2.2402 to $2.1942(6) \AA$; $\mathrm{C} 8 \cdots \mathrm{~N} 2$ : from $2.3219 \AA$ to $2.3021(9) \AA$ ] when comparing solid state and the optimized in vacuo outcomes. As a result, $d_{\mathrm{S} 1-\mathrm{N} 2}$ is decreased by $0.0474 \AA$ (MP2: $0.0473 \AA$ ), while, as previously stated, $d_{\text {S1-C8 }}$ shortens even by $0.0727 \AA$ upon crystallization. (Tables 2,5 ). On the contrary, the C9C 8 and the $\mathrm{C} 9=\mathrm{N} 2$ bonds, slightly lengthen by $\approx 0.01 \AA$. In the crystal, the sign inversion of the BDP parameter is due to the simultaneous $\mathrm{C} 9=\mathrm{N} 2$ bond length increase ( $\approx 0.016 \AA$ ) and the larger C9-N1 bond length decrease ( $\approx 0.019 \AA$ ).

| Bonds | DTC, 100(2) $\mathrm{K}^{1}$ | DTC, $\mathrm{RT}^{2}$ | $\mathrm{DTC}^{2} \mathrm{RT}^{3}$ |  | TAYCUR, RT |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| S1-N2 | $1.6539(4)$ | $1.6494(18)$ | $1.6421(19)$ | $1.6514(49)$ | $1.6478(69)$ |  |
| N2=C9 | $1.3325(5)$ | $1.3266(25)$ | $1.3308(27)$ | $1.3293(80)$ | $1.3286(85)$ |  |
| C9-N1 | $1.3144(5)$ | $1.3175(25)$ | $1.3074(24)$ | $1.3084(85)$ | $1.3087(109)$ |  |
| C9-C8 | $1.5343(5)$ | $1.5213(24)$ | $1.5317(29)$ | $1.5332(75)$ | $1.5344(109)$ |  |
| S1-C8 | $1.8959(6)$ | $1.8930(19)$ | $1.8777(20)$ | $1.8788(65)$ | $1.8649(57)$ |  |
| Angles |  |  |  |  |  |  |
| S1-N2-C9 | $93.92(3)$ | $94.3(1)$ | $93.8(1)$ | $94.0(4)$ | $93.9(5)$ |  |
| N2-C9-N1 | $126.52(3)$ | $126.6(2)$ | $127.0(2)$ | $126.6(5)$ | $126.3(6)$ |  |
| N2-C9-C8 | $106.68(3)$ | $106.5(2)$ | $106.1(2)$ | $106.1(4)$ | $105.7(5)$ |  |
| N2-S1-C8 | $80.58(2)$ | $80.36(8)$ | $80.93(9)$ | $80.7(2)$ | $80.9(3)$ |  |
| Torsions |  |  |  |  |  |  |
| S1-N2-C9-C8 | $-2.55(4)$ | $-2.5(2)$ | $-5.6(2)$ | $1.2(4)$ | $1.8(5)$ |  |
| S1-N2-C9-N1 | $177.27(4)$ | $177.0(2)$ | $177.0(2)$ | $-176.9(5)$ | $-176.7(7)$ |  |
|  |  |  |  |  |  |  |

Table 3: Experimental estimates for relevant bond length and angles ( $\AA$, deg) describing the thiazete ring in DTC and related compounds. See Figure 1 and Scheme 2 for the atom numbering. Esd's in parentheses.

It is worth stressing that the changes examined before remarkably decrease when electron correlation effects are studied at the MP2 theory level. For instance, at the MP2 level, the in vacuo estimate for BDP in 4, yet still positive, lowers from $+0.017 \AA$ to $+0.006 \AA$, while the large reduction of the S1-C8 distance upon change of phase decreases from 0.073 to just $0.020 \AA$. However, it shall be noted that both DFT and MP results predicted the same geometrical trends, providing a further validation that the detected crystal field effects are not fake products of model shortcomings.

### 1.5.3 Charge redistribution along the conjugated system

The $\nabla^{2} \rho(\mathbf{r})$ and $\varepsilon(\mathbf{r})$ profiles along the $\mathrm{N} 2-\mathrm{S} 1, \mathrm{C} 9=\mathrm{N} 2$ and $\mathrm{C} 9-\mathrm{N} 1$ bond paths for in vacuo and solid-state DTC are compared, respectively in Figures 4 and 5. Regarding the isolated molecule (compound 4), we reported results coming from both $\rho_{\mathrm{VQM}}$ and $\rho_{\mathrm{VQM} \text {-FROZEN }}$ (ED for in vacuo QM optimization and for in vacuo QM simulation at frozen geometry, respectively), whereas the condensed-phase curves refer to the experimental ED distribution, $\rho_{\mathrm{ExP}}$, for the molecule extracted from the crystal, the multipole-projected thoretical periodic ED distribution, $\rho_{\mathrm{MM}-\mathrm{PQM}}$, and the corresponding primary density $\rho_{\mathrm{PQM}}$ (ED from the solid state QM periodic wave function). The

[^4]$\nabla^{2} \rho(\mathbf{r})$ and $\varepsilon(\mathbf{r})$ profiles of the primary periodic density are compared with those from $\rho_{\mathrm{VQM}}$ and $\rho_{\text {VQM-Frozen }}$ densities in Figure 4., Figure 5 compares the experimental profiles and those obtained from the periodic calculation before and after the multipolar projection on the theoretical structure factors. Therefore, Figure 4 is useful to disentangle matrix effects from pure geometric effects caused by crystallization, while Figure 5 allows to evaluate the overall agreement between experiment and theory, and in particular the effect of the multipolar model bias. ${ }^{[14 b]}$ As expected, the $\rho(\mathbf{r})$ bcp invariably falls in the VSCC region of the less electronegative atom, i.e. S1 or C9 (plots on the right of Figures 4 and 5). Moreover, remarkable changes in terms of charge density distribution occur through the in vacuo-solid transition (Figure 4), which may be mostly due to the change of geometry.


Figure 4: Electron density Laplacian (left) and ellipticity (right) profiles along the N2-S1, C9-N2 and C9-N1 bond vectors in DTC, comparing theoretical in vacuo and solid-state electron density models. $d$ is the distance from the atom on the left and the indicated atomic locations. The position of the $\rho(\mathbf{r})$ bcp is marked by a coloured dot. Different colours refer to the electron density model employed to compute the $\nabla^{2} \rho(\mathbf{r})$ and $\varepsilon(\mathbf{r})$ profiles: (i) green: $\rho_{\mathrm{VQM}}$; (ii) purple: $\rho_{\mathrm{VQM}-\text { FROZEN }}$; (iii) red: $\rho_{\mathrm{PQM}}$.


Figure 5: Same as Figure 4, but comparing charge density models of DTC in the solid state. The colour-code is here defined as follows: (i) black: $\rho_{\text {EXP }}$; (ii) light blue: $\rho_{\mathrm{MM}-\mathrm{PQM}-; ~(i i i) ~ r e d: ~} \rho_{\mathrm{PQM}}$.

In detail:
(i) opposite variations with phase changes occur in the $\mathrm{C} 9-\mathrm{N} 1$ and $\mathrm{C} 9=\mathrm{N} 2$ bonds, the former slightly growing and the latter slightly reducing their shared character, as underlined by the respectively larger and smaller uniformity of their Laplacian distributions in the bonding regions;
(ii) the ellipticity of the $\mathrm{C} 9-\mathrm{N} 1$ bond is in the crystal somewhat less peaked near N 1 , since the nitrogen $p$-lone pair is more involved in the bond, as already shown by the decrease of $\alpha$ and $\alpha$ ' angles (Figure 3). For N2 just the opposite is true;
(iii) the $\mathrm{N} 2-\mathrm{S} 1$ bond has a less straightforward behaviour, as it is not simply triggered by the geometry change: in the crystal the ellipticity is larger and more uniform along the bonding region, while the bcp is remarkably further displaced towards the S atom. The roots of the changes described above for C-N and S-N bonds are clearly detectable. The reverse behaviour of C9-N1 and $\mathrm{C} 9=\mathrm{N} 2$ bonds conforms with the shortening of the former and lengthening of the latter and with the
large growth of the N 2 negative charge, from $-1.06 e$ in the in vacuo optimized geometry to $-1.21 e$ in the crystal (increased weight of resonance forms $b-d$ ). The $S$ atom largely increases its electronic charge as well, namely from $+2.67 e$ up to $+2.92 e$ upon shortening of the $\mathrm{S}-\mathrm{N}$ bond; the $\mathrm{S}-\mathrm{N}$ bcp further shifts itself towards the electropositive $S$ atom because of the bond largely enhanced polarity. The larger ellipticity for the S-N bond in the crystal suggests that the resonance forms $c-d$ become more and more relevant, as they conform with an increase of the negative charge on the oxygen atoms, along with the ( $e-h$ ) implying a larger positive charge on S . Actually, the oxygen atoms global negative charge notably increases in magnitude, in details from $2.43 e$ (in the in vacuo optimized geometry) to $2.60 e$ (in the crystal).

Two main conclusions may be drawn looking at the ED Laplacian profiles displayed in Figure 5. First, there is a remarkable agreement between theory and experiment concerning the description of the bonding features in the conjugated $\mathrm{C}-\mathrm{N}=\mathrm{C}-\mathrm{S}$ system, provided that structure factors are both projected on the multipole model. Second, a significant bias is introduced by this model, since the shape of profiles from $\rho_{\mathrm{MM}-\mathrm{PQM}}$ are definitely more alike to those from $\rho_{\mathrm{EXP}}$ than to those resulting from the primary density $\rho_{\mathrm{PQM}}$. Specifically, the trend retrieved in the multipole model is a decrease of the shared character of the bonds, leading to deeper ED Laplacian minima and higher ED Laplacian maxima in the bonding region.

### 1.5.4 Integrated source function

The experimental Source Function percentage contributions (SF\%) of the various atomic basins $\Omega$ in solid DTC for the N1-C9, C9=N2 and N2-S1 bcp's are graphically represented in Figure 6, while table 6 reports theoretical SF\% data for in vacuo and in-crystal DTC. As we can observe in Figure 6 , generally the thiazete substituents have a minor influence (individual $\mathrm{SF} \%$ being < $5 \%$ ) on the conjugated system features, except for the contributions of the two ethyl groups to the C9-N1 bcp, which are slightly higher than $5 \%$ because of their proximity to this bond and their well-known inductive ( +I ) effect ${ }^{[16]}$. A further confirmation of the increasing equalization of $\mathrm{N} 1-\mathrm{C} 9$ and $\mathrm{N} 2=\mathrm{C} 9$ bonds upon crystallization for $\rho_{\mathrm{VQM}}$ and $\rho_{\mathrm{PQM}}$ model densities can be deduced from the integrated SF results on the $\rho_{\mathrm{VQM}}$ and $\rho_{\mathrm{PQM}}$ densities (Table 6), as the $\mathrm{SF} \%_{\mathrm{C} 9+\mathrm{N} 2}$ value becomes slightly closer to $\mathrm{SF} \%_{\mathrm{C} 9+\mathrm{Nl} .}{ }^{[44]}$




Figure 6: Source Function percentage contributions (SF\%) to the charge density values at the $\mathrm{S} 1-\mathrm{N} 2, \mathrm{C} 9=\mathrm{N} 2$ and $\mathrm{C} 9-$ N1 bcp's in DTC, as computed from the in-crystal experimentally derived multipole model $\rho_{\text {Exp }}$. The position of each bcp is denoted by a black dot. Each atom $\Omega$ is displayed as a sphere whose volume is proportional to the $\mathrm{SF} \%$ contribution from $\Omega$ to the electron density at the indicated bcp. The colour of the sphere is blue if the $\mathrm{SF} \%$ contribution is positive and yellow if negative.

|  | Percentage Source Function values, $\mathrm{SF} \%$ ( $\Omega, \mathrm{bcp}$ ) |  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | C9-N1 |  |  | C9-N2 |  |  | S1-N22 |  |  |
|  | N 1 | C 9 | N 2 | N 2 | C 9 | N 1 | N 2 | S 1 | N 1 |
| $\rho_{\mathrm{VQM}}$ | 44.2 | 38.8 | 6.3 | 46.7 | 39.7 | 4.2 | 35.9 | 40.8 | 1.2 |
| $\rho_{\mathrm{VQM}-\mathrm{FRO}}$ | 44.7 | 38.9 | 5.8 | 46.4 | 39.3 | 4.4 | 35.6 | 39.9 | 1.2 |
| $\rho_{\mathrm{PQM}}$ | 44.5 | 39.1 | 5.6 | 46.1 | 39.3 | 4.5 | 35.8 | 39.2 | 1.2 |
| $\rho_{\mathrm{MM}-\mathrm{PQM}}$ | 44.8 | 39.7 | 4.5 | 47.2 | 39.3 | 3.6 | 42.1 | 34.6 | 1.2 |
| $\rho_{\mathrm{EXP}}$ | 45.0 | 39.3 | 5.0 | 47.8 | 39.1 | 3.8 | 43.7 | 34.3 | 1.3 |
|  |  |  |  |  |  |  |  |  |  |

Table 4: Values of integrated Source Function for the DTC molecule from various models. See Figure 1 and Scheme 2 in the main text for the atom numbering.

The decrease of the N 2 SF contribution at the C1-N9 bcp ED agrees with the negative charge enhancement at N 2 , while for N 1 the opposite occurs: upon crystallization, its contribution slightly raises at $\mathrm{C} 2=\mathrm{N} 9 \mathrm{bcp}$, complying with its improved ability to release its $\mathrm{p}-\pi$ electrons (see $\alpha, \alpha$, angles in Figure 3). Despite bond length values become more similar, the combination of the two effects mentioned above, which may be described through enhanced contributions from resonance structures $b-e$, does not increase electron delocalization in the $\mathrm{N}-\mathrm{C}=\mathrm{N}$ moiety. Upon crystallization, the SF\% contributions from $\mathrm{S} 1+\mathrm{N} 2$ atoms to their bcp density reduce ( -1.7 ) rather than augment, despite the S1-N2 becomes shorter. Basically, only the SF\% from S1 diminishes (-1.6), implying a stronger impact from those resonance structures featuring a positive $S$ atom and an increased positive charge on it and on O atoms (see Figure 3). Experimentally derived SF data are only qualitatively close to those resulting from the crystal periodic wavefunction and actually closer to those derived o by projecting the theoretical structure factors onto the multipolar model.

### 1.5.5 Dipole moment enhancemen.

In the previous pages we discussed atomic charges $q(\Omega)$, defined according to QTAIM and displayed in Figure 3. From them, we may provide a quantitative measure of the actual larger polarization, as a whole, of the DTC molecule in the crystal, by evaluating the molecular dipole moment $\boldsymbol{\mu}$. This quantity is strongly model-dependent ${ }^{[32 \text { f,i,j,k,l] }}$ and it is notoriously quite difficult to be accurately determined. By using QTAIM, molecular boundaries are naturally defined also in the crystal, through the zero-flux surfaces of the composing atoms. ${ }^{[9,15 b]}$ Hence, it is possible to gain an accurate evaluation of $\boldsymbol{\mu}$ in the condensed phase, using a method equally applicable to the in vacuo estimate. ${ }^{[9,15 a, 15 b]}$ Comparing this latter value with the (formally equivalent) value one obtains from the usual procedure implemented in the quantum chemical codes, like Gaussian-09, provides a check on the numerical accuracy of the QTAIM estimate. ${ }^{[15 b]}$ Discrepancies between the modules of the two values, due to numerical errors in the QTAIM basin integration, were found to be lower than $0.1 \%$ for all systems 1-4. The total molecular dipole $\boldsymbol{\mu}$ has then been partitioned into a first moment contribution, $\mu_{\mathrm{A}}$, representing the atomic polarization term due to the atomic first moments plus a charge transfer (CT) component $\mu_{\mathrm{CT}}$ developing from the net atomic charges (see section 1 and Ref [45]). Since both composing terms are not origin-dependent for a neutral system, they thus maintain a physical meaning by themselves. ${ }^{[15]}$ Total dipole moment module $|\boldsymbol{\mu}|$ values are listed in Table 7, together with their components $\left|\mu_{\mathrm{A}}\right|$ and $\left|\mu_{\mathrm{CT}}\right|$, for DTC in vacuo (optimized geometry and crystal frozen geometry), in-crystal, and from experiment. The two vectors are almost
collinear, but as expected, oppositely directed, ${ }^{\mathrm{a}}$ as denoted by the angle $\gamma$ between $\mu_{\mathrm{A}}$ and $\mu_{\mathrm{CT}}$, reported in Table 5 as well. Values for systems 1-3 are also reported, in order to provide exhaustive data. ${ }^{[46]}$

| System, density | $\|\boldsymbol{\mu}\|$ | $\left\|\boldsymbol{\mu}_{\mathrm{A}}\right\|$ | $\left\|\boldsymbol{\mu}_{\mathrm{CT}}\right\|$ | $\boldsymbol{\gamma}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}, \rho_{\mathrm{VQM}}$ | 3.5 | 1.8 | 4.2 | 122.1 |
| $\mathbf{2}, \rho_{\mathrm{VQM}}$ | 6.1 | 3.3 | 8.6 | 146.2 |
| $\mathbf{3}, \rho_{\mathrm{VQM}}$ | 8.1 | 4.1 | 12.1 | 166.5 |
| $\mathbf{4}, \rho_{\mathrm{VQM}}$ | 9.6 | 5.8 | 15.2 | 167.4 |
| $\mathbf{4}, \rho_{\mathrm{VQM}-\mathrm{FROZEN}}$ | 9.7 | 5.1 | 14.7 | 167.7 |
| 4, $\rho_{\mathrm{PQM}}$ | 13.0 | 5.0 | 17.8 | 163.1 |
| $\mathbf{4 ,} \rho_{\mathrm{EXP}}$ | $15.4(1.5)$ | 5.7 | 20.3 | 153.6 |

Table 5: Values (Debye) of the molecular total dipole moment module, $|\underline{\mu}|$, and of its charge transfer, $\left|\underline{\mu}_{\mathrm{CT}}\right|$, and atomic polarization, $\left|\underline{\mu}_{\mathrm{A}}\right|$, components for the molecules 1-4, from various theoretical models and experiment. The angle $\gamma$ between $\mu_{\mathrm{A}}$ and $\underline{\mu}_{\mathrm{CT}}$ is also reported.

A remarkable result is surely the agreement - within almost one experimental esd - between the theoretical evaluation for the DTC molecular dipole module in the bulk and the analogue multipolederived evaluation from X-ray diffraction data. However, the neat enhancement of the DTC molecular dipole module, on passing from the in vacuo optimized geometry to the crystal (from 9.6 to 13.0 D , see Table 5), is to be considered the most important result. The observed $35 \%$ enhancement nicely parallels that found, theoretically, for the urea crystal ${ }^{[15 b]}(+37 \%)$. As the only geometrical change due to crystallization bears a negligible increase (from 9.6 to 9.7 Debye), such large enhancement is to be ascribed to the matrix effect of the crystal, resulting from the interplay between two cooperating effects. First, an augmentation of the CT component (from 15.2 to 17.8 Debye), due to the discussed general increase of the atomic charges magnitudes in the thiazete ring and in the sulphonyl groups. Then, the packing constraints caused by crystallization lead to a reduction in the magnitude of the atomic polarization (from 5.8 down to 5.0 Debye), as already retrieved in other systems. ${ }^{[15 a, 15 c, 48]}$ Since the $\mu_{\mathrm{A}}$ and $\mu_{\mathrm{CT}}$ vectors in DTC (4) are almost antiparallel ( $\gamma>160^{\circ}$ ), the two effects concur in enhancing the molcular dipole moment upon crystallization. The enhancement is, however, mostly ( $76 \%$ ) provided by the CT component, and so by the increased charge separation of bonded atoms in the bulk, implying that crystallization of DTC is driven by electrostatics. The resonance forms of the DTC molecule leading to an increase of charge separation, hence to an increase of the electrostatic energy gain produced by molecules interacting among each other, turn out to be largely energy-stabilized upon crystallization. Moreover, the increase of their influence, induce large geometrical distortions to occur, so that the single $\mathrm{N}-\mathrm{C}$ bond turns out to be shorter than the formally double $\mathrm{N}=\mathrm{C}$ bond in the crystal.

[^5]

Figure 7: Molecular dipole vector modulus $v s$. the bond difference parameter, $\mathrm{BDP}=d_{\mathrm{C9}-\mathrm{N} 1}-d_{\mathrm{C} 9=\mathrm{N} 2}$, through the compound series 1-4 in Scheme 2, plus the values computed from the $\rho_{\exp }$ (blue rhombus) and $\rho_{\mathrm{PQM}}$ (yellow triangle) models. Units are Debye and $\AA$ and the reported entries come from the QTAIM partitioning of the corresponding charge density distributions. The esd for the $\rho_{\text {exp }}$ dipole moment is also shown. The two linear least-squares fittings displayed in the Figure differ in the last point: the blue curve includes the $\rho_{\exp }$ model and has equation $|\boldsymbol{\mu}|=6.8(9) \cdot(10 \cdot \mathrm{BDP})^{2}-$ $1.57(9) \cdot 10^{2} \cdot \mathrm{BDP}+12.5(2)$, with correlation coefficient $\mathrm{R}^{2}=0.997$, while the yellow curve includes the $\rho_{\mathrm{PQM}}$ model and has equation $|\boldsymbol{\mu}|=2.8(7) \cdot(10 \cdot \mathrm{BDP})^{2}-1.02(9) \cdot 10^{2} \cdot \mathrm{BDP}+11.1(2)$ with $\mathrm{R}^{2}=0.997$. Inset: mutual orientation and moduli of molecular dipole moments of gas-phase optimized compounds $\mathbf{3}$ and $\mathbf{4}$, plus the solid-state $\rho_{\exp }$.

Despite the change of geometry (see above) seems to be the only factor influencing most of the bonding properties in the DTC crystal, the molecular dipole moment module enhancement clearly shows a different behaviour. In fact, shortening of N1-C9 and lengthening of N2=C9 bonds only occur when an enhancement of the molecular dipole moment module can stabilize the DTC molecule. In other words, bond length inversion turn out to be manifest in a real system only in the bulk, where such a change is exploited because it becomes, there, energetically convenient.
Table 5 and Figure 7 show that in the series of compounds 1-4 a systematic increase of the total molecular dipole moment module occurs, and a fairly well inverse quadratic correlation is evident between its module and the bond difference parameter $\mathrm{BDP}=d_{\mathrm{C} 9-\mathrm{N} 1}-d_{\mathrm{C} 9=\mathrm{N} 2}$ (Figure 7). Note also that the total dipole moment has always a very similar orientation with respect to the thiazete ring (Figure 7, inset). Therefore, the increment of the $\mu$ vector modulus is likely the main cause of all the $\rho(\mathbf{r})$ rearrangements previously commented, or viceversa, those $\rho(\mathbf{r})$ rearrangements dictate the observed dipole moment enhancement.

### 1.6 Conclusions

This chapter is focused on 3-diethylamino-4-(4-methoxyphenyl)-1,1-dioxo-4H-1 $\lambda^{6}, 2$-thiazete-4-carbonitrile (DTC), a synthetic compound whose core chemical moiety is an uncommon 4membered thiazete-1,1-dioxide heterocycle showing significant similarity with $\beta$-sultamic drugs. Crystallographic investigations carried out at room temperature on DTC polymorphs revealed that in the conjugated $-\mathrm{N}-\mathrm{C}=\mathrm{N}-\mathrm{SO}_{2}{ }^{-}$system the formally single $\mathrm{N}-\mathrm{C}$ bond is, on average, $0.018 \AA$ shorter than the formally double $\mathrm{N}=\mathrm{C}$ bond. To clarify the subtle interplay between structure, electron delocalization and crystal field polarization effects, we investigated the charge density distribution of DTC either by single-crystal X-ray diffraction at $T=100(2) \mathrm{K}$ and quantum mechanical simulations. We employed to this purpose both local and non-local topological descriptors provided by the Quantum Theory of Atoms in Molecules, relating topological and structural changes of crystalline and in vacuo DTC to the smaller or larger importance of resonance forms in the $-\mathrm{N}-\mathrm{C}=\mathrm{N}-\mathrm{SO}_{2}-$ moiety. As a result, we provided a rationale for the aforementioned C $\mathrm{N} / \mathrm{C}=\mathrm{N}$ bond length inversion: the large DTC dipole moment enhancement occurring in the crystal stabilizes highly polar resonant forms so as to exploit more convenient electrostatic interactions with neighbouring molecules. As a consequence, a significant electronic rearrangement occurs within the molecule, resulting in an unusual and counterintuitive bond length alternation pattern. Such findings also lead to further possible implications we discussed in this chapter, aiming at an accurate in silico modelling of crystal structures. From the results obtained it is possible to draw the following conclusions:
(i) the $\mathrm{C}-\mathrm{N} / \mathrm{C}=\mathrm{N}$ bond length inversion in the solid state of DTC with respect the DTC structure in vacuo, is due to a significant ( $\approx+35 \%$ ) in-crystal DTC dipole moment enhancement that has its roots in a concomitant growth of the charge transfer, along with a decrease in the magnitude of the atomic polarization term. In particular such dipole enhancement derives at most (76\%) from the charge transfer component, hence from the augmented charge separation of bonded atoms in the bulk. As a consequence, upon crystallization the highly polar resonant forms in Scheme 3 ( $c-e$ and $g-h)$ are stabilized and the increase of their weight significantly influences the molecular geometry. The electrostatic contribution to the total cohesive energy of DTC represents the ultimate leading force of this process. As this system lacks strong directional hydrogen bond networks, higher first and second electrostatic moment magnitudes need to be explored to achieve more favourable electrostatic interactions with neighbouring molecules. .
(ii) The bias introduced by the multipolar model may lead to wrong conclusions when subtle changes are discussed, and ones where delocalization effects are mainly intertwined with the
polarization effects caused by the crystal matrix. In these cases, correct conclusions can be safely achieved only if the changes are assessed through comparable approaches, like the examination of theoretical and experimental structural EDs, both filtered through the same multipolar model expansion. ${ }^{[48]}$
(iii) As it is well known, the interplay between the molecular and the crystal structure determines essential bulk features in a material, among which second-harmonic generation, pyroelectricity and piezoelectricity. Despite none of these properties can be exploited by DTC itself because of its centrosymmetric space group, it emerges as an interesting test case to shed light on how crystallization may produce changes in the molecular structure, that in turn define the crystal field itself. Since these changes are essentially quantum-mechanical in nature, the suitability of methods intrinsically neglecting quantum effects in accurately displaying the crystalline matrix effects and/or predicting crystal structures are questioned. This is the case, for instance, of those based on force fields methods.

The joint theoretical and experimental approach employed in this study overcomes such limitations, as it detects and rationalizes also subtle and counterintuitive effects. However, we cannot ignore its lack of predictability. Aiming at a further improvement of the computational recipes for in silico modelling of crystalline materials in terms of accuracy and reliability, we sense that the knowledge of accurate single-crystal X-ray structures and experimentally-derived charge densities will be more and more relevant in the next future, providing precious hints as well as paradigmatic cases to be interpreted.

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[48] Volkov, A.; Abramov, Y.; Coppens, P.; Gatti, C. Acta Crystallogr. 2000, A56, 332-339.

## CHAPTER 2

## SOURCE FUNCTION FOR THE ELECTRON SPIN DENSITY: <br> DEVELOPEMENT AND APPLICATION OF A NEW QTAIM BASED CHEMICAL DESCRIPTOR

### 2.1 Introduction:

## On the electron spin density distribution:

Electron spin density distribution is a physical observable that can be obtained experimentally through magnetic scattering of polarized X-rays and neutrons diffraction techniques ${ }^{[1,2]}$. In a couple of very recent works, M. Deutsch et al. have performed a joint refinement of X-ray and polarized neutron diffraction data using a split-spin version of the well-known Hansen \& Coppens $\varphi \rho^{[3]}$, leading to accessible much improved experimental $s(\mathbf{r})$ and to first spin-resolved electron density distributions $\rho(\mathbf{r})_{\mathrm{s}}^{[44,5]}$. It is clear that with the increased availability of large scale facilities providing intense neutron and synchrotron X-ray sources, such kind of extended model will provide a very valuable tool to understand and predict specific magnetic interactions in complex solid-state networks ${ }^{[4,5,6]}$. However, it is neither possible to obtain direct information on the fundamental factors causing spin polarization effects nor to distinguish the very subtle exchange/pairing mechanisms using the $s(\mathbf{r})$ scalar field alone. In general $s(\mathbf{r})$ can be also obtained from quantum mechanics and do exist a lot of interpretive models, generally rooted in the atomic or molecular orbitals framework, that are used for the purpose of analyze such scalar field. In this thesis, a novel QTAIM based chemical descriptor is introduced, the Source Function for the spin density ( $\mathrm{SF}_{\mathrm{S}}$ ). This descriptor is able to gain, in terms of a cause-effect relationship, quantitative insights on the relative capability of different atoms or groups of atoms in a system to determine the spin density at any point within a given molecular system. In this sense, since $s(\mathbf{r})$ is directly connected to magnetic phenomena in complex systems, a very powerful method to distinguish different spin polarization mechanisms ${ }^{\mathrm{b}}$, often in competition to each other, is provided. Magnetism depends on non-local effects and can be exploited through space or through chemical bonds. Magnetic properties will thus depend on how the spin information is propagated from a given paramagnetic centre to its neighbouring atoms. It will be shown in the next subsections that the $\mathrm{SF}_{\mathrm{s}}$ is a tool able to reconstruct $\mathrm{s}(\mathbf{r})$ at any point in terms of atomic contributions, so giving a very clear picture of how the magnetic centre is "magnetically" connected to the ligands within a molecule and of how these ligands may in turn, to various extent and in various ways, influence the magnetic center itself.

[^6]
### 2.2 Source Function for electron density:

Back in 1998, R. F. W. Bader and C. Gatti showed that the electron density at a point $\mathbf{r}$ in space may be seen as caused by a local source LS and by its operation at all other points of the space ${ }^{[7]}$, (Eq. 2). The LS is given, Eq. 1, by

$$
L S\left(\mathbf{r}, \mathbf{r}^{\prime}\right)=-\frac{1}{4 \pi} \frac{\nabla^{2} \rho\left(\mathbf{r}^{\prime}\right)}{\left|\mathbf{r}-\mathbf{r}^{\prime}\right|}
$$

In this expression $-\left(4 \pi\left|\mathbf{r}-\mathbf{r}^{\prime}\right|\right)^{-1}$ is a Green's function or an influence function and represents how effective is the cause, the Laplacian of the density $\left(\nabla^{2} \rho\left(\mathbf{r}^{\prime}\right)\right)$ at $\mathbf{r}^{\prime}$ multiplied by the volume element at $\mathbf{r}^{\prime}$, in determining the effect, the electron density at $\mathbf{r},(\rho(\mathbf{r}))$. Then if we replace the integration of the LS over the whole space with separate integrations over the disjoint and exaustive partitioning of $\mathbf{R}^{3}$ offered by the basins defined through the zero-flux recipe of the QTAIM ${ }^{[8]}$, the density at $\mathbf{r}$ may be seen, Eq. 2, as determined by a sum of atomic contributions $S(\mathbf{r} ; \Omega)$, each of which is termed as the source function (SF) from the atom $\Omega$ to $\rho(\mathbf{r})$.

$$
\rho(\mathbf{r})=\int_{R^{3}} L S\left(\mathbf{r}, \mathbf{r}^{\prime}\right) d r^{\prime}=\sum_{\Omega} \int_{\Omega} L S\left(\mathbf{r}, \mathbf{r}^{\prime}\right) d \mathbf{r}^{\prime}=\sum_{\Omega} S F(\mathbf{r}, \Omega) \text { eq. } 2
$$

Eq. 1 and 2 are expressions that clearly remind that for the electrostatic potential at $\mathbf{r}, \mathrm{V}_{\text {elec }}(\mathbf{r})$.

$$
V_{e l e c}=\int \frac{\rho\left(\mathbf{r}^{\prime}\right)}{\left|\mathbf{r}-\mathbf{r}^{\prime}\right|} d r^{\prime} \quad \text { eq. } 3 \mathrm{a}
$$

Indeed both $\rho(\mathbf{r})$ and $V_{\text {elec }}(\mathbf{r})$ are a solution of the Poisson's equation $\nabla^{2} \varphi(\mathbf{r})=-q(\mathbf{r})$

$$
\varphi(\mathbf{r})=\int \frac{q\left(\mathbf{r}^{\prime}\right)}{4 \pi\left|\mathbf{r}-\mathbf{r}^{\prime}\right|} d \mathbf{r}^{\prime} \quad \text { eq. } 3 \mathrm{~b}
$$

with $\varphi$ being $\rho(\mathbf{r})$ or $\mathrm{V}_{\text {elec }}(\mathbf{r})$, q being, respectively, $\rho(\mathbf{r})$ or $\nabla^{2} \rho(\mathbf{r})$, and exploiting the definition of $\mathrm{V}_{\text {elec }}$ in terms of the Poisson's equation $\nabla^{2} \mathrm{~V}_{\text {elec }}(\mathbf{r})=4 \pi \cdot \rho(\mathbf{r})$.

Eq. 2 give us an expression which relates $\rho(\mathbf{r})$ at a point to the behaviour of this scalar (in terms of $\left.\nabla^{2} \rho\left(\mathbf{r}^{\prime}\right)\right)$ in the other points of the space. Decomposition of $\rho(\mathbf{r})$ in terms of SF atomic contributions enables one to view the properties of the electron density (ED) distribution from a new perspective.

It shows that $\rho(\mathbf{r})$ is never really local in nature but originates from the cumulative result of the influence of all other parts of the system. This is in agreement with the Density Functional Theory where the ED at a point is known to be a unique functional of the external potential, defined by the positions and nuclear charge of all nuclei in the system. However, through the SF, such non local dependence of the ED is examined using the lenses of chemistry, i.e. in terms of contributions from well defined chemical entities, like atoms or group of atoms within the system. For instance, the SF decomposition may provide a chemically meaningful picture of how a system responds to a perturbation, like chemical substitution, change of environment, by observing the changes on $\rho$ (or on a given property of $\rho$ ) and the atomic contribution to such changes at any point $\mathbf{r}$. Precious insights on the impact of perturbation on the various parts of a system are provided this way. Finally the SF chemical descriptor is amenable to experimental determination, since, as discussed in Chapter 1, the ED and its Laplacian may be also obtained from experimental structure factors measured through very accurate single crystal X-ray diffraction experiments ${ }^{[10-14,17-18]}$. This is certainly one of the most attractive properties of the SF descriptor, enabling a direct comparison between theory and experiment. ${ }^{[10]}$

### 2.3 Source Function for electron spin density:

### 2.3.1 Theory:

The Source Function for the electron spin density $\left(\mathrm{SF}_{\mathrm{s}}\right)$ is obtained through an expression formally similar to that for the electron density ${ }^{[26]}$.

$$
s(\mathbf{r})=\int_{R^{3}} L S_{S}\left(\mathbf{r}, \mathbf{r}^{\prime}\right) d \mathbf{r}^{\prime}=\sum_{\Omega} \int_{\Omega} L S_{S}\left(\mathbf{r}, \mathbf{r}^{\prime}\right) d \mathbf{r}^{\prime}=\sum_{\Omega} S F_{s}(\mathbf{r}, \Omega) \text { eq. } 4
$$

In eq.4, however, the decomposition in atomic terms is still done in terms of $\rho(\mathbf{r})$ and not of $s(\mathbf{r})$. Thus the Laplacian of the spin density $\left(\nabla^{2} \mathrm{~s}(\mathbf{r})\right)$ does not integrate to zero in the atomic basins as it is for the ED Laplacian, because the atomic surface has a net flux of the electron spin density gradient through the surface. The local source and cause for $\mathrm{s}(\mathbf{r})$ at $\mathbf{r}\left(\mathrm{LS}_{\mathrm{s}}\right)$ is given by

$$
L S_{s}=-\frac{1}{4 \pi} \frac{\nabla^{2} s\left(\mathbf{r}^{\prime}\right)}{\left|\mathbf{r}-\mathbf{r}^{\prime}\right|}=-\frac{\nabla^{2} s\left(\mathbf{r}^{\prime}\right)}{4 \pi\left|\mathbf{r}-\mathbf{r}^{\prime}\right|}=-\frac{\nabla^{2} \boldsymbol{\rho}_{\alpha}\left(\mathbf{r}^{\prime}\right)-\nabla^{2} \boldsymbol{\rho}_{\beta}\left(\mathbf{r}^{\prime}\right)}{4 \pi\left|\mathbf{r}-\mathbf{r}^{\prime}\right|} \text { eq. } 5
$$

in terms of $\nabla^{2} s(\mathbf{r})$ rather then $\nabla^{2} \rho(\mathbf{r})$; the global effect is $\mathrm{s}(\mathbf{r})$ while the effectiveness of the local cause just remains the same as for electron density because it is a purely geometrical factor that
include the reciprocal of the distance between the $\mathbf{r}$ (reference point) and $\mathbf{r}^{\prime}$ (the local point). Since $\nabla^{2} s(\mathbf{r})$ is different with respect to $\nabla^{2} \rho(\mathbf{r})$, information on $\rho(\mathbf{r})$ transmission is different from the information on $\mathrm{s}(\mathbf{r})$ transmission. The reconstruction for the $\mathrm{s}(\mathbf{r})$ has a similar formal expression and $\mathrm{SF}_{\mathrm{s}}$ denote the source function from atom $\Omega$ to $\mathrm{s}(\mathbf{r})$. To clarify the differences between information on $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ transmission, the comparison between the various quantities entering in the definition of the source function for the electron density and spin electron density is necessary.

### 2.3.2 Comparison between the electron density and spin electron density behaviour:

Electron density and electron spin density distribution are defined respectively by

$$
\begin{aligned}
\rho(\mathbf{r}) & =\rho_{\alpha}(\mathbf{r})+\rho_{\beta}(\mathbf{r}) \\
\mathrm{s}(\mathbf{r}) & =\rho_{\alpha}(\mathbf{r})-\rho_{\beta}(\mathbf{r})
\end{aligned}
$$

with $\rho_{\alpha}(\mathbf{r})$ and $\rho_{\beta}(\mathbf{r})$ being the spin $\alpha$ and $\beta$ contributions to the total ED density. These two scalar fields present very different behaviour and properties. First of all the analysis of $\rho(\mathbf{r})$ is simpler with respect to $s(\mathbf{r})$ because $\left(\operatorname{LS}\left(\mathbf{r}^{\prime}\right)\right)$ will be always positive where $\nabla^{2} \rho\left(\mathbf{r}^{\prime}\right)$ is negative ( $\rho\left(\mathbf{r}^{\prime}\right)$ concentrated) and viceversa (see Tab.1).

| $\rho\left(\mathbf{r}^{\prime}\right)$ | $\nabla^{2} \rho\left(\mathbf{r}^{\prime}\right)$ | $\mathrm{LS}\left(\mathbf{r}^{\prime}\right)$ | Effect on $\rho(\mathbf{r})$ |
| :---: | :---: | :---: | :---: |
| $>0$ | $>0$ | $<0$ | decreases $\rho$ |
| $>0$ | $<0$ | $>0$ | increases $\rho$ |

Tab.1: Behaviour of electron density distribution as a function of the sign of the Local Source Function

The situation becomes more complicate and interesting when we analyse the electron spin density field. Regardless of the sign of $s(\mathbf{r})$, the local source behaviour depends on the local concentration/dilution of $\rho_{\alpha}\left(\mathbf{r}^{\prime}\right)$ and $\rho_{\beta}\left(\mathbf{r}^{\prime}\right)$. If $\rho_{\alpha}\left(\mathbf{r}^{\prime}\right)$ is locally diluted ( $\nabla^{2} \rho_{\alpha}\left(\mathbf{r}^{\prime}\right)$ positive) and $\rho_{\beta}\left(\mathbf{r}^{\prime}\right)$ is instead locally concentrated ( $\nabla^{2} \rho_{\beta}\left(\mathbf{r}^{\prime}\right)$ negative) then $\nabla^{2} s\left(\mathbf{r}^{\prime}\right)$ will be positive (see the $2^{\text {nd }}$ row of the Tab.2); the local source will be negative and the infinitesimal region around this point will cause the effect of decreasing $s(\mathbf{r})$ (denoted as " $\beta$ " effect in the last column), making the spin density less positive or more negative with respect to the effect caused by the sum of contributions from the remaining regions of the system. On the contrary if at $\mathbf{r}^{\prime}$ the $\alpha$ distribution is locally concentrated and the $\beta$ distribution is locally depleted (third row of Tab. 2) there will be an increase of $s(\mathbf{r})$ (denoted as " $\alpha$ " effect in the last column). When $\rho_{\alpha}\left(\mathbf{r}\right.$ ') and $\rho_{\beta}(\mathbf{r}$ ") are both diluted or both
concentrated, the sign of the local source will depend on the relative magnitude of $\nabla^{2} \rho_{\alpha}\left(\mathbf{r}^{\prime}\right)$ and $\nabla^{2} \rho_{\beta}\left(\mathbf{r}^{\prime}\right)$.

| $s\left(\mathbf{r}^{\prime}\right)$ | $\nabla^{2} \rho_{\alpha}\left(\mathbf{r}^{\prime}\right)$ | $\nabla^{2} \rho_{\beta}\left(\mathbf{r}^{\prime}\right)$ | Relative magnitude | $\nabla^{2} s\left(\mathbf{r}^{\prime}\right)$ | $\operatorname{LS}_{s}\left(\mathbf{r}^{\prime}\right)$ | Effect on $s(\mathbf{r})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\pm$ | $>0$ | $>0$ | $\begin{aligned} & \nabla^{2} \rho_{\alpha}>\nabla^{2} \rho_{\beta} \\ & \nabla^{2} \rho_{\alpha}<\nabla^{2} \rho_{\beta} \end{aligned}$ | $\begin{aligned} & >0 \\ & <0 \end{aligned}$ | $\begin{aligned} & <0 \\ & >0 \end{aligned}$ | $\begin{aligned} & \longrightarrow \beta \\ & \longrightarrow \alpha \end{aligned}$ |
| $\pm$ | $>0$ | $<0$ |  | $>0$ | $<0$ | $\longrightarrow \beta$ |
| $\pm$ | $<0$ | $>0$ |  | $<0$ | $>0$ | $\longrightarrow \alpha$ |
| $\pm$ | $<0$ | $<0$ | $\begin{aligned} & \left\|\nabla^{2} \rho_{\alpha}\right\|>\left\|\nabla^{2} \rho_{\beta}\right\| \\ & \left\|\nabla^{2} \rho_{\alpha}\right\|<\left\|\nabla^{2} \rho_{\beta}\right\| \end{aligned}$ | $\begin{aligned} & <0 \\ & >0 \end{aligned}$ | $\begin{aligned} & >0 \\ & <0 \end{aligned}$ | $\begin{aligned} & \longrightarrow \alpha \\ & \longrightarrow \beta \end{aligned}$ |

Tab.2: Behaviour of electron density spin distribution as function of the sign of the Local Source Function

For example, the first row of Tab. 2 reports the situation where both $\rho_{\alpha}\left(\mathbf{r}^{\prime}\right)$ and $\rho_{\beta}\left(\mathbf{r}^{\prime}\right)$ are diluted; in this case $\mathrm{LS}_{\mathrm{s}}\left(\mathbf{r}\right.$ ') will be negative and will generate a " $\beta$ " contribution only if $\rho_{\alpha}(\mathbf{r}$ ') is more diluted than $\rho_{\beta}\left(\mathbf{r}^{\prime}\right)$, while it will be p0ositive if $\rho_{\beta}\left(\mathbf{r}^{\prime}\right)$ is more diluted with respect $\rho_{\alpha}\left(\mathbf{r}^{\prime}\right)$. On the contrary, in case they are both concentrated there will be an $\alpha$ effect if $\rho_{\alpha}\left(\mathbf{r}^{\prime}\right)$ is more concentrated than $\rho_{\beta}\left(\mathbf{r}^{\prime}\right)$; while if it is $\rho_{\beta}\left(\mathbf{r}^{\prime}\right)$ that is more concentrated, its Laplacian will be more negative than that of the $\alpha$ distribution and the local source will be negative causing an effect " $\beta$ ". Is very important to stress that, differently from $\rho(\mathbf{r})$, it is no longer sufficient to have the $\alpha$ and $\beta$ density distributions both concentrated to have a positive source or both diluted to have a negative source. One may obtain a positive or a negative source in both cases. Everything depend on the relative magnitude of concentration or dilution of the $\alpha$ or $\beta$ distributions. Let's see an application of what reported in Tab. 1 and 2 on a very simple system, water triplet. Using a simple orbital model, the molecular system is hybridized $\mathrm{sp}^{2}$ and presents two unpaired electrons in the $\mathrm{p}_{\mathrm{x}}$ orbital perpendicular to the molecular plane (see Figure 1) ${ }^{\text {c }}$.

[^7]

Fig.1: water Triplet ${ }^{3} \mathrm{~B}_{1} ; \nabla^{2} \rho(\mathbf{r})$ and $\rho(\mathbf{r})$ critical points are reported. The $\nabla^{2} \rho(\mathbf{r})$ critical points are denoted as follows: green points $(3,+3)$ charge concentration, red points denote $(3,-1)$ saddle points and violet point denote $(3,+1)$ saddle point. The bond critical point is reported in black

| CP | $\rho(\mathbf{r})$ | $\nabla^{2} \rho(\mathbf{r})$ | $\mathrm{s}(\mathbf{r})$ | $\nabla^{2} \mathrm{~s}(\mathbf{r})$ | $\rho_{\alpha}(\mathbf{r})$ | $\nabla^{2} \rho_{\alpha}(\mathbf{r})$ | $\rho_{\beta}(\mathbf{r})$ | $\nabla^{2} \rho_{\beta}(\mathbf{r})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.288 | -2.14 | -0.0050 | 0.21 | 0.141 | -0.96 | 0.146 | -1.18 |
| 2 | 0.888 | -5.17 | 0.0631 | 1.07 | 0.475 | -2.05 | 0.412 | -3.12 |
| 3 | 1.03 | -6.85 | 0.0051 | 2.04 | 0.518 | -2.4 | 0.513 | -4.45 |
| 4 | 0.61 | -1.18 | 0.3818 | -4.54 | 0.496 | -2.86 | 0.114 | 1.68 |

Tab.3: Values of electron density, electron spin density, Laplacian of total $\rho(\mathbf{r})$ and in terms of its $\alpha$ and $\beta$ counterparts, Laplacian of spin density distribution, at each critical point considered in Fig. 1

Let's consider $\nabla^{2} s(\mathbf{r})$ and the $L_{s}$ at a number of critical points (CP) in $\nabla^{2} \rho(\mathbf{r})$ or in $\rho(\mathbf{r})$. At the bond critical point lying on O-H bond (bcp point 1 coloured in black in Fig.1) s(r) is negative, and both the $\alpha$ and $\beta$ distributions are concentrated $\left(\nabla^{2} \rho_{\alpha}(\mathbf{r})\right.$ and $\left.\nabla^{2} \rho_{\beta}(\mathbf{r})<0\right)$. Since $\nabla^{2} \rho_{\beta}(\mathbf{r})$ is more negative then its $\alpha$ counterpart we observe a positive $\nabla^{2} s(\mathbf{r})$ at the bcp. The infinitesimal region around this critical point will generate a " $\beta$ " transmission effect. At the bond charge concentration (BCC, point 2, coloured in green in Fig.1) s(r) is positive, differently from the bcp 1. Also in this case both $\rho_{\alpha}(\mathbf{r})$ and $\rho_{\beta}(\mathbf{r})$ are concentrated and $\nabla^{2} \rho_{\beta}(\mathbf{r})$ is more negative then $\nabla^{2} \rho_{\alpha}(\mathbf{r})$. So again $\nabla^{2} s(\mathbf{r})>0$ and also this region will have a negative local source generating a beta transmission
effect, regardless that the sign of the spin density was positive in this case. There are three critical points related to the non bonded charge concentrations within the molecular system: the $(3,+3)$ charge concentration corresponding to the lone pair lying in the molecular plane and associated to a $\mathrm{sp}^{2}$ orbital (CC, point 3, coloured in green in Fig.1) and two (3,-1) critical points associated to the unpaired electrons in the $p_{z}$ orbital (points $\mathbf{4}$ and $\mathbf{4}^{\prime}$ coloured in red in Fig.1) that are very close to the spin density maximum in this plane. Both kind of critical points have positive spin density but differ a lot in their behaviour. In fact at the lone pair charge concentration $\mathbf{3}, \mathrm{s}(\mathbf{r})$ is marginally positive and the Laplacian of the $\beta$ distribution is much more negative than the Laplacian of the $\alpha$ distribution as a reaction to the large concentration of the neighbouring unpaired electrons (this assertion is supported by the fact that $s(\mathbf{r})$ is close to become negative near CP 3). Hence $\nabla^{2} s(\mathbf{r})$ is greater then zero and the region around the lone pair CC will cause a $\beta$ effect. If we look at the out of plane ( $3,-1$ ) CPs $\mathbf{4}$ and $\mathbf{4}^{\prime}$, we find a completely different behaviour. In fact at this CP the spin density is very large, dominated by the $\alpha$ unpaired electron and, more important, while $\rho_{\alpha}(\mathbf{r})$ is concentrated, $\rho_{\beta}(\mathbf{r})$ is diluted. As a consequence $\nabla^{2} s(\mathbf{r}) \ll 0$, leading to a very positive local source from the region around CPs $\mathbf{4}$ and $\mathbf{4}^{\prime}$. This region will give a large $\alpha$ effect, hence it will cause an increase of the spin density in the other regions of the system. Though both CC $\mathbf{3}$ and CP 4,4' have positive spin density, they have opposite local source effects linked to the chemical difference between the two regions; in fact the first is dominated by a paired lone pair while the second is dominated by unpaired electrons.

### 2.3.3 Total atomic spin population and atomic laplacian of the spin density:

The total spin population of each atom within a molecular system is defined by

$$
S P(\Omega)=N_{\alpha}(\Omega)-N_{\beta}(\Omega) \text { eq. } 6
$$

where

$$
N(\Omega)=\int_{\Omega} \rho(\mathbf{r}) d r \text { eq. } 7
$$

is the atomic population of the atomic basin $\Omega$, defined as the portion of $\mathrm{R}^{3}$ bounded by a surface never crossed by ED gradient lines:

$$
\nabla \rho(\mathbf{r}) \bullet n(\mathbf{r})=0 \text { eq. } 8
$$

( $\mathrm{n}(\mathbf{r})$ being the unit vector normal to the surface at $\mathbf{r}$ ). It is clear that, from the definition of electron density and spin electron density, eq. 7 can be re-written as sum of the $\alpha$-electrons and $\beta$-electrons contributions

$$
\left.N(\Omega)=\int_{\Omega} \rho_{\alpha}(\mathbf{r})+\rho_{\beta}(\mathbf{r})\right) d \mathbf{r} \text { eq. } 9
$$

while eq. 6 can be written as difference between the two ED counterparts

$$
S P(\Omega)=\int_{\Omega}\left(\rho_{\alpha}(\mathbf{r})-\rho_{\beta}(\mathbf{r})\right) d \mathbf{r} \text { eq. } 10
$$

Analogously for the atomic spin cause: the atomic Laplacian of the spin density, $\nabla^{2} \mathrm{~s}(\Omega)$, is given by:

$$
\left.\nabla^{2} s(\Omega)=\int_{\Omega} \nabla^{2} s(\mathbf{r}) d r=\int_{\Omega} \nabla^{2} \mid \rho_{\alpha}(\mathbf{r})-\rho_{\beta}(\mathbf{r})\right] d \mathbf{r} \text { eq. } 11
$$

Atomic electron spin density and the atomic laplacian of the spin density reveal us how the lone electron is localized on the oxygen atom in water triplet molecular system. The oxygen spin density population amounts to about $67 \%$ of the total unpaired population. The integrated $\nabla^{2} \mathrm{~s}(\mathbf{r})$ is positive for the hydrogen and negative for the oxygen (see Tab.4); these values of the Laplacian of the electron spin density may be interpreted as the effect of the atoms within the molecular system at very remote points (where the geometric Green's function term ${ }^{\text {d }}$ may be taken out from the integral), or as an average effect of the atom.

| $\Omega$ | $\mathrm{q}(\Omega)$ | $\mathrm{SP}(\Omega)$ | $\nabla^{2} s(\Omega)$ |
| :---: | :---: | :---: | :---: |
| H | 0.425 | 0.288 | 0.019 |
| O | -0.850 | 1.422 | -0.038 |

Tab.4: Values of atomic net charge, atomic electron spin density, and atomic Laplacian of spin density

We analyse in the following the reconstruction of the ED and of the spin ED at the CPs displayed in Fig. 1, in terms of the corresponding SF or $\mathrm{SF}_{\mathrm{S}}$ atomic contributions (Table 5). Considering the SF electron density contributions at the bcp 1 (Figure 1) it is possible to note how the contribution from the oxygen atom is larger than that of its bonded hydrogen atomic basin, reflecting the polarity of the bond. In fact at bcp the oxygen atom causes about $60 \%$ of the CP ED value, while about $40 \%$ of this value comes from the bonded hydrogen and a negligible amount from the remaining nonbonded hydrogen. The reconstruction of $s(\mathbf{r})$ at the same reference point is completely different. Considering CP 1, the oxygen atom overdetermines its negative spin density while the two hydrogens, that gives a positive spin density contribution, counteract the effect of the oxygen.

Indeed it is possible to see that $\nabla^{2} \mathbf{s}(\mathbf{r})$ for the oxygen is almost all positive in the molecular plane, hence its $\mathrm{LS}_{\mathrm{s}}$ value is here negative (Fig.2) and the $\mathrm{SF}_{\mathrm{s}}$ is negative. The bcp $\mathbf{1}$ is associated to a covalent bond and is therefore normal to find this opposing effect from the two bonded atoms; however it is interesting that at bcp the oxygen contributes a negative spin density despite its unpaired alpha electrons.

|  | H |  | O |  | H |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CP | SF | $\mathrm{SF}_{\mathrm{s}}$ | SF | $\mathrm{SF}_{\mathrm{s}}$ | SF | $\mathrm{SF}_{\mathrm{s}}$ |
| 1 | 0,1109 | 0,0063 | 0,1725 | $-0,0137$ | 0,0041 | 0,0024 |
| 2 | 0,0170 | 0,0042 | 0,8622 | 0,0561 | 0,0073 | 0,0030 |
| 3 | 0,0061 | 0,0027 | 1,0178 | $-0,0004$ | 0,0061 | 0,0027 |
| 4 | 0,0082 | 0,0032 | 0,5937 | 0,3740 | 0,0082 | 0,0032 |

Tab.5: Values of SF and SFs (atomic units) in ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$ UHF/UHF computational levels


Fig.2: Electron density Laplacian, electron spin density $\mathrm{s}(\mathbf{r})$ and its Laplacian, Local Source for electron spin density in the ( $y, z$ ) plane for ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$, at UHF/UHF spin-contamination annihilated computational levels. Atomic units (a.u.) are used throughout. Contour maps are drawn at interval of $\pm(2,4,8) \cdot 10^{n},-4 \leq n \leq 0\left(s, \nabla^{2} s\right)$ and $-3 \leq n \leq 0\left(\nabla^{2} \rho\right)$. Dotted blue (full red) lines indicate negative (positive) values and full black lines mark boundaries of atomic basins. The O-H bond critical point (bcp, 1) and the bonded charge concentration point (BCC, 2 ) are shown as black and green dots.

Note that, at variance with case of the electron density reconstruction, spin transmission occurs not just through bond, but also through space. Indeed, the other non bonded hydrogen, gives an almost equal contribution to that of the bonded H . This is a fundamental difference with respect to the electron density case, where the contribution to the reconstruction of $\rho(\mathbf{r})$ at bcp given by the bonded hydrogen atom largely exceeds that of the non-bonded hydrogen.

[^8]

Fig.3: Electron spin density $\mathrm{s}(\mathbf{r})$ and its Laplacian, Local Source function for electron spin density in the ( $\mathrm{x}, \mathrm{z}$ ) plane for ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$, at UHF/UHF spin-contamination annihilated computational levels. Atomic units (a.u.) are used throughout. Contour maps are drawn as in Figure 2. The CC critical point (CP number 3 coloured green) and the two lone pair electron critical points (CPs number 4 and 4', coloured red) are shown.

The spin reconstruction for the three critical points associated respectively to the non-bonded lone pair (CC 3) and the two unpaired alpha electrons around the oxygen atom (CP $\mathbf{4}$ and $\mathbf{4}^{\mathbf{4}}$, ) are all characterised by a positive spin density. Nevertheless their reconstructions in terms of atomic contributions, largely differ. In fact at the two (3;-1) CPs the only contribution to $s(\mathbf{r})$ is given by the oxygen atom (the same is true for the reconstruction of $\rho(\mathbf{r})$ ) because the point is located inside a region of extremely highly negative $\nabla^{2} s(\mathbf{r})$ (which causes a positive contribution in terms of $\mathrm{SF}_{\mathrm{s}}$ ), see Fig. 3. On the contrary at the lone pair $\mathrm{CCs}(\mathbf{r})$ is marginally positive and the contributions from the two hydrogen atoms dominate, overdetermining $\mathrm{s}(\mathbf{r})$ at the point (Table 5).. The contribution of the oxygen atom is instead negative but very small since the positive contribution due to the unpaired $\alpha$-electron regions, is slightly overcompensated by the negative $\mathrm{LS}_{\mathrm{s}}$ contribution due to the $\beta$-density region around CP number $3^{\text {e }}$ (see the map of $\nabla^{2} \mathrm{~s}(\mathbf{r})$ in Fig.3). In conclusion the reconstruction of $\mathrm{s}(\mathbf{r})$ at CC $\mathbf{3}$ is dominated by hydrogen atoms; interestingly, in the case of the reconstruction of the ED it is exactly the opposite. Negative sources have been often seen with some suspicion in the case of the ED reconstruction, being $\rho(\mathbf{r})$ everywhere positive (or null). The physical and chemical meaning behind their occurrence has, however, been fully and convincingly explained (see in particular Ref. 10). For the electron spin density reconstructions, negative or positive contributions are not surprising and everywhere possible. They also have a clear, immediate physical meaning. In fact negative $\mathrm{SF}_{\mathrm{s}}$ values cause an increase of $\rho_{\beta}(\mathbf{r})$ at the reference
point, making $s(\mathbf{r})$ less positive when $s(\mathbf{r})$ is positive or more negative when $s(\mathbf{r})$ is negative. ${ }^{f}$. Negative $\mathrm{SF}_{\mathrm{s}} \%$ values mean that the atom (or group of atoms) in question opposes to the value of $\mathrm{s}(\mathbf{r})$ at reference point due to the remaining atoms, making it less negative (or even positive), by enhancing $\rho_{\alpha}(\mathbf{r})$ if $s(\mathbf{r})$ is negative, or less positive (or even negative) by enhancing $\rho_{\beta}(\mathbf{r})$ if $s(\mathbf{r})$ is positive. Finally at the bonded charge concentration CC number 2 the contribution from the two hydrogen atoms is negligible because of the close proximity of this CP to the oxygen nucleus (the same is true for the electron density SF contributions).

### 2.3.4 Numerical accuracy of $\rho(r)$ and $s(r)$ reconstruction:

Reconstruction of scalar fields requires particular attention on the accuracy and precision of the process through all the portion of space under analysis. In particular, when reconstructing $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ through SF and $\mathrm{SF}_{\mathrm{s}}$ contributions it is important to assess whether such reconstructions are accurate enough, that is if they are within few per cent of the value to be reconstructed, and if such an accuracy is reasonably uniform through the molecular space. In general is known that the electron density may be accurately reconstructed provided $\rho(\mathbf{r})$ is equal to or larger than $10^{-3}$ a.u. In case of $\rho(\mathbf{r})$ smaller than $10^{-3}$ a.u. some problems arise and they become particularly serious if the value of ED that has to be reconstructed is smaller than $10^{-4}$ a.u. As a consequence one expects to find similar problems in the case of electron spin density reconstruction. Since $s(\mathbf{r})$ is an electron density difference between the two spin counterparts, its values are generally smaller than $\rho(\mathbf{r})$ also in regions close to the nuclei and in particular in the covalent bonding regions. ${ }^{g}$ For comparing the accuracies of the $s(\mathbf{r})$ vs $\rho(\mathbf{r})$ reconstructions, local percentage errors defined as a function of a distance parameter $t$ along the $\mathrm{O}-\mathrm{H}$ internuclear axis are introduced; in this way it is possible to explore the different behaviour, if any, of core, valence and bonding regions. The two percentage error ( $f_{1}$ and $f_{2}$ ) are calculated at each point $\mathbf{r}$ along the $O-H$ axis by

$$
f_{1}=\frac{\rho(\mathbf{r})_{S F}-\rho(\mathbf{r})_{t r u e} * 100 \text { eq. } 12}{\rho(\mathbf{r})_{t r u e}}
$$

and

$$
f_{2}=\frac{s(\mathbf{r})_{S F}-s(\mathbf{r})_{\text {true }}}{s(\mathbf{r})_{\text {true }}} * 100 \text { eq. } 13
$$

[^9]Since in general the electron spin density has smaller values than the electron density, one may imagine the $s(\mathbf{r})$ reconstruction to be more difficult. However, the spin density Laplacian has somewhat dampened oscillations with respect to the electron density Laplacian (see Fig.4), so the effect due to the generally lower values for spin densities could be compensated for in some way.


Fig.4: comparison of Laplacian of electron density (blue line) with respect the Laplacian of electron spin density (red line) as a function of a distance parameter t along the $\mathrm{O}-\mathrm{H}$ internuclear axis

From the comparison in terms of percentage error functions, the general accuracy for $\mathrm{s}(\mathbf{r})$ results to be worse than for $\rho(\mathbf{r})$, and especially in the regions near to the nuclei $(0.1<\mathrm{t}<0.35)$, even for the oxygen atom (see Fig.5a and 5 b). This result is quite unexpected since in such regions $s(\mathbf{r}$ ) is large enough and so a good accuracy in the reconstruction of both $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ is expected.


Fig.5: Comparison of the accuracy in reconstruction of electron density with respect the electron spin density using percentage errors defined as a function of a distance parameter $t$ along $\mathrm{O}-\mathrm{H}$ internuclear axis. Fig.5a report electron density (red line) vs $f_{1}$ percentage error function (blue line); Fig. 5 b report electron spin density (red line) vs $f_{2}$ percentage error function (blue line). Both $\rho(\mathbf{r})$ and $s(\mathbf{r})$ are in a.u.


Fig.6: Comparison of the accuracy in reconstruction of electron density with respect the electron spin density using an improved angular integration. Percentage errors are defined as a function of a distance parameter t along $\mathrm{O}-\mathrm{H}$ internuclear axis. Colours and units are the same as in Fig.5a and Fig.5b.

Such kind of behaviour can be explained as follows: at variance with $\rho(\mathbf{r})$ and $\nabla^{2} \rho, \mathrm{~s}(\mathbf{r})$ and $\nabla^{2} s_{s(\mathbf{r})}$ are far from being spherically symmetric in the atomic cores. In the case of the $s(\mathbf{r})$ reconstruction, a very accurate angular mesh need to be adopted also when integrating in the core region. By using such an improved grid for the core (the number of point is increased by four times), enabled us to obtain a very much better accuracy in the reconstruction of the electron spin density with errors tipically well below $1 \%$ and a maximal, almost acceptable, error value of about $4 \%$ only for just one very small region, namely the one where the spin density sign changes from positive to negative (see Figure 6b). Adoption of an improved angular grid for the core region had also a positive impact on the errors of the $\rho(\mathbf{r})$ reconstruction, being all lowered to values very close to $0.1 \%$ or so (see Fig.6a).

### 2.3.5 On the interpretation of $s(r)$ information using $S_{s}$ QTAIM based descriptor:

The relatively simple case of water in its ${ }^{3} \mathrm{~B}_{1}$ state (Fig.1) is chosen as an example of application of QTAIM based descriptor $\mathrm{SF}_{\mathrm{s}}$ with the aim to analyze whether such tool enables one to gain interesting and valuable insights regarding the transmission of electron spin density information and the magnetic coupling mechanism (ferromagnetic or anti-ferromagnetic coupling between atoms, spin exchange or super-exchange etc.) that are behind such transmission information. The interpretation of the results obtained in water triplet are very encouraging and, of course, pushed us to extend the application of the $\mathrm{SF}_{\mathrm{s}}$ chemical descriptor to molecular systems that are much complicated with respect this first "simpler" case. Nevertheless the results described till now for the water system do not explain in a very exhaustive way, which are the mechanism behind the transmission of electron spin density information. In particular, it is not clear if $s(\mathbf{r})$ is transmitted
through spin delocalization or spin polarization mechanisms, or also through their in tandem operation. In a very recent work by Deutch et al, the experimental decomposition of the electron density in its spin counterparts is performed for an azido double bridged $\mathrm{Cu}-\mathrm{Cu}$ molecular system (Figure 7) using an extended version of the well known Hansen\&Coppens multipolar model ${ }^{[5]}$, that permits to refine data-set of very good quality obtained combining both polarized X-ray and neutron diffraction techniques. ${ }^{\text {h }}$


Fig.7: azido double-bridge Copper II di-nuclear complex; the azido groups bridge the two $\mathrm{Cu}(\mathrm{II})$ ions through two terminal N atoms ( $\mu-1,3$ ), in what is called an END-TO-END coordination mode (EE).


Fig.8: separated $\alpha$ (a) and $\beta$ (b) electron density distributions of azido double bridge di-nuclear ( $\mathrm{Cu}-\mathrm{Cu}$ ) complex obtained combining Polarized Neutron Diffraction and X-Ray Diffraction experiments, using a spin-split version of the original Hansen\&Coppens Multipolar Model refinement

In their work the authors discuss the electron spin density distribution in terms of orbital interactions; in particular they use a fragment orbital approach and consider the interactions between the highest occupied $d$ orbitals of copper atoms and the two (one for each azido bridge) highest doubly occupied $\pi_{\text {gerade }}$ azido orbitals. The interpretation of $\mathrm{s}(\mathbf{r})$ distribution was then done through the concept of spin delocalization (due to the overlap between the fragment orbitals) and

[^10]spin polarization (that involve both the $\pi_{\text {gerade }}$ and the lowest unoccupied $\pi_{\text {ungerade }}$ molecular orbitals of the $N_{3}{ }^{-}$fragment and where the fundamental importance of $\pi-\pi^{*}$ excitations to produce the ferromagnetic coupling between the two copper atoms has been emphasized); to this aim the authors have employed either two-electron active orbitals models either more complicated ones, i.e. multi-electron models using more sophisticated multi-configurations wavefunction models.
Mimicking the orbital interpretation adopted by Aronica et al, we thought it worth introducing in our $\mathrm{SF} / \mathrm{SF}_{\mathrm{s}}$ analysis a physically-rooted partitioning of the values of the observables listed in Tab. 1 (and also of their derived SF and $\mathrm{SF}_{\mathrm{S}}$ values) in terms of a sum of two contributions: a magnetic one arising from the unpaired $\alpha$-electrons orbitals (hereinafter magnetic orbitals) and a reaction or relaxation contribution due to the remaining orbitals. ${ }^{[26]}$

## Computational details:

The correct analysis of the decomposition of both $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ in an open shell molecular system as ${ }^{3} \mathrm{~B}_{1}$ water triplet requires the use of some particular precaution in the calculation of the wavefunction ${ }^{i[19]}$. For this reason, different levels of theory were employed during all the in vacuo quantum mechanical simulation. Thus we performed $\operatorname{CASSCF}(8,8)$, UHF (Unrestricted Hartee Fock), ROHF (Restricted Open Hartree Fock) calculations with a $6-311++G(2 d, 2 p)$ basis set; moreover computations on both spin-contamination annihilated and spin contaminated UHF wavefunctions were performed; such calculations revealed that spin contamination by states of higher multiplicity than the triplet state was very small $\left(\left\langle S^{2}\right\rangle=2.0069\right)$, and becomes almost negligible when annihilation procedure is applied ( $\left\langle S^{2}\right\rangle=2.000014$ ). Static electron correlation corrections were considered by performing a $\operatorname{CASSCF}(8,8)$ computation. To this aim the starting guess was taken from the UHF spin contamination annihilated Natural Orbitals, obtaining a Slater determinant expansion of the wavefunction which included 3136 configurations of the correct symmetry and spin multiplicity. Thanks to the Natural orbitals analysis ${ }^{j}$ magnetic orbitals were very easily singled out, based on their occupation numbers, in all cases. In ROHF calculations, the wavefunction include natural orbitals with occupation numbers equal to one by definition because both $\beta$-density and relaxation contribution are equal to zero everywhere; for the other adopetd levels of theory the occupation numbers of magneric orbitals were either one or marginally different from one (highest deviation from one being 0.0003 for $\operatorname{CASSCF}(8,8)$ wavefunction). Spin densities were instead

[^11]calculated from the naturals orbitals obtained from separate diagonalizations of the $\alpha$ - and $\beta$-density matrices ${ }^{\mathrm{k}}$.

## Results and discussion:

In the molecular system ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$ the two magnetic orbitals have $\mathrm{B}_{1}$ and $\mathrm{A}_{1}$ symmetry. They are obtained through the diagonalization of the first order density matrix and by taking those natural orbitals with occupation number $(n)$ equal to or marginally different from one.


Fig.9: 3D spin density plots in the $(x, y)$ and $(z, y)$ plane, as evaluated just for the $\mathrm{B}_{1}$ and $\mathrm{A}_{1}$ symmetry magnetic natural orbitals at the $\operatorname{CASSCF}(8,8)$ level of theory. An isosurface value of $0.015 \mathrm{a} . \mathrm{u}$.
was selected, with maxima of spin density equal to 0.596 a.u. for $B_{1}$ symmetry orbital and 0.250

$$
\text { a.u. for } \mathrm{A}_{1} \text { symmetry orbital. }
$$

Figure 9, 10 and 11 report the 3D plot of the two magnetic natural orbitals (NOs) densities, of their sum and of the total spin density, respectively, for the $\operatorname{CASSCF}(8,8)$ level of theory wavefunction. For magnetic orbitals, $\rho(\mathbf{r}) \equiv \mathrm{s}(\mathbf{r}), \nabla^{2} \rho(\mathbf{r}) \equiv \nabla^{2} \mathrm{~s}(\mathbf{r}), \rho_{\alpha}(\mathbf{r}) \equiv \mathrm{s}(\mathbf{r}), \nabla^{2} \rho_{\alpha}(\mathbf{r}) \equiv \nabla^{2} \mathrm{~s}(\mathbf{r})$ while $\rho_{\beta}(\mathbf{r})$ and $\nabla^{2} \rho_{\beta}(\mathbf{r})$ are both null, so that only $s(\mathbf{r})$ and $\nabla^{2} s(\mathbf{r})$ values need to be reported (Table 6 , values in parentheses). It is very important to stress that $s(\mathbf{r})$ and $\nabla^{2} s(\mathbf{r})$ contributions due to the remaining orbitals are obtained by subtracting those of the magnetic orbitals from the total $\mathrm{s}(\mathbf{r})$ and $\nabla^{2} \mathrm{~s}(\mathbf{r})$ values. Their contributions may differ from zero at a given point, despite they are both null when integrated over the whole space.

[^12]

Fig.10: Same as Fig. 9 above, but summing up the spin density contributions of the $\mathrm{B}_{1}$ and $\mathrm{A}_{1}$ symmetry magnetic natural orbitals. Maxima of spin density fall at 0.603 a.u.


Fig.11: As Figures 9 and 10 above but plotting the total spin density. The maxima and minima of spin density fall at 0.618 a.u and -0.008 a.u. respectively.

As already discussed in the previous paragraph, besides the ( $3,-1$ ) bond critical point (bcp) of the $\rho(\mathbf{r})$ distribution (bcp 1, Fig. 1), suitable references points (rps) of the $-\nabla^{2} \rho(\mathbf{r})=\mathrm{L}(\mathbf{r})$ field for the SF analysis have been selected (Fig. 1).

Table 6 reports the values of $\rho(\mathbf{r}), \rho_{\alpha}(\mathbf{r}), \rho_{\beta}(\mathbf{r}), s(\mathbf{r})$ and the corresponding Laplacians at each reference point mentioned; such results have been obtained using wavefunctions evaluated at a common geometry (the UHF/6-311++G(2d,2p) optimized geometry ${ }^{1}$ ). The locations of each reference point differ as they correspond to the selected critical point for the considered wavefunction; however since each critical point comes from the analysis of $\rho(\mathbf{r})$, they almost coincide for the three computational levels shown in Table 6.

[^13]| RP | $\rho(\mathbf{r})$ | $\nabla^{2} \rho(\mathbf{r})$ | $\mathrm{s}(\mathbf{r})$ | $\nabla^{2} \mathrm{~s}(\mathbf{r})$ | $\rho_{\alpha}(\mathbf{r})$ | $\nabla^{2} \rho_{\alpha}(\mathbf{r})$ | $\rho_{\beta}(\mathbf{r})$ | $\nabla^{2} \rho_{\beta}(\mathbf{r})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CASSCF (8.8)//UHF(6-311++G(2d.2p)) |  |  |  |  |  |  |  |  |
| 1 | 0.291 | -2.06 | $-0.0075(0.0020)$ | $0.24(0.13)$ | 0.142 | -0.91 | 0.149 | -1.15 |
| 2 | 0.888 | -5.08 | $0.0763(0.0508)$ | $0.90(1.21)$ | 0.482 | -2.09 | 0.406 | -2.99 |
| 3 | 1.022 | -6.64 | $0.0219(0.0038)$ | $1.73(1.97)$ | 0.522 | -2.46 | 0.500 | -4.18 |
| 4 | 0.614 | -1.23 | $0.3824(0.3722)$ | $-4.45(-4.40)$ | 0.498 | -2.84 | 0.116 | 1.61 |
| UHF/(6-311++G(2d.2p)) spin contamination annihilated wavefunction |  |  |  |  |  |  |  |  |
| 1 | 0.288 | -2.14 | $-0.0050(0.0029)$ | $0.21(0.11)$ | 0.141 | -0.96 | 0.146 | -1.18 |
| 2 | 0.888 | -5.17 | $0.0631(0.0511)$ | $1.07(1.18)$ | 0.475 | -2.05 | 0.412 | -3.12 |
| 3 | 1.030 | -6.85 | $0.0051(0.0037)$ | $2.04(1.95)$ | 0.518 | -2.40 | 0.513 | -4.45 |
| 4 | 0.610 | -1.18 | $0.3818(0.3677)$ | $-4.54(-4.34)$ | 0.496 | -2.86 | 0.114 | 1.68 |
| ROHF//UHF(6-311++G(2d.2p)) |  |  |  |  |  |  |  |  |
| 1 | 0.287 | -2.14 | 0.0031 | 0.11 | 0.145 | -1.01 | 0.142 | -1.13 |
| 2 | 0.890 | -5.21 | 0.0483 | 1.20 | 0.469 | -2.01 | 0.421 | -3.20 |
| 3 | 1.031 | -6.87 | 0.0032 | 1.95 | 0.517 | -2.46 | 0.514 | -4.41 |
| 4 | 0.607 | -1.13 | 0.3637 | -4.28 | 0.485 | -2.7 | 0.121 | 1.57 |

Tab.6: Values of electron density, electron spin density, Laplacian of total $\rho(\mathbf{r})$, Laplacian of the $\alpha$ and $\beta$ counterparts of $\rho(\mathbf{r})$ and Laplacian of spin density distribution (in a.u.) at each critical point considered in Fig. 1 for the three adopted computational levels of theory; in parentheses the contributions from the two magnetic NOs are reported. For these NOs $\rho(\mathbf{r}) \equiv \mathrm{s}(\mathbf{r}), \nabla^{2} \rho(\mathbf{r}) \equiv \nabla^{2} \mathrm{~s}(\mathbf{r}), \rho_{\alpha}(\mathbf{r}) \equiv \mathrm{s}(\mathbf{r}), \nabla^{2} \rho_{\alpha}(\mathbf{r}) \equiv \nabla^{2} \mathrm{~s}(\mathbf{r})$ while $\rho_{\beta}(\mathbf{r})$ and $\nabla^{2} \rho_{\beta}(\mathbf{r})$ are both null; in the specific case of the ROHF wavefunction, $\mathrm{s}(\mathbf{r}) \equiv \rho_{\alpha, \text { mag }}(\mathbf{r})$ and $\nabla^{2} \mathrm{~s}(\mathbf{r}) \equiv \nabla^{2} \rho_{\alpha, \text { mag }}(\mathbf{r})$ where $\rho_{\alpha, \text { mag }}(\mathbf{r})$ and $\nabla^{2} \rho_{\alpha, \text { mag }}(\mathbf{r})$ denote the magnetic contribution to $\rho_{\alpha}(\mathbf{r})$ and $\nabla^{2} \rho_{\alpha}(\mathbf{r})$, respectively.

The decomposition of $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ in contributions given by the two magnetic orbitals and the reaction orbitals show how the former dominate both the large $\mathrm{s}(\mathbf{r})$ and its largely negative $\nabla^{2} \mathrm{~s}(\mathbf{r})$ at the two symmetric $(3,+1) \mathrm{L}(\mathbf{r})$ points $\mathbf{4}$ and $\mathbf{4}^{\prime}$ as well as the the spin density depletion $\left(\nabla^{2} \mathrm{~s}>0\right)$ at the in-plane NBCC 3 associated to the lone pair (see Tab.6). At bcp $\mathbf{1}$ in the case of the $\operatorname{CASSCF}(8,8)$ and UHF level of theory, the remaining orbitals overreact to the small positive $\mathrm{s}(\mathbf{r})$ contribution due to the two magnetic orbitals.


Fig.12: Electron density Laplacian, electron spin density and its Laplacian in the ( $y, z$ ) plane for ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$, at (top) $\operatorname{CASSCF}(8,8)$ and (bottom) UHF/UHF spin-contamination annihilated computational levels. Atomic units (a.u.) are used throughout. Contour maps are drawn at interval of $\pm(2,4,8) \cdot 10^{n},-4 \leq n \leq 0\left(\mathrm{~s}(\mathbf{r}), \nabla^{2} \mathrm{~s}(\mathbf{r})\right)$ and $-3 \leq n \leq 0\left(\nabla^{2} \rho(\mathbf{r})\right.$ ). Dotted blue (full red) lines indicate negative (positive) values and full black lines mark boundaries of atomic basins. The $\mathrm{O}-\mathrm{H}$ bond critical point $(\mathrm{bcp}, \mathbf{1})$ and the bonded charge concentration point $(\mathrm{BCC}, \mathbf{2})$ are shown as black and green dots, respectively.


Fig.13: Electron density Laplacian, spin density and its Laplacian in the ( $x, z$ ) plane, at (top) $\operatorname{CASSCF}(8,8)$ and (bottom) UHF/UHF spin contamination annihilated computational levels. Contour levels as in Figure 12. The non-bonded charge concentration (NBCC, $\mathbf{3}$ ) and the $(3,+1) \mathrm{L}(\mathbf{r})$ rcps $(\mathbf{4})$ are shown as green and red dots, respectively.

The last consideration is not true in the case of the ROHF wavefunction, because the reaction mechanism is unattainable and, as a consequence, $\mathrm{s}(\mathbf{r})$ remains positive at this CP . Considering the bonded charge concentration (BCC 2, coloured green), the contributions to $s(\mathbf{r})$ from the two set of orbitals are equal in sign and definitely larger for the magnetic orbital set, but the $\nabla^{2} s(\mathbf{r})$ value of
the magnetic orbitals is positive $\left(\nabla^{2} \mathrm{~s}=1.2 \mathrm{au}\right)$ and larger in magnitude than that of the remaining orbitals which is negative $\left(\nabla^{2} \mathrm{~s}=-0.3\right.$ au and -0.1 au for the $\operatorname{CASSCF}(8,8)$ and the UHF wavefunctions, respectively). This leads to a global dilution of the spin density at BCC 2.


Fig.14: Electron density Laplacian, electron spin density and its Laplacian in the ( $y, z$ ) plane for ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$ due just to the non-magnetic natural orbitals for the $\operatorname{CASSCF}(8,8)$, the UHF spin-contamination annihilated and the UHF spincontaminated computational levels. Atomic units (a.u.) are used throughout. Contour levels as in Fig.12. The O-H bond critical point (bcp, 1) and the bonded charge concentration point (BCC, 2) are shown as black and green dots.

Considering static and dynamic electron correlation at the $\operatorname{CASSCF}(8,8)$ level of theory, one may generally observe (Tab. 6, Figures 12-14) a similar qualitative picture relative to that at the UHF spin-contamination annihilated level; this agreement increases a lot when just contributions given by the magnetic orbitals are compared (Tab. 6). The spin density at the in-plane NBCC 3 associated to the lone pair shows a completely different behaviour. In fact the introduction of electron correlation effects raises $s(\mathbf{r})$ by more than five time, with respect to the value of the spincontamination annihilated wavefunction; this increase in the $s(\mathbf{r})$ value is due the reaction or relaxation contribution (Tab. 6). This noticeable effect due to electron correlation can be also observed in the $s(\mathbf{r})$ maps reported in Fig.13, where the small region of negative spin density of the UHF model lying close to the non bonded maximum disappears in the corresponding $\operatorname{CASSCF}(8,8)$ plot. The effects of electron correlation are even more evident if the UHF model spin contamination is not annihilated (the plot for this model is not shown, however, in Fig. 13). It is clear that the
electron correlation effects involve the reaction orbitals, as it is possible to deduct from Fig. 14 and Fig. 15 where maps of $s(\mathbf{r})$ and $\nabla^{2} s(\mathbf{r})$ relative to the planes shown in Fig. 12-13 and obtained using only these natural orbitals are reported.

It is now interesting to comment briefly on the different portraits of the ED and of the electron spin density Laplacians. In water, $\nabla^{2} \rho(\mathbf{r})$ implies relatively contracted valence shell charge concentration (VSCC) zones, mainly localized around nuclei and along covalent bonds, while the $\nabla^{2} \mathrm{~s}(\mathbf{r})$ negative regions are definitely more extended and possibly disjoint (Fig. 12 and 13). Furthermore, a given region of space may occur to be diluted for $\rho(\mathbf{r})$ and concentrated for $s(\mathbf{r})$ or vice-versa.


Fig.15: As in Fig. 14 above, in the ( $\mathrm{x}, \mathrm{z}$ ) plane with same contour levels. The non-bonded charge concentration (NBCC $3)$ and the $(3,+1) \mathrm{L}(\mathbf{r})$ critical points ( $\mathrm{CPs} \mathbf{4}$ and $\left.\mathbf{4}^{\prime}\right)$ are shown as green and red dots.

### 2.3.6 Electron spin density in terms of its $S F_{S}$ percentage:

We are now ready to investigate how the spin density is reconstructed in terms of spin density SF atomic contributions (eq. 4) at the chosen reference points of ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$. We will show that by decomposing the spin density in terms of non-local effects precious chemical insight may be retrieved. Table 5 reports the Bader's atomic spin population in water triplet for a wavefunction evaluated using the UHF spin contamination annihilated level of theory. These populations,
however, differ marginally with the level of theory, ranging from 0.29 to 0.31 for the H atom and from 1.42 to 1.39 for the O atom. They also indicate that $\approx 2 / 3$ of the unpaired electrons are localized in the oxygen atomic basin $\left(\Omega_{(0)}\right)$. The Laplacian of the electron spin density distribution integrates to about $0.02 \mathrm{a} . \mathrm{u}$. in the hydrogen atomic basin and to $-0.04 \mathrm{a} . \mathrm{u}$. in the oxygen atomic basin, for all adopted levels of theory. The integrated values of $\nabla^{2} s(\mathbf{r})$ reveals the influence exerted by each atom at great distance, i.e. when the Green's factor ${ }^{m}$ is small enough to be safely taken out from the integral as a constant. Therefore, H atoms in water triplet will tend to exploit a $\beta$ effect at large distances, while the O atom is expected to behave opposedly, hence to act as an $\alpha$ source, at such distances.

In general, regardless of the positive or negative value of the integrated spin density Laplacian, the actual sign of the $\mathrm{SF}_{\mathrm{S}}$ descriptor (eq. 4) will depend on the choice of the reference point which determines, through the Green's factor, the relative weight of the local cause $\nabla^{2} s\left(\mathbf{r}^{\prime}\right)$ in the various regions of the integrated atom. In Figure 16 the relative SF and $\mathrm{SF}_{\mathrm{S}}$ percentage contributions from each atomic basins of the ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$ molecular system and at each previously considered critical points (see Fig. 1 and Tab. 6 and 7 ) are reported for the $\operatorname{CASSCF}(8,8)$ model. Analogous data for the spin-contamination annihilated UHF and for the ROHF wavefunctions are shown in Figures 17 and 18. The corresponding SF and $\mathrm{SF}_{\mathrm{S}}$ absolute values are listed in Table 7 for all investigated models. Considering the bond critical point (bcp 1), the SF decomposition of the electron density distribution reveals a classical covalent polar bond with the oxygen atom (the more electronegative atom in the bond) providing $\approx 60 \%$ of $\rho(\mathbf{r})$ at the bcp. The remaining $\approx 40 \%$ is due to the bonded hydrogen, while its symmetry-related $\mathrm{H}^{\prime}$ atom has an almost negligible influence. The reconstruction of the electron spin density transmission information, obtained through the $\mathrm{SF}_{\mathrm{s}}$ chemical descriptor, is completely different. At the bcp 1, the O atom $\mathrm{SF}_{S}$ contribution is negative for both the $\operatorname{CASSCF}(8,8)$ and the UHF spin contamination annihilated levels of theory, which enable spin relaxation. The corresponding $\mathrm{SF}_{\text {S }}$ percentage contribution is positive ( $154.6 \%$ at the CASSCF $(8,8)$ level and $275.9 \%$ at the UHF spin contamination annihilated level), indicating a $\beta$ effect in this context (red colour code in Fig. 16 and 17), since it concurs to the negative $s(\mathbf{r}$ ) value at the bcp (Fig. 16 and 17).

[^14]

Fig.16: SF and $\mathrm{SF}_{\text {S }}$ percentage contributions at reference points (rps) for ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$ at the $\mathrm{CASSCF}(8,8)$ computational level. The separate contributions to $\mathrm{SF}_{S}$ due to the magnetic ( $\mathrm{SF}_{\mathrm{S}}$ mag) and the remaining ( $\mathrm{SF}_{\mathrm{S}}-\mathrm{SF}_{\mathrm{S}}$ mag) natural orbitals are also shown (for SF only those due to magnetic orbitals, denoted as SF mag). Each atom is displayed as a sphere, whose volume is proportional to the SF and $\mathrm{SF}_{\mathrm{S}}$ percentage contribution to $\rho(\mathbf{r})$ or $\mathrm{s}(\mathbf{r})$ values at the rp (first column). Colour codes: blue (yellow) atoms act as positive (negative) sources for $\rho(\mathbf{r})$ at rp considered; green (red) atoms act as positive (negative) sources for $s(\mathbf{r})$ at rp , hence yielding a $\alpha(\beta)$ effect (the sign of percentage sources is instead positive or negative whether the atomic source concurs or opposes to electron spin density at rp ).

Both hydrogen atomic basins counteract the influence of the O atom through an $\alpha$ effect; this picture of the $\mathrm{s}(\mathbf{r})$ reconstruction is confirmed by the extended zone of negative $\nabla^{2} \mathrm{~s}(\mathbf{r})$ in their basins (see Fig. 12 and 13). Such description reflects and quantifies a spin polarization mechanism, where the full pairing of covalent $\mathrm{O}-\mathrm{H}$ bonds in the $\mathrm{X}^{1} \mathrm{~A}_{1}$ water ground state is perturbed by the presence of unpaired electrons in the triplet excited state. Interestingly, at the $\operatorname{CASSCF}(8,8)$ level of theory the symmetry-related $\mathrm{H}^{\prime}$ atom provides a quite large $\mathrm{SF}_{\mathrm{S}}$ contribution at bcp 1, very similar to that from H ; on the contrary for the UHF model the hydrogen atomic basins give quite different contributions to the $s(\mathbf{r})$ value at bond critical point; the reported discrepancy is an important effect due to the introduction of electron correlation in wavefunction calculation. In both cases it is however possible to conclude that the spin polarization in the molecular plane takes place both through bond and through space mechanisms. More importantly, both mechanisms imply that the strong $\beta$ effect at the bcp due to the oxygen atom is partly (in case of $\operatorname{CASSCF}(8,8)$ level of theory)
or largely (UHF spin contamination annihilated computational level) counteracted by both hydrogen atoms.

| Point | H |  | O |  | H' |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | SF | SFs | SF | SFs | SF | SFs |
| $\operatorname{CASSCF}(8,8) / / \mathrm{UHF} / 6-311++\mathrm{G}(2 \mathrm{~d}, 2 \mathrm{p})$ |  |  |  |  |  |  |
| 1 | 0.1155 | 0.0022 (0.0087) | 0.1704 | -0.0115 (-0.0091) | 0.0046 | 0.0019 (0.0023) |
| 2 | 0.0192 | 0.003 (0.0044) | 0.8585 | 0.0713 (0.0439) | 0.008 | 0.0023 (0.0029) |
| 3 | 0.0068 | 0.0021 (0.0027) | 1.0088 | 0.0177 (-0.0016) | 0.0068 | 0.0021 (0.0027) |
| 4 | 0.0091 | 0.0024 (0.0031) | 0.5953 | 0.3761 (0.3644) | 0.0091 | 0.0024 (0.0031) |
| UHF/6-311++G(2d,2p) spin-contamination annihilated wavefunction |  |  |  |  |  |  |
| 1 | 0.1109 | 0.0063 (0.0106) | 0.1725 | -0.0137 (-0.0102) | 0.0041 | 0.0024 (0.0026) |
| 2 | 0.017 | 0.0042 (0.0049) | 0.8622 | 0.0561 ( 0.0433) | 0.0073 | 0.003 (0.0033) |
| 3 | 0.0061 | 0.0027 (0.0030) | 1.0178 | -0.0004 (-0.0022) | 0.0061 | 0.0027 (0.0030) |
| 4 | 0.0082 | 0.0032 (0.0035) | 0.5937 | 0.374 ( 0.3594) | 0.0082 | 0.0032 (0.0035) |
| ROHF//UHF/6-311++G(2d,2p) |  |  |  |  |  |  |
| 1 | 0.1104 | 0.0108 | 0.1724 | -0.0102 | 0.0041 | 0.0026 |
| 2 | 0.0168 | 0.0049 | 0.8643 | 0.0404 | 0.0072 | 0.0033 |
| 3 | 0.0061 | 0.003 | 1.0188 | -0.0027 | 0.0061 | 0.003 |
| 4 | 0.0081 | 0.0035 | 0.5901 | 0.3554 | 0.0081 | 0.0035 |

Tab.7: SF and SFs values (in a.u.) in ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$ as a function of the computational level and with contribution due to magnetic natural orbitals given in parenthesis. Values reported in this Table for SF and SFs yield the percentage source contributions at the $\mathbf{1 - 4}$ reference points shown in Figure 16 for $\operatorname{CASSCF}(8,8)$ computational level and in Figures 17 and 18 for UHF and ROHF level of theory respectively. The source contributions of magnetic natural orbitals to $\operatorname{SF}(\Omega)$ equal by definition those to $\operatorname{SFs}(\Omega)$ and are thus not reported in the Table, while their related $\%$ source contributions clearly differ; For the ROHF wavefunction, $\mathrm{s} \equiv \mathrm{s}$ mag and thus $\mathrm{SF}_{\mathrm{S}} \equiv \mathrm{SF}_{\mathrm{S}}$ mag

The comparison between the three considered computational models reveals a qualitatively similar $\mathrm{SF}_{\mathrm{S}}\left(\mathrm{H}^{\prime}\right)$ contribution, but the UHF and in particular the ROHF levels of theory give a quite large overestimated counteracting $\alpha$-effect of the hydrogen atom involved in the O-H bond. ${ }^{n}$ Further insight is provided by examining the separate contributions to $\mathrm{SF}_{\mathrm{S}}$ due to the magnetic ( $\mathrm{SF}_{\mathrm{S}}$ mag) and the remaining (relaxation) orbitals $\left(\mathrm{SF}_{\mathrm{S}}-\mathrm{SF}_{\mathrm{S}} \mathrm{mag}\right)$ (see Fig. 16, 17 and 18 and Table 6 and 7). Considering the bond critical point (bcp 1), the relaxation orbitals contributions to $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ at $\operatorname{CASSCF}(8,8)$ level of theory have a magnitude of about $99 \%$ and $127 \%$ respectively; moreover both the magnetic and the remaining orbitals concur to the strong $\beta$ effect at bcp 1 due to the oxygen atom $(+122.0 \%$ by the magnetic orbitals and $+32.6 \%$ by the remaining orbitals). On the
other side, the two H atoms show a different counteracting $\alpha$ effect due to the magnetic orbitals, while the remaining orbitals are concurring to the value of the electron spin density at bcp $\mathbf{1}$ with a $\beta$-effect (of quite different magnitude for H and $\mathrm{H}^{\prime}$ ).


Fig.17: SF and $\mathrm{SF}_{\text {S }}$ percentage contributions at some reference points (rps) for $3 \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$ at the UHF/UHF spin contamination annihilated level. The separate contributions to $\mathrm{SF}_{\mathrm{S}}$ due to the magnetic ( $\mathrm{SF}_{\mathrm{S}} \mathrm{mag}$ ) and the remaining $\left(\mathrm{SF}_{\mathrm{S}}-\mathrm{SF}_{\mathrm{S}} \mathrm{mag}\right.$ ) natural orbitals are also shown (for SF only those due to magnetic natural orbitals, denoted as SF mag). Atoms are displayed as in Fig. 16 with same colour codes.

The decomposition of $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ in terms of SF and $\mathrm{SF}_{\mathrm{S}}$ reported in Fig. 16 gives a clear picture of what are the causes of spin transmission information at the reference point considered, in fact the counteracting $\alpha$-effect given by the bonded hydrogen atomic basin is due to the magnetic orbitals $\left(\mathrm{SF}_{\mathrm{S}}\right.$ mag $\left.=-117.8 \%\right)$ but is largely compensated for by the $\beta$-effect promoted by the remaining (bonding) orbitals $\left(\left(\mathrm{SF}_{\mathrm{S}}-\mathrm{SF}_{\mathrm{S}} \mathrm{mag}\right)=+88.7 \%\right)$. The opposite is true in the case of the hydrogen atomic basin not involved in the $\mathrm{O}-\mathrm{H}$ bond; in fact the relaxation orbitals have here a very small infuence ( $+5.9 \%$ ) while the effect of the magnetic orbitals still remains significant ( SFs mag $=-$ $31.4 \%)^{\circ}$. Both $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ are largely dominated by the oxygen atomic basin at the bonded charge concentration (BCC) reference point $\mathbf{2}$ because of the close proximity of the critical point to this

[^15]atom. At BCC 2 the electron spin density is positive, about one order of magnitude larger than at bcp 1 (see Tab. 6), and similarly determined by the magnetic and remaining orbitals, with the former yielding $\alpha$ contributions for both oxygen and hydrogen atomic basins. At the two symmetric saddle points 4 and $\mathbf{4}^{\prime}$, associated to the unpaired electrons, $s(\mathbf{r})$ is two order of magnitude larger than at bcp and, like for $\rho(\mathbf{r})$, almost all determined by the oxygen atomic basin for all the computational levels considered (Fig. 16, 17, 18). In any case at these reference points $s(\mathbf{r})$ is dominated by the magnetic orbitals, both for oxygen and hydrogen contributions (UHF $=95.9 \%$; $\operatorname{CASSCF}(8,8)=97.3 \%)$. In particular, over $93 \%$ of them, at $\operatorname{CASSCF}(8,8)$ level, comes from the magnetic orbital $B_{1}$ since points $\mathbf{4}$ and $\mathbf{4}^{\prime}$ are representative of the $\alpha$-spin density described by the $\mathrm{O}[p x]$ functions. Considering the SF contributions to $\rho(\mathbf{r})$ is possible to note the different nature of the two points 2 and 4 as in case of $\mathrm{SF}_{\mathrm{S}}$. In fact at the BCC 2 reference point, both UHF and $\operatorname{CASSCF}(8,8)$ levels of theory give an almost equal contribution from the magnetic orbitals (UHF $=$ $5.9 \%$; CASSCF $=5.8 \%$ ) with a marginal influence on the reconstruction of $\rho(\mathbf{r})$; on the contrary at saddle points $\mathbf{4}$ and $\mathbf{4}^{\prime}$, such influence is about ten times larger (UHF $=60.1 \% ;$ CASSCF $=60.4 \%$ ), though clearly not as dominant as it is for $s(\mathbf{r})$. At the non-bonded charge concentration (NBCC 3) ${ }^{\mathrm{p}}$ $\mathrm{s}(\mathbf{r})$ is positive, with magnitude largely dependent on the wavefunction model. In fact, at this reference point the value of $\rho(\mathbf{r})$ is dominated by the oxygen atomic basin for each computational levels of theory, but $\mathbf{s}(\mathbf{r})$ is, at the UHF spin contamination annihilated and ROHF computational models, over-determined by the hydrogen atoms (UHF $=108 \%$; ROHF $=183.1 \%$ see Fig. 17 and 18), despite the NBCC 3 lies on the opposite side of these atoms. The introduction of static and dynamic correlation at the $\operatorname{CASSCF}(8,8)$ level of theory, enables one to recover a much less unanticipated result, as the two hydrogen atoms and the oxygen atom contribute, respectively, to $19 \%$ and $81 \%$ of the $\mathrm{s}(\mathbf{r})$ value. It is possible to explain the behaviour of the different levels of theory by considering the separated orbital contributions. The large $\alpha$-effect from the hydrogen atoms results in the UHF model from a dominant $\alpha$-contribution due to the magnetic orbitals, slightly opposed by the $\beta$-effect due to the remaining orbitals. This is not true for the oxygen atom because these orbital effects are reversed and the $\beta$-effect of the magnetic orbitals slightly prevails. More importantly, only the $\mathrm{A}_{1}$ totally symmetric magnetic orbital is really involved in such mechanisms.

[^16]

Fig.18: SF and $\mathrm{SF}_{\mathrm{S}}$ percentage contributions at rps for ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$ at the ROHF//UHF spin contamination annihilated geometry level. The separate contributions to SF and $\mathrm{SF}_{\mathrm{S}}$ due to the magnetic natural orbitals are also shown (SF mag and $\mathrm{SF}_{\mathrm{S}}$ mag, respectively). Atoms are displayed as in Fig. 16 with same colour codes.

In fact the $\mathrm{A}_{1}$ magnetic orbiotal allows the hydrogen atomic basin to exert a direct influence on the positive spin density at the non bonded charge concentration, while causing the oxygen atom to partly oppose to such influence. In the case of the ROHF wavefunction, the $\mathrm{SF}_{\mathrm{S} \text { mag }}{ }^{\mathrm{q}}$ contributions from all the atomic basins are very much alike in magnitude to those of the UHF model (see Tab. 7). In any case, because of the lack of the spin relaxation mechanism, the dominance of the hydrogen atoms $\alpha$-effect is even largely enhanced for ROHF (compare Fig. 17 and 18). The effect of including a larger amount of electron correlation $(\operatorname{CASSCF}(8,8)$ model $)$ is to enhance by one order of magnitude, from 0.0018 (UHF) to 0.0193 a.u., the contribution to $\mathrm{SF}_{\mathrm{S}}(\mathrm{O})$ from the non magnetic orbitals, while that from magnetic orbitals is very similar in the two models, both for O and H atoms. As a consequence the percentage $\operatorname{SF}_{\text {S }}$ sources for the $\operatorname{CASSCF}(8,8)$ and the UHF (or ROHF) models at NBCC 3 look very different among each other (Fig. 16, 17 and 18). Finally, it is possible to asses that $\mathrm{SF}_{\mathrm{S}}$ contributions, and in particular their magnetic and non magnetic components, can distinguish the different nature of critical points associated to the unpaired-

[^17]electrons or to the lone-pair electrons (NBCC 3 and CPs 4 and 4 respectively), while the corresponding SF values do not (Fig. 16, 17 and 18).

## Conclusions:

Analogously to the source function for the electron density (SF), the spin density source function $\left(\mathrm{SF}_{\mathrm{S}}\right)$ reconstructs the electron spin density at a reference point in terms of separate atoms or group of atoms contributions. It is clear that the reconstruction of the spin density information transmission from the paramagnetic center to the non-magnetic ones, is strongly dependent on the choice of the reference point because of the large anisotropy of $\mathrm{s}(\mathbf{r})$ and $\nabla^{2} \mathrm{~s}(\mathbf{r})$ within atomic basins. For this reason, the electron spin density at a point can be almost fully determined by the atomic basin to which the point belongs to as it is the case, in the molecular system water triplet $\left({ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}\right)$, of the saddle points $\mathbf{4}$ and $\mathbf{4}^{\prime}$ associated to the unpaired electrons in the $\mathrm{O}\left(\mathrm{p}_{\mathrm{z}}\right)$ atomic orbital. ${ }^{[26]}$ At the same time, the opposite may also occur, and even in regions within the basin of the paramagnetic center as it is the case of the charge concentration maximum associated to the lone pair, lying $0.33 \AA$ from the oxygen atomic basin and on opposite side with respect to the hydrogen atoms. At this point, the spin density is very low in value and almost fully determined by the two distant H atoms. In particular, if only the limited electron correlation enabled by the UHF model is included, the $\mathrm{s}(\mathbf{r})$ value found at this point is even overestimated $\left(\mathrm{SF}_{\mathrm{S}}\left(\mathrm{H}+\mathrm{H}^{\prime}\right) \%=108\right)$ by the contribution brought in by the two hydrogen atomic basins. In water triplet, the dominant oxygen atom contributions and the dominant hydrogen atoms contributions for the different spin density computational levels of theory evaluated at reference points associated to the unpaired and to the lone pair electrons, respectively, have been rationalized in terms of magnetic and relaxation or reaction contributions. Such kind of analysis allows the chemical interpretation of the electron spin density transmission and, in particular, has shown how static and dynamic electron correlation effects should be considered in the reconstruction of $\mathrm{s}(\mathbf{r})$ in terms of atomic (or group of atoms) contributions. In fact, when electron correlation effects are introduced $\operatorname{CASSCF}(8,8)$ level of theory), the oxygen atomic basin contribution becomes dominant also for the spin density at the lone pair position, as expected. It is very important to highlight that the electron correlation leaves almost unaffected both the oxygen and the hydrogen atomic basins magnetic contributions to the spin density at such position, while it increases the oxygen relaxation contribution by one order of magnitude with respect to the UHF spin contamination annihilated computational model. This means that at the uncorrelated (ROHF) or almost uncorrelated (UHF) levels of theory the magnetic orbitals are already very similar to those of the $\operatorname{CASSCF}(8,8)$ model where electron correlation is
included ${ }^{\mathrm{r}}$. Increasing the wavefunction quality has instead a noticeable effect on the reaction or relaxation component. The magnetic term does not necessarily determine a positive spin density at any reference point, but may instead produce a decrease of the local spin density ( $\beta$-effect). Furthermore, the relaxation term may either concur or counteract the magnetic term in determining the spin density at a given point, regardless its link to an orbital density integrating to a null spin population over the whole space.

### 2.3.7 Transferability of $\rho(r)$ and $s(r)$ in n-alkanes and n-alkyl radicals: similarities and

 differences as viewed through the Source Function descriptorsBoth electron density and electron spin density at a point could be seen as caused by an internal source contribution from the atom where the point is located and by a sum of source contributions from the remaining atoms, or groups of atoms, within a molecule. In chemistry the atomic group transferability paradigm could be deduced from a huge amount of experimental evidences and it is corroborated by QTAIM from a quantitative point of view for a large variety of group properties ${ }^{[8]}$. Using the SF tool one may view chemical transferability from a new and insightful perspective. It is worth to highlight that this topological descriptor enables one to distinguish the case of a) perfect transferability which is achieved when the electron density of a piece of matter is fully transferable, from the case of b) compensatory transferability, exemplified for instance by the occurrence of a constant electron population for an atomic group, obtained through a compensation of charge transfers within the group, or by the situation of a constant atomic population that, however, realizes, only through significant charge polarizations within the atom itself ${ }^{[8-10 ;}{ }^{20,21]}$. Perfect transferability implies that not only the group electron density be transferable but also that the sum of contributions to that density from the remaining atoms, or group of atoms, in the system remains constant. As it is well known ${ }^{[6]}$, the terminal methyl group in $n$-alkanes, past ethane, is characterized by very transferable atomic properties like energy, electron population, volume and spectroscopic properties, regardless of the length of the chain. The transferability of the electron distribution in the methyl group is so good that a constant value for $\rho(\mathbf{r})_{b}$ at its terminal C-H bond is also observed, past ethane (see Tab. 8). Such a transferability realizes because of a constant contribution from the $\mathrm{CH}_{3}$ group and a constant external contribution from the remaining atoms in the chain, regardless of its length.

[^18]$$
\mathrm{SF}\left(\mathbf{r}_{\mathrm{b}} ; \Omega \Sigma\right)
$$
ethane

$0.27040 .0100 \quad 0.0026$
propane

| $\mathrm{H}^{2} \mathrm{CH}_{2}----\mathrm{CH}_{2}-----\mathrm{CH}_{3}$ |  |  |
| :---: | :---: | :---: |
| 0.2701 | 0.0091 | 0.0035 |

butane

$$
\begin{array}{cccc}
\mathrm{H}_{-\mathrm{CH}_{2}-----\mathrm{CH}_{2}------\mathrm{CH}_{2}-----\mathrm{CH}_{3}}^{0.2701} & 0.0091 & 0.0020 & 0.0016
\end{array}
$$

pentane

| $\mathrm{H}^{-\mathrm{CH}_{2}-----\mathrm{CH}_{2}-----\mathrm{CH}_{2}-----\mathrm{CH}_{2}------\mathrm{CH}_{3}}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.2702 | 0.0090 | 0.0019 | 0.0008 | 0.0009 | 0.2827 |

Tab.8: Electron density transferability as viewed through the Source Function, in n-alkyl radicals. The electron densities at a terminal C-H bcp are reported along with their total SF contributions from the various $\mathrm{CH}_{2}$ and $\mathrm{CH}_{3}$ groups in each system. All values are given in atomic units (a.u.). Structures of all the molecular systems here presented are obtained performing Gaussian09 QM optimizations in vacuo at UPBE1PBE level of theory, using 6-311+G** as basis set.

To study the transferability of the electron spin density, the corresponding series of $n$-alkyl radicals were chosen; all the wave functions for all the molecular systems were calculated by the UPBE1PBE/6-311+G** level of theory, after optimizing their geometries in vacuo at the same theoretical level. ${ }^{[27]}$ All the alkyl radicals are characterized by two extended chain conformations, in particular the one we studied is the more stable. In such conformation the radical carbon 2 p atomic orbital housing the unpaired electron is eclipsed to a $\beta$-CH bond. Tables 8,9 and 10 report the values of $\rho(\mathbf{r})$ and $s(\mathbf{r})$ considering both a terminal CH bond critical point and the $-\nabla^{2} \rho(\mathbf{r})(3,-1)$ non bonded charge concentration (NBCC) critical point corresponding to the unpaired electron on the radical terminal methyl group $\mathrm{CH}_{2}{ }^{\bullet}$ as reference points. The results (Tables 9 and 10) show how the terminal methyl radical group and the neighboring methylene group produce a significant contributions to the $\mathrm{s}(\mathbf{r})$ to the reference points considered, while this is not true for the remaining group moieties within the molecular system. Interestingly, for the covalently linked atoms $\mathrm{SF}_{\mathrm{S}}$ contributions are opposite in sign denoting a spin polarization along these bonds. More importantly, the analysis of the reconstruction of $\mathrm{s}(\mathbf{r})$ in terms of $\mathrm{SF}_{\mathrm{S}}$ contributions due to all the atomic groups reveals that the transferability is also ensured for the spin electron density and not just for $\rho(\mathbf{r})$; in fact the contribution from the terminal methyl radical is constant throughout the series and this is true also for the contribution from the external groups ( $\left.\mathrm{s}(\mathbf{r})_{\text {ext }}=0.0079 \mathrm{au}\right)$. Despite its very low

[^19]value, the transferability for $\mathrm{s}(\mathbf{r})$ is also ensured if the CH terminal bond critical point ${ }^{\mathrm{t}}$ is considered. Also at this reference point, the reconstruction of $s(\mathbf{r})$ in terms of $\mathrm{SF}_{S}$ contributions show that the external groups give a negative contribution to the spin density, in clear opposition with respect to the terminal $\mathrm{CH}_{2}$ radical contribution.
$\mathrm{SF}_{\mathrm{S}}\left(\mathbf{r}_{\mathrm{b}} ; \Omega \Sigma\right)$
Ethane
$\mathrm{H}-\mathrm{CH}_{2}----\mathrm{CH}_{2}-----\mathrm{H}$
-0.0055 0.0189 -0.0149
Propane
$\mathrm{H}-\mathrm{CH}_{2}----\mathrm{CH}_{2}-----\mathrm{CH}_{2}$
-0.0001 -0.0054 0.0040
Butane

0.0000 -0.0001 -0.0054 0.0041

Pentane
$\begin{array}{ccccc}\mathrm{H}-\mathrm{CH}_{2}----\mathrm{CH}_{2}----\mathrm{CH}_{2}----\mathrm{CH}_{2}-----\mathrm{CH}_{2} \\ 0.0000 & 0.0000 & -0.001 & -0.0054 & 0.0040\end{array}$
$\mathrm{s}\left(\mathbf{r}_{\mathrm{b}}\left(\mathrm{H}-\mathrm{CH}_{2}\right) \quad \mathrm{SF}_{\mathrm{S}}\left(\mathbf{r}_{\mathrm{b}} ; \mathrm{ext}\right)\right.$
$-0.0015 \quad-0.0055$
$-0.0016 \quad-0.0056$
$-0.0016 \quad-0.0055$
$-0.0016 \quad-0.0055$

Tab.9: Electron spin density transferability, as viewed through the Source Function for the spin density, in n-alkyl radicals. The spin densities at a terminal $\mathrm{C}-\mathrm{H} \mathrm{bcp}$ are reported along with their total $\mathrm{SF}_{\mathrm{S}}$ contributions from the various $\mathrm{CH}_{2}$ and $\mathrm{CH}_{3}$ groups in each system. All values are given in atomic units (au). Structures of all the molecular systems are obtained as in Tab.8.

In figure 20 are reported the reconstructions for the electron and the electron spin density in terms of SF and $\mathrm{SF}_{\mathrm{S}}$ percentages, respectively, and considering both the bcp and the ( $3,-1$ ) reference points in the butyl radical molecular system (Figure 19). Analysing the $\mathrm{s}(\mathbf{r})$ reconstruction at the terminal C-H bcp (Fig.20c), it is clear that if the contributions for the atomic groups decay faster than for $\rho(\mathbf{r})$ (compare Tables 8 and 9 ), on the other hand this is not true if we consider the individual atomic contributions since those of the hydrogen atoms always largely oppose those from carbon atoms. In particular, the small positive contribution from the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group is the result of a huge percentage positive contribution from the carbon and an almost compensating percentage negative contribution from the two linked hydrogen atoms. Moreover the reconstruction of $\mathrm{s}(\mathbf{r})$ at the terminal bcp reveal a not negligible positive contribution from the H 10 atom of the neighboring methylene group, that is eclipsed to the unpaired electron orbital. Summarizing, at the $\mathrm{bcp}, \mathrm{s}(\mathbf{r})$ is due to an almost compensation between a negative and greater in magnitude

[^20]contribution from the $\mathrm{CH}_{2}$ group directly bonded to the methyl radical and a smaller and positive contribution from the terminal $\mathrm{CH}_{2}{ }^{\circ}$.

| $\mathrm{SF}_{\mathrm{S}}\left(\mathbf{r}_{\mathrm{b}} ; \Omega \Sigma\right)$ | $\mathrm{s}(\mathbf{r})_{\mathrm{b}}\left(\mathrm{H}-\mathrm{CH}_{2}\right)$ | $\mathrm{SF}_{\mathrm{S}}\left(\mathbf{r}_{\mathrm{b}} ; \mathrm{ext}\right)$ |
| :---: | :---: | :---: |
| Ethane |  |  |
| H-CH2----- $\mathrm{CH}_{2}----\mathrm{H}$ |  |  |
| -0.0079 0.0924 -0.0054 | 0.0791 | -0.0079 |
| Propane |  |  |
| $\mathrm{H}-\mathrm{CH}_{2}----\mathrm{CH}_{2}-$---- $\mathrm{CH}_{2}$ |  |  |
| $-0.0001-0.00780 .0870$ | 0.0791 | -0.0079 |
| Butane |  |  |
| H-CH2----- $\mathrm{CH}_{2}----\mathrm{CH}_{2}----\mathrm{CH}_{2}$ |  |  |
| $0.0000-0.0001-0.0078$ 0.0864 | 0.0791 | -0.0079 |
| Pentane |  |  |
| $\mathrm{H}-\mathrm{CH}_{2}$----- $\mathrm{CH}_{2}-$---- $\mathrm{CH}_{2}-$---- $\mathrm{CH}_{2}-$------ $\mathrm{CH}_{2}$ |  |  |
| $\begin{array}{llllll}0.0000 & 0.0000 & -0.0001 & -0.0078 & 0.0868\end{array}$ | 0.0791 | -0.0079 |

Tab.10: Electron spin density transferability as viewed through the Source Function for the spin density, in n-alkyl radicals. The spin densities at $(3 ;-1)$ saddle point in $-\nabla^{2} \rho(\mathbf{r})$ as reference point are reported along with their total $\mathrm{SF}_{\mathrm{S}}$ contributions from the various $\mathrm{CH}_{2}$ and $\mathrm{CH}_{3}$ groups in each system. All values are given in atomic units (au). Structures of all the molecular systems are obtained as in Tab.8.

Regarding the NBCC critical point corresponding to the unpaired electron (Fig. 20d), it has a spin density which is larger by two order of magnitude. Again both the hydrogen atoms of the $\mathrm{CH}_{2}{ }^{\boldsymbol{}}$ radical oppose to its carbon atomic contribution, but in a much weaker way in percentage. In this case, the positive contributions from the hydrogens of the neighboring methylene group to $s(\mathbf{r})$ are small in percentage but large in value, this because here the reconstructed spin density is two order of magnitude larger. Eventually, it is possible to conclude that $\mathrm{SF}_{\mathrm{S}}$ is able to distinguish very clearly the different nature of different critical points. In fact considering the terminal CH bcp, the spin transmission information follows sigma covalent bonds and it is dominated by the reaction of the external groups to the positive SFs contribution from the terminal methyl radical. The situation is completely different for the $(3,-1)$ saddle critical point in $-\nabla^{2} \rho(\mathbf{r})$ associated to the 2 p orbital housing the unpaired electron. Here the radical carbon atomic basin gives a $\mathrm{SF}_{\mathrm{S}}$ contribution equal to $120 \%$ of the total $s(\mathbf{r})$ value. Table 11 report atomic charges, spin density and Laplacian of the spin density in butyl radical molecular system looking at the separate contributions from all atoms. From the results reported it is possible to see that more than $90 \%$ of the unpaired electron stays on the terminal methyl radical group and essentially on the carbon atomic basin. This is true in all the alkyl radical molecular systems considered within the series. ${ }^{[27]}$

| $\Omega$ | $\mathrm{q}(\Omega)$ | $\mathrm{SP}(\Omega))$ | $\nabla^{2} \mathrm{~s}(\Omega)$ |
| :---: | :---: | :---: | :---: |
| C 1 | -0.009 | 0.001 | 0.000 |
| H 2 | -0.001 | 0.000 | 0.000 |
| H 3 | 0.004 | 0.000 | 0.000 |
| H 4 | -0.002 | 0.001 | 0.000 |
| $\mathrm{CH}_{3}$ | -0.008 | 0.002 | -0.001 |
| C 5 | 0.042 | 0.010 | 0.001 |
| H 6 | -0.004 | 0.003 | -0.002 |
| H 7 | -0.008 | 0.000 | -0.001 |
| $\mathrm{CH}_{2}$ | 0.029 | 0.012 | -0.001 |
| C 8 | 0.031 | -0.007 | -0.066 |
| H 9 | 0.004 | 0.020 | 0.004 |
| H 10 | 0.007 | 0.057 | 0.011 |
| $\mathrm{CH} 2_{2}$ | 0.043 | 0.071 | -0.051 |
| C 11 | -0.114 | 0.895 | 0.124 |
| H 12 | 0.029 | 0.009 | -0.035 |
| H 13 | 0.028 | 0.009 | -0.035 |
| $\mathrm{CH}{ }_{2}$ | -0.057 | 0.914 | 0.054 |

Tab.11: Atomic charge, electron spin population and integrated electron spin density Laplacian for each atom within butyl radical molecular system and for the various $\mathrm{CH}_{2}$ and $\mathrm{CH}_{3}$ groups. All values are given in atomic units (au).

Structures of all the molecular systems here presented are obtained performing Gaussian09 QM optimizations in vacuo at UPBE1PBE level of theory using $6-311+\mathrm{G}^{* *}$ as basis set.


Fig. 19: Molecular scheme for butyl radical molecular system optimized at UPBE1PBE/6-311+G**

(a)

(c)

(b)

(d)

Fig.20: SF and $\mathrm{SF}_{\text {S }}$ percentage contributions at reference points (rps) for butyl radical molecular system at the UPBE1PBEcomputational level. The separate contributions to $\mathrm{SF}_{\mathrm{S}}$ due to each atom is displayed as a sphere, whose volume is proportional to the SF and $\mathrm{SF}_{\mathrm{S}}$ percentage contribution to $\rho(\mathbf{r})$ or $\mathrm{s}(\mathbf{r})$ values at the rp. Figure 20a and 20b report contributions from all the atomic basins to $\rho(\mathbf{r})$ at bcp and NBCC as reference points respectively, Fig. 20c and 20d report contributions from atomic basins to $s(\mathbf{r})$ at the same reference points. Colour codes are the same as in Fig. 16.

Note: Here are presented as red balls those atoms bringing a "beta" density contribution and as green balls those atoms bringing an "alpha" density contribution.

In figures 21 and $22 \mathrm{~s}(\mathbf{r}), \nabla^{2} \mathrm{~s}(\mathbf{r})$ and $\mathrm{LS}_{\mathrm{S}}(\mathbf{r})$ maps are reported. They refer to the plane containing the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group and perpendicular to the carbon 2 p atomic orbital housing the unpaired electron (Fig.21) and the plane containing such orbital (Fig. 22).


Fig.21: $s(\mathbf{r}), \nabla^{2} s(\mathbf{r})$ and $\mathrm{LS}_{\mathrm{s}}(\mathbf{r})$ in the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ plane for butane alkyl radical molecular system, geometry is optimized at UPBE1PBE/6-311+G** theoretical level. Atomic units (a.u.) are used throughout. Contour maps are drawn at interval of $\pm(2,4,8) \cdot 10^{n},-4 \leq n \leq 0\left(\mathrm{~s}, \nabla^{2} \mathrm{~s}\right)$ and $-3 \leq n \leq 0\left(\nabla^{2} \rho\right)$. Dotted blue (full red) lines indicate negative (positive) values and full black lines mark boundaries of atomic basins. The terminal CH bond critical point is shown as a black dot and it is used as reference point in the evaluation of $\mathrm{LS}_{\mathrm{s}}(\mathbf{r})$ map.


Fig.22: $\mathrm{s}(\mathbf{r}), \nabla^{2} \mathrm{~s}(\mathbf{r})$ and $\mathrm{LS}_{\mathrm{S}}(\mathbf{r})$ in the unpaired electron plane for butane alkyl radical molecular system, geometry is optimized at UPBE1PBE/6-311+G** theoretical level. Atomic units (a.u.) are used throughout. Contour maps are drawn as in Fig. 21 with the same colour contours. The NBCC critical point associated with the unpaired electron and used as a reference point to evaluate the $\mathrm{LS}_{\mathrm{s}}(\mathbf{r})$ map is shown as a green dot.

The maps in the plane of the unpaired electron located in a singly occupied p-orbital (Fig. 22) show that $\mathrm{s}(\mathbf{r})$ is delocalized on the terminal CH bond and that along this bond the hydrogen atomic basin behaves in part as the unpaired electron on the terminal carbon atom as for its ability to produce $\alpha$ effect (see the maps of $\nabla^{2} \mathrm{~s}$ ). On the other hand, in the plane of the terminal $\mathrm{CH}_{2}{ }^{\bullet}$, where spin polarization phenomena between bonded atoms can be observed, a pronounced $\beta$ effect around terminal carbon atom is reached; this different situation is due to the positive region in $\nabla^{2} \mathrm{~s}(\mathbf{r})$ maps encompassing the carbon and the two hydrogen atomic basins. In conclusion the analyses of the electron spin densities, the Laplacian of the spin density and the $\mathrm{LS}_{\mathrm{S}}$ for a member of the series $\left(\mathrm{C}_{4} \mathrm{H}_{9}{ }^{\circ}\right)$ allows us to distinguish the different behaviour of the $\nabla^{2} \mathrm{~s}(\mathbf{r})$ of the terminal carbon atom in the molecular plane and in the perpendicular plane. In both planes $s(\mathbf{r})$ is positive (or partly positive) in the carbon basin, but $\nabla^{2} s(\mathbf{r})$ (and hence the $\mathrm{LS}_{\mathrm{S}}$ ), is totally different. When integrated
over the whole space the behaviour in the perpendicular plane dominates. It is also clear also why the hydrogen atomic basins oppose the terminal carbon contributions.

The results presented above are obtained not considering the problems of spin contamination and not including static and dynamic electron correlation, which can both influence significantly the results of the topological analyses of $\rho(\mathbf{r})$ and $s(\mathbf{r})$.. For this reason the calculation of the spin contamination annihilated wavefunction [Gaussian code : $\operatorname{IOP}(5 / 14=2)$, pop $=$ noab] was performed at the same UPBE1PBE/6-311+G(d,p) level of theory, both for the geometry optimization and the $\mathrm{SF}_{\mathrm{S}}$ analysis. Interestingly, but not unexpectedly, significant differences were reached only in the analysis of $s(\mathbf{r})$. In fact, considering the bond critical point, a difference of $0,6 \%$ in terms of electron density value is reached between the spin-contaminated and the spin contamination annihilated wave functions; on the other hand it is possible to observe a percentage difference as large as $265 \%$ for the electron spin density, with $\mathrm{s}(\mathbf{r})$ becoming less negative and decreasing in magnitude upon spin contamination annihilation. The situation change when NBCC is considered: at this critical point the percentage difference between the values of $\mathrm{s}(\mathbf{r})$ is equal to $17,5 \%$ and with spin annihilated value increasing in magnitude with respect to that of the spin contaminated wavefunction in this case. The removal of the spin contamination has a large effect on the local evaluation of the electron spin density which is either overestimated or underestimated in magnitude by the contaminated wavefunction, depending on the location (clearly this is an obvious result, since both wavefunctions need to integrate to the same number of unpaired electrons, namely one in this case). Integration of the spin density over the atomic basins of the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group typically shows that more than $91 \%$ of the excess $\alpha$ density lies in this group and essentially on the C atom ( $90 \%$ ), the second most important contribution ( $6 \%$ ) coming from the eclipsed $\beta$-hydrogen atom mentioned above. Tables 12, 13 compare respectively the electron density and the electron spin density transferability at the $\mathrm{C}-\mathrm{H}$ bcp of the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group for all considered radicals. Perfect transferability is confirmed to occur also for the spin contamination annihilated wave function. The dominant contribution to $\rho(\mathbf{r})$ at the bcp electron density ( 0.265 au ) comes from the terminal methyl group hosting the bcp, while the remaining methyl and methylene bridge groups adjust their contributions to provide a constant residual density ( 0.013 au ). An almost perfect transferability is recovered also for the very low value of $s(\mathbf{r})(-0.0004 \mathrm{au})$ for all systems at the bcp. The overall $\alpha \mathrm{SF}_{\mathrm{S}}$ contribution from the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group, $\mathrm{s}(\mathbf{r})=0.0041$, is more than compensated for by an overall $\beta$ and constant contribution, $s=-0.0045$, arising from the remaining part of the molecule, regardless of the length of the chain. Even in the case of spin contamination annihilated wave function, spin transferability is ensured through a combination of opposing $\alpha$ and $\beta$ SF $_{S}$ cumulative effects of similar magnitude. An equally remarkable transferability characterizes
the value of the spin density at the $(3,-1)-\nabla^{2} \rho$ critical points associated to the non-bonded charge concentrations (NBCC) and largely due to the unpaired electron (see Tab. 14). At the NBCC, $\mathrm{s}(\mathbf{r})$ is large and positive ( 0.0968 a.u.) and completely dominated by the overall $\alpha$ effect contribution from the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group ( 0.1026 a.u.). The remaining groups of the molecule counteract slightly such contribution through a comparatively modest overall $\beta$ effect ( -0.0058 a.u.). In conclusion, as in case of the spin contaminated wave function, perfect transferability holds true for both the $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ distributions in n -alkyl radicals. Yet, it realizes in quite different ways, largely dependent on the selected reference point.
$\mathrm{SF}\left(\mathbf{r}_{\mathrm{b}} ; \Omega \Sigma\right)$
Ethane

0.26400 .01040 .0027

Propane
$\mathrm{H}-\mathrm{CH}_{2}$----- $\mathrm{CH}_{2}-$---- $\mathrm{CH}_{3}$ 0.26470 .00910 .0033
0.2771

Butane
 0.26450 .00920 .00110 .0022

Pentane

| $\mathrm{H}^{-\mathrm{CH}_{2}----\mathrm{CH}_{2}-----\mathrm{CH}_{2}-----\mathrm{CH}_{2}------\mathrm{CH}_{3}}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0.2647 | 0.0092 | 0.0013 | 0.0014 | 0.0009 | 0.2771 |

Tab.12: Electron density transferability as viewed through the Source Function, in n-alkyl radicals. For these molecules, the bcp electron densities of the terminal C-H bond, along with their SF contributions from the various $\mathrm{CH}_{2}$ and $\mathrm{CH}_{3}$ groups in each molecule, are reported.. All values are given in atomic units (a.u.). Data are obtained from spin contamination annihilated wavafunction, at optimized geometry and using the UPBE1PBE level of theory with 6$311+\mathrm{G}^{* *}$ basis set.

In figures 23 and 24 are reported the reconstructions of $\rho(\mathbf{r})$ and $s(\mathbf{r})$ in terms of SF and $\mathrm{SF}_{\mathrm{S}}$ atomic components for the $n$-butyl radical at the bcp and the NBCC reference points, respectively. Comparison between figures 20c and 23b reveals that, as in the case of spin contaminated wave function, at the bcp the atoms bonded to each other always oppose themselves in their action, one giving an $\alpha$ and the other a $\beta$ effect. This situation is reached in case of through-bond spin transmission between covalently bonded atoms ("antiferromagnetically" coupled). ${ }^{[27,28]}$

$$
\mathrm{SF}_{\mathrm{S}}\left(\mathbf{r}_{\mathrm{b}} ; \Omega \Sigma\right)
$$

$$
\mathrm{s}(\mathbf{r})_{\mathrm{b}}\left(\mathrm{H}-\mathrm{CH}_{2}\right) \quad \mathrm{SF}_{\mathrm{S}}\left(\mathbf{r}_{\mathrm{b}} ; \mathrm{ext}\right)
$$

Ethane

0.00403 -0.00422-0.0027

$$
-0.00044 \quad-0.00448
$$

Propane

0.00403 -0.00422-0.0027
-0.00044
-0.00448
Butane

$0.00409-0.00422-0.0024-0.00004-0.00041-0.00450$

Pentane

$0.00409-0.00422-0.0024-0.00004-0.00000 \quad-0.00041-0.00450$

Tab.13: Electron spin density transferability as viewed through the Source Function for the spin density, in n-alkyl radicals. For these molecules, the bcp electron spin densities of the terminal C-H bond, along with their SF contributions from the various $\mathrm{CH}_{2}$ and $\mathrm{CH}_{3}$ groups in each molecule, are reported.. All values are given in atomic units (a.u.). Molecular systems were computed at the same level of theory indicated in Tab.12.

$$
\mathrm{SF}_{\mathrm{S}}\left(\mathbf{r}_{\mathrm{b}} ; \Omega \Sigma\right)
$$

$\mathrm{s}(\mathbf{r})_{\mathrm{b}}\left(\mathrm{H}-\mathrm{CH}_{2}\right) \quad \mathrm{SF}_{\mathrm{S}}\left(\mathbf{r}_{\mathrm{b}} ; \mathrm{ext}\right)$
Ethane
$\mathrm{H}-\mathrm{CH}_{2}$----- $\mathrm{CH}_{2}-----\mathrm{H}$
$0.10246-0.0560-0.00210 .09665-0.00581$
Propane
$\mathrm{H}-\mathrm{CH}_{2}-----\mathrm{CH}_{2}-----\mathrm{CH}_{3}$
$0.10246-0.0560-0.00210 .09665$-0.00581
Butane
$\mathrm{H}-\mathrm{CH}_{2}----\mathrm{CH}_{2}$----- $\mathrm{CH}_{2}----\mathrm{CH}_{3}$
0.10264 -0.0560 -0.00019 -0.00004
$0.09680-0.00583$
Pentane

$0.10263-0.0560-0.00019-0.00004-0.00000 \quad 0.09680 \quad-0.00584$

Tab.14: Electron spin density transferability as viewed through the Source Function for the spin density, in n-alkyl radicals. The spin densities at $(3 ;+1)$ saddle point in $\nabla^{2} \rho(\mathbf{r})$ as reference point are reported along with their total $\mathrm{SF}_{\mathrm{S}}$ contributions from the various $\mathrm{CH}_{2}$ and $\mathrm{CH}_{3}$ groups in each system. All values are given in atomic units (a.u.).

Molecular systems were computed at the same level of theory indicated in Tab.12.

Moreover both the individual atomic $\mathrm{SF}_{\mathrm{S}}$ contributions and the overall contributions from the terminal $\mathrm{CH}_{2}{ }^{\circ}$ or from its neighbouring $\mathrm{CH}_{2}$ group are very large in magnitude compared to the $\mathrm{s}(\mathbf{r})$ value they concur to reconstruct at reference point considered. Interestingly, while the SF
contributions from the hydrogen atoms of the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group to the $\mathrm{C} 11-\mathrm{H} 13 \mathrm{bcp} \rho(\mathbf{r})$ markedly differ between each other, this is not at all the same for the corresponding $\mathrm{SF}_{\mathrm{S}}$ contributions which are more comparable in magnitude. ${ }^{\text {u }}$ For this reason, it is possible to conclude that the spin density at C-H bcp originates from much less local sources than it is for its corresponding electron density. The reconstruction of $s(\mathbf{r})$ at the NBCC located above the plane of the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group (Fig. 24b) reveals a different situation: here $s(\mathbf{r})$ is quite large and positive and it is essentially determined by the carbon atom where the unpaired electron is essentially located $\left(\mathrm{SF}_{\mathrm{S}} \%_{(\mathrm{C} 11)}=113.4 \%\right)$; its linked hydrogen and carbon atoms neutralize the slight $\alpha$-effect excess arising from the C 11 atom. So it is possible to assess that the $\mathrm{SF}_{\mathrm{S}} \%$ values are able to neatly distinguish the case where the reference point characterizes a covalent bonding interaction, with respect to the case where it is associated to a NBCC largely due to a fairly localised unpaired electron. In fact spin information transmits differently in dependence of the reference point considered. In any case, the magnitude of the overall $\mathrm{SF}_{\mathrm{S}}$ contributions from the two hydrogen atoms of the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group and the magnitude of the cumulative $\mathrm{SF}_{\mathrm{S}}$ contribution from the $\beta$ $\mathrm{CH}_{2}$ group, are similar for both reference points. The large discrepancy on the $\mathrm{SF}_{\mathrm{S}}$ percentages arises from the three order of magnitude larger $\mathrm{s}(\mathbf{r})$ value at NBCC compared to that at the $\mathrm{C}-\mathrm{H}$ bcp. Reconstruction of both $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ in terms of magnetic and of reaction or relaxation $\mathrm{SF}_{\mathrm{S}}$ contributions, are also reported in Fig. 23 and 24. The magnetic contribution is due only to an $\alpha$ density but it does not always lead to an $\alpha$-effect. In fact it is possible that it may also result in an overall decrease of $s(\mathbf{r})$ in dependence of the reference point considered. At the same time the reaction contribution may either concur or counteract the magnetic one in determining $\mathrm{s}(\mathbf{r})$ at the reference point. In the case of $n$-alkyl radicals, the situation is very simple as there is only one magnetic natural orbital, whose effects are clearly reported in Figures 23c and 24b for the case of $n$ butyl radical for both bcp and NBCC reference points. The role of the reaction contribution may be assessed from the difference of (b) and (c) $\mathrm{SF}_{\mathrm{S}}$ values in Figure 23 and, analogously, of (a) and (b) $\mathrm{SF}_{\mathrm{S}}$ values in Figure 24.

[^21]
$\rho(r)=0.2771 \mathrm{au}$ $s(r)=-0.0004 \mathrm{au}$

(b)

(a)
(c)

Fig.23: Atomic SF (a) and $\mathrm{SF}_{\mathrm{S}}$ (b) percentages at the $\mathrm{C} 11-\mathrm{H} 13$ bond critical point (shown as a black dot in the molecular scheme) for the $n$-butyl radical. In (c) the $\mathrm{SF}_{\mathrm{S}}$ percentages only due to the magnetic orbital density are displayed. The values of $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ at the bcp are given in a.u. Atoms are portrayed as spheres with volumes proportional to their source percentage contributions to $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ values at the bcp. Colour codes: (a) blue or yellow whether atoms represent positive or negative sources for $\rho$ at the bcp; (b) and (c) green or red whether atoms represent positive ( $\alpha$ effect) or negative ( $\beta$ effect) sources for s at bcp . Note, instead, that in (b) and (c) the sign of percentage atomic sources is positive (negative) when the atom concurs (opposes) to the $s(\mathbf{r})$ value at the bcp.

$\rho(r)=0.1717 \mathrm{au}$
$s(r)=+0.0968$ au

(a)

(b)

Fig. 24: n-butyl radical: (a) atomic $\mathrm{SF}_{\mathrm{S}}$ percentages at the $(3,-1)-\nabla^{2} \rho(\mathbf{r})$ critical point, located above the plane of the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group, highlighted as a black dot in the molecular scheme and associated to non-bonded charge concentrations largely due to the unpaired electron. In (b) the $\mathrm{SF}_{\mathrm{S}}$ percentages only due to the magnetic orbital density are displayed. The values of $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ at the reference point are shown. Colour codes for atoms and signs of atomic $\mathrm{SF}_{\text {S }}$ percentages as in Fig. 23

One observes that the magnetic orbital density dominates the reconstruction of $\mathrm{s}(\mathbf{r})$ and that the remaining relaxation density moderately (from $5 \%$ to $20 \%$ in magnitude) concurs to the effects produced by the former density, for both reference points considered. These effects may be either of
$\alpha$ or of $\beta$ in nature for the two densities, but they always agree in their nature in this case, at least for the more significant contributions.

## Conclusions:

Comparison between the electron density and the electron spin density case is illuminating about the different way $\rho(\mathbf{r})$ and $s(\mathbf{r})$ information is transmitted and comparison between different reference points allow us to gain information on how such observable are transmitted as a function of the reference point considered. In this subsection the perfect transferability in a series of n -alkyl radical through the $\mathrm{SF}_{\mathrm{S}}$ contributions at two different reference points has been examined. The first is a $(3,-1)$ critical point in the $-\nabla^{2} \rho(\mathbf{r})$ corresponding roughly to the maximum in the $\mathrm{s}(\mathbf{r})$ above (or below) the plane of the terminal methyl radical group. ${ }^{v}$ while the second reference point examined is the C-H bond critical point of the terminal methylene radical group. Wavefunctions for all the molecular systems within the series were calculated at the UPBE1PBE/6-311+G(d,p) level of theory, using the Gaussian-09 code. Both spin contaminated and spin contamination annihilated wavefunctions were used for both geometry optimization and $\mathrm{SF}_{\mathrm{S}}$ analysis. As expected, integration of the spin density over the basin of the terminal $\mathrm{CH}_{2}{ }^{\circ}$ group typically shows that more than $90 \%$ of the excess $\alpha$ density lies in this group and essentially on the carbon atomic basin ( $90 \%$ ), the second most important contribution ( $6 \%$ ) coming from the eclipsed $\beta$-hydrogen atom mentioned above. Perfect transferability of electron density is found to occur also in the $n$-alkyl radicals, and with similar mechanisms to those operative in the corresponding alkanes. Moreover, an almost perfect transferability is also recovered for the very low value of $s(\mathbf{r})(-0.0004$ a.u.) at the bcp. At this reference point, the $\alpha \mathrm{SF}_{\mathrm{S}}$ contribution from the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group is compensated for by an overall $\beta$ and constant contribution arising from the remaining part of the molecule, regardless of the length of the chain. So it is possible to asses that perfect transferability of $s(\mathbf{r})$ is ensured through a combination of opposing $\alpha$ and $\beta \mathrm{SF}_{\mathrm{S}}$ cumulative effects of similar magnitude. Quite different is the case for the spin density reconstruction at the non bonded charge concentration located above the plane of the terminal $\mathrm{CH}_{2}{ }^{\bullet}$ group, where the very large spin density value is essentially determined by the carbon atom carrying the unpaired electronand where the role of its linked hydrogen and carbon atoms is just that of neutralizing the slight $\alpha$-effect excess arising from the radicalic carbon. In summary, though perfect transferability holds true for both the electron and

[^22]the electron spin density in n-alkyl radicals, it realizes in quite different ways and largely dependent on the selected reference point.

### 2.4 INTERPRETATION OF FERRO-MAGNETIC INTERACTIONS IN AZIDO Cu(II) DINUCLEAR COMPLEXES USING THE SF S $_{S}$ BASED TOPOLOGICAL DESCRIPTORS:

### 2.4.1 Introduction:

Applications of $\mathrm{SF}_{\mathrm{S}}$ concerning crystalline systems are now discussed in the remaining part of this chapter . To this purpose an investigation of molecular crystals will be discussed in the next paragraphs, regarding specifically the study of ferromagnetic interactions in two azido doublebridged Copper II dinuclear complexes. Several studies have been previously performed on metal azido complexes and their magneto-structural relationships. In the case of azido double-bridge Copper II dinuclear complexes, the azido groups bridge the $\mathrm{Cu}(\mathrm{II})$ ions through one terminal N atom ( $\mu-1,1$ ), in the so-called END-ON (EO) coordination mode, or through two terminal N atoms ( $\mu-1,3$ ) in the so-called END-TO-END coordination mode (EE) (see Fig. 25). In both EO and EE systems, the bridge may be either symmetric with the two $\mathrm{N}-\mathrm{Cu}$ bonds being equivalent and short (around $2.0 \AA$ ) or asymmetric with one short (about $2.0 \AA$ ) and one long (from $2.3 \AA$ to $2.7 \AA$ ) Cu N bond. Generally, EO systems are symmetric while EE systems are asymmetric. In a magnetic perspective, the EO coordination mode mostly provides ferromagnetic $\mathrm{Cu}-\mathrm{Cu}$ interactions ${ }^{\mathrm{w}}$, while the magnetic interactions are zero or generally very small and weakly antiferromagnetic (with a coupling constant J of less than $-100 \mathrm{~cm}^{-1}$ ) in the asymmetric EE systems even if it is possible to observe a ferromagnetic interaction in some cases. The few EE symmetric systems showing 6 -fold coordination of Cu (II) are instead strong anti-ferromagnetic in nature, with a very large coupling constant and the two bridging azido groups supporting strong overlap between the $\mathrm{Cu} \mathrm{d}_{\mathrm{x} 2-\mathrm{y} 2}$ magnetic orbitals (with, in this case, $x$ and $y$ directed approximatevely along the two $\mathrm{Cu}-\mathrm{N}$ (azide) bonds). Asymmetric EE molecular systems where the two copper atoms have a square pyramidal geometry, display instead one terminal azido nitrogen (namely that associated to the short $\mathrm{Cu}-\mathrm{N}$ bond) pointing to the $\mathrm{d}_{\mathrm{x} 2-\mathrm{y} 2}$ magnetic orbital of Cu and the other terminal pointing approximatively to the (almost filled) $\mathrm{d}_{\mathrm{z2}}$ orbital of Cu . The long apical $\mathrm{Cu}-\mathrm{N}_{\text {azide }}$ bonds comply with such simple orbital picture.

[^23]
(a)


(b)

Fig. 25: General structures for azido double-bridge Copper II dinuclear complexes: in 25a symmetric (left) and asymmetric (right) END-ON (EO) coordination modes are reported while in 25 b the symmetric (top) and asymmetric (bottom) END-TO-END coordination mode (EE) are shown.

The two cases presented in this subsection have been chosen because their experimental spin density maps from polarized neutron diffraction (PND) studies have been reported in literature, along with remarkable insights based on quantum mechanical approaches. The first case, studied by Aebersold et al ${ }^{[22]}$, involves a symmetric EO di-nuclear copper azido bridged molecular system featuring a short $\mathrm{Cu}-\mathrm{Cu}$ internuclear distance, a large FM interaction and having four pterbutylpiridine ligands other than the azido groups and two perclorate anions to guarantee the complex neutrality (Figure 26).


Fig. 26: Symmetric EO di-nuclear copper azido bridged molecular system. The ligands are four p-terbutylpiridine other than the azido groups and two perclorate anions to guarantee the complex neutrality.

The second case, already introduced in the previous paragraphs, examines an asymmetric EE complex (see Fig. 7), with large $\mathrm{Cu}-\mathrm{Cu}$ internuclear distance, small FM coupling, having a square pyramidal coordination of the Cu II atoms yielded by the double-bridged azide ligands and the polydentate ligand in its hydrogenated form. Such system has been investigated by polarized neutron diffraction PND and through quantum-mechanical approaches by Aronica et al ${ }^{[23]}$;
moreover, it has been studied very recently also by joint PND and XRD experiments, employing a spin-split version of the original Hans-Coppens Multipolar Model refinement, in order to gain distinct alpha and beta electron density distributions ${ }^{[5]}$ (Fig. 8). In EO molecular system the spin distribution has been investigated in terms of orbital language, employing a fragment orbital approach and by considering the interactions between the highest occupied d atomic orbitals on the Cu atoms and the highest doubly occupied $\pi_{\text {gerade }}$ azido orbitals. The mixing of these 4 orbitals gives four molecular orbitals. The interpretation of the spin distribution was then provided by applying the concepts of spin delocalization (caused by the overlap between the fragment orbitals) and spin polarization (caused by spin interaction within the $\pi_{\text {gerade }}$ orbital of the $\mathrm{N}_{3}{ }^{-}$fragment) and also going beyond the active-electron estimate, considering as well the lowest vacant single molecular orbital of the $\mathrm{N}_{3}{ }^{-}$fragment of $\pi_{\text {ungerade }}$ symmetry. Essentially, the spin distribution may be read as the result of two mechanisms: first, a spin delocalization from the $\mathrm{Cu}^{2+}$ ions towards azido bridges and then a spin polarization within the $\pi$ orbitals of the azido groups (considering also the LUMO of the azido group). In the case of the EE molecular system the spin distribution has been investigated in terms of the shape of the two single occupied molecular orbitals (SOMOs). These orbitals are in-phase and out-of-phase arrangements of the $\mathrm{Cu}_{\mathrm{x} 2-\mathrm{y} 2}$ atomic orbitals and show large contributions to the azido bridge. Moreover the spin density distribution has been analysed in terms of the relevance of spin polarization effects. These account for the polarization of the inactive orbitals (those doubly occupied) and, namely, those of the azido groups, in particular those of the bridging azido units concerning typical $\pi-\pi^{*}$ (gerade to ungerade) excitations.

### 2.4.2 Results and discussion:

The wave functions for both EO and EE molecular systems here presented are obtained performing Gaussian09 QM energy determinations in vacuo at UB3LYP level of theory using pob-TVPZ as basis set and the experimental molecular structures reported in references 22 and 23. Considering the EO system, about $60 \%$ of unpaired electrons density is localized on the $\mathrm{Cu}(\mathrm{II})$ ions, $20 \%$ is delocalized over the azido groups and the remaining $20 \%$ on the pyridine nitrogen atoms, as displayed by the spin populations (see Tab.15). The central nitrogen of the azido group shows a small negative spin population, $\mathrm{s}(\mathrm{N} 2)$; moreover, the integrated $\nabla^{2} \mathrm{~s}(\mathbf{r})$ is relevant only for the Cu atoms and the azido group atoms. Note that an average positive value for the Laplacian of the spin density, correspondingh to a dominating beta-effect, was a bit unexpected for the copper atom. Thus, the attitude of the metal centre in being a source of $\alpha$-spin seems to be very directional, very localized and through an $\alpha$-spin-delocalization towards the ligands as the $\nabla^{2} s(\mathbf{r})$ map in the plane
containing the two copper atoms plainly displays (see Fig. 27). A further remarkable feature in terms of $\nabla^{2} \mathrm{~s}(\Omega)$ values is the difference among the azido group nitrogens, with the terminal one performing otherwise than the remaining two and the central one being the atom with the highest $\alpha$ spin effect.

| $\Omega$ | $\mathrm{q}(\Omega)$ | $\mathrm{s}(\Omega)$ | $\nabla^{2} \rho_{\alpha}(\Omega)$ | $\nabla^{2} \rho_{\beta}(\Omega)$ | $\nabla^{2} \mathrm{~s}(\Omega)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Cu | 1.095 | +0.617 | +0.009 | -0.009 | +0.018 |
| N 1 | -0.489 | +0.089 | -0.004 | +0.003 | -0.007 |
| N 2 | -0.138 | -0.011 | -0.011 | +0.011 | -0.022 |
| N 3 | +0.039 | +0.110 | +0.008 | -0.008 | +0.016 |
| N$)_{3}{ }^{\circ}$ | -0.588 | +0.188 | -0.007 | +0.006 | -0.013 |
| N 4 | -1.056 | +0.095 | +0.001 | -0.001 | +0.002 |
| N 5 | -1.084 | +0.086 | +0.001 | -0.001 | +0.001 |

Tab. 15: Atomic charges, electron spin populations,, atomic Laplacians of electron spin density divided in $\alpha$ and $\beta$ counterparts and Atomic Laplacians of electron spin density in the symmetric EO molecular system and only for the atomic basins (copper and nitrogens) involved in the azido-bridge. All values are given in atomic units (a.u.).


Fig. 27: Electron spin density $s(\mathbf{r})$ and its Laplacian and Electron density Laplacian in the ( $\mathrm{x}, \mathrm{y}$ ) plane for symmetric EO di-nuclear copper azido bridged molecular system at UB3LYP/pob-TVPZ computational levels. Atomic units (a.u.) are used throughout. Contour maps are drawn at interval of $\pm(2,4,8) \cdot 10^{n},-4 \leq n \leq 0$ (s, $\left.\nabla^{2} \mathrm{~s}\right)$ and $-3 \leq n \leq 0\left(\nabla^{2} \rho\right)$. Dotted blue (full red) lines indicate negative (positive) values.

Considering the aspherical $d$-electron distribution around the two copper atoms, it is possible to see from the maps of the Laplacian of the spin density how they are fourfold coordinated in an almost square planar arrangement of ligands. According to crystal field theory, and for a $d^{9}$ configuration on Cu atom, the $\mathrm{d}_{\mathrm{x} 2-\mathrm{y} 2}$ orbital is the magnetic singly occupied orbital. By analysing $\nabla^{2} \rho(\mathbf{r})$, the Charge Depletions (CD) on the Cu atom, related to the singly occupied $\mathrm{d}_{\mathrm{x} 2-\mathrm{y} 2}$ orbital, are indeed found to be pointing towards the charge concentrations (CC) related to the nitrogen lone pairs, in agreement with a key-lock interaction mechanism between the metal and the ligands. From the map
of $\mathrm{s}(\mathbf{r})$ and $\nabla^{2} \mathrm{~s}(\mathbf{r})$ reported in Fig. 27, it is possible to note that the spin density surrounding the Cu has the shape of the $\mathrm{d}_{\mathrm{x} 2-\mathrm{y} 2}$ orbital; the same $\mathrm{d}_{\mathrm{x} 2-\mathrm{y} 2}$ shape is even more evident considering $\nabla^{2} \mathrm{~s}(\mathbf{r})$ around the metal centers. Based on the Cu orbital filling related to $\mathrm{Cu} \mathrm{d}^{9}$ in square-planar coordination, the CDs, oriented along the ligands are expected to be characterized by larger spin density values, while the CCs, oriented along the orthogonal direction XY by smaller $s(\mathbf{r})$ values. In this case, a difference of one order of magnitude indeed occurs in the spin density values of the CCs (0.021 a.u.) relative to those of the CDs (0.282 a.u.). The CC is located in a region of positive $\nabla^{2} s(\mathbf{r})$, transmitting $\beta$-spin density, while the CD behaves as a source of $\alpha$-spin density.

(a)

(b)

Fig. 28: aspherical $d$-electron distribution around the two copper atoms in EO molecular system (a) and EE molecular


Fig. 29: Electron density Laplacian in the ( $\mathrm{x}, \mathrm{y}$ ) plane for symmetric EO di-nuclear copper azido bridged molecular system at UB3LYP/pob-TVPZ computational levels. Orange dots represent CC while CD are represented by purple dots, eventually bcp are represented by black dots. Atomic units (a.u.) are used throughout and contour maps are drawn as in Fig. 27 with the same colour codes. In the left and right panels, the CC and CD critical points are denoted by orange and by purple dots, respectively, while the bcps by dots coloured in black.

It's worthy to stress that $\nabla^{2} \rho(\mathbf{r})$ and $s(\mathbf{r})$ perform complementary roles, since the former is concentrated when double occupancy occurs, while the latter is concentrated in case of single
occupancy. Interestingly, the maps of $\mathrm{s}(\mathbf{r})$ and a fortiori those of the Laplacian of the spin density, which are both observables, are also visibly showing "physical", "observable" orbitals in the present case. ${ }^{\mathrm{X}}$ Considering the $\mathrm{SF}_{\mathrm{S}}$ contributions, the spin density at the CD is almost entirely provided by the contributions from the Cu atom, while the one on the CC pointing towards the azido N receives not negligible and opposing contributions from two of the azido group atoms and a positive "ferromagnetic" coupled contribution from the other Cu atom (see Fig. 30). The $\mathrm{SF}_{\mathrm{S}}$ contributions at the Laplacian CD and CC of the Cu atom are reported in table A2.1 and A.2.2 in appendix A2.

(a)

(b)

Fig. 30: Atomic $\mathrm{SF}_{\text {S }}$ percentages reconstructing the electron spin density at the CD on the $\mathrm{Cu}-\mathrm{N} 1$ bond (a) and CC along the $\mathrm{Cu}-\mathrm{Cu}$ ' axis (b) for the EO molecular system. Atoms are portrayed as spheres with volumes proportional to their source percentage contributions to $s(\mathbf{r})$ values at the critical points considered. Colour codes: green or red whether atoms represent positive ( $\alpha$ effect) or negative ( $\beta$ effect) sources for $s(\mathbf{r})$ at the critical point considered.

The reconstruction of $\mathrm{s}(\mathbf{r})$ in terms of $\mathrm{SF}_{\mathrm{S}}$ contributions along the $\mathrm{Cu}-\mathrm{N}_{\text {bridge }}(\mathrm{N} 1)$ internuclear axis deserves further consideration, beyond that already illustrated for the CD close to the Cu atom and roughly lying along this axis. Looking at the $\mathrm{CC}(\mathrm{s}(\mathbf{r})=0.021 \mathrm{a} . \mathrm{u}$.) associated to the N 1 lone pair, pointing towards the CD of the Cu atom, a sign of the spin delocalization mechanism or of the socalled $\mathrm{Cu}-\mathrm{Cu}$ ' super-exchange interaction through the non-magnetic bridging nitrogens (Fig. 31a), is immediately evident. While the $\mathrm{SF}_{\mathrm{S}}$ contribution from the central nitrogen atom of the azidic group opposes to the positive spin density at the CC, the two copper atoms concur to the positive $\mathrm{s}(\mathbf{r}) \mathrm{CC}$ value with significant contributions from both the metal centers ( $20.7 \%$ in total). Other few reference points are of some interest along the $\mathrm{Cu}-\mathrm{N}_{\text {bridge }}$ axis. At the N nucleus, the large positive $\mathrm{s}(\mathbf{r})(0.245$ a.u.) is entirely due to the nitrogen itself, while the negative spin density at the Cu

[^24]nucleus (Fig. 31c, $\mathrm{s}(\mathbf{r})=-0.038$ a.u.) - differently from the positive spin density at the $\mathrm{CD}-$ is determined by contributions of the same sign from the N1 and N2 atoms of the azide groups and of the opposite sign from the other copper atom. It so appears that the two Cu atoms behave as non "ferromagnetically coupled" when the region of beta spin density around the Cu atom is reconstructed. The spin density at the $\mathrm{Cu}-\mathrm{N}$ bridge bond critical point is almost zero, though still positive $(\mathrm{s}(\mathbf{r})=0.001 \mathrm{a} . \mathrm{u}$.$) ; it is located close to a wide region of negative spin density separating$ the copper basin from the region of positive spin density on the bridging nitrogen due to the spin delocalization from the metal center. ${ }^{y}$ The region of negative spin density leads to a large negative contribution from the N 1 atom at bcp, almost compensating for the positive contribution from the Cu at this point. Eventually, the spin density reconstruction in terms of $\mathrm{SF}_{\mathrm{S}}$ contributions at $\mathrm{Cu}-\mathrm{N} 1$ bcp (not reported in Fig.31) shows a wide delocalization of sources, typical of reconstructions at bcps.

(a)

(b)

(c)

Fig. 31: Atomic $\mathrm{SF}_{\mathrm{S}}$ percentages electron spin density reconstructions along the $\mathrm{Cu}-\mathrm{N} 1$ bond for the EO molecular system: at the CC on the N1 atomic basin (a), at the N1 nucleus (b) and at the Cu nucleus (c). Atoms are portrayed as in Fig. 30 with same colour codes.

The reconstruction of $\mathrm{s}(\mathbf{r})$ in terms of $\mathrm{SF}_{\mathrm{S}}$ contributions for three reference points along a $\mathrm{Cu}-\mathrm{N} 5$ bond (that is of Cu with a terminal nitrogen pirydil ligand) reveals that the patterns displayed are similar to those retrieved for $\mathrm{Cu}-\mathrm{N}_{\text {azide }}$ bridge. At bcp, the nitrogen of the azido groups appear to be clearly involved in the spin delocalization through copper, because the $d_{x 2-y 2} \mathrm{Cu}$ orbital is connecting all these ligand atoms through the overlap with their fragment double-occupied HOMO orbitals (Fig.32).

[^25]
(a)

(b)

(c)

Fig. 32: Atomic $\mathrm{SF}_{\mathrm{S}}$ percentages electron spin density reconstructions along the $\mathrm{Cu}-\mathrm{N} 5$ bond for the EO molecular system: at the Cu nucleus (a), at the bcp (b) and at the N5 nucleus (c). Atoms are portrayed as in Fig. 30 with same colour codes.

The $\mathrm{SF}_{\mathrm{S}}$ contributions to the spin density along the two $\mathrm{N}-\mathrm{N}$ bonds of the azido groups are also woth of investigation. The spin density is large on $\mathrm{N} 1(\mathrm{~s}(\mathbf{r})=0.245$ a.u.) but then it decreases and turns out to be about two order smaller along the N1-N2 and N2-N3 internuclear axes. As displayed in the map of $\nabla^{2} \rho(\mathbf{r})$ (Fig. 27, right panel ), the bridging atom N 1 is the only one featured with a $\mathrm{sp}^{2}$-like hybridization, hence $\mathrm{s}(\mathbf{r})$ delocalizes through almost pure atomic p-orbitals on N 2 and N3 atoms; this clarifies the reason of why the spin density along the N1-N2 and N2-N3 bonds is so low. Note also (figure 33 and 34) : a) the large contributions to $s(\mathbf{r})$, along these bonds, from quite delocalized sources; b) the different roles of the central and terminal nitrogen atoms ${ }^{2}$ and $c$ ) the large and almost equal contributions from the two Cu atoms, which always promote the enhancement of the alpha spin density along the two bonds through an electron spin delocalization mechanism.

(a)

(b)

(c)

Fig. 33: Atomic $\mathrm{SF}_{\text {S }}$ percentages electron spin density reconstructions along the N1-N2 bond for the EO molecular system : at the N1 nucleus (a), at the bcp (b) and at the N2 nucleus (c). Atoms are portrayed as in Fig. 30 with same colour codes.

[^26]The spin density along the $\mathrm{Cu}-\mathrm{Cu}$ ' inter-nuclear axis, hence along the formally doubly occupied $\mathrm{d}_{\mathrm{xy}}$ bond, is negative on the Cu nucleus, then it turns slightly positive and, eventually, it quickly decays to about zero till the mid-point (see Fig. 35). The negative spin density on Cu nucleus (with different in sign $\mathrm{SF}_{\mathrm{S}}$ contributions from the Cu atom considered and from the other Cu atomic basin) is clearly explained by the maps of the Laplacian of the spin density, either in the plane of the azide ligands (Figure 27) and in the plane perpendicular to it and containing the metal centers (Figure 35) and taking into account the specific position of the reference point; then, as $\mathrm{s}(\mathbf{r})$ turns positive, the $\mathrm{SF}_{S}$ contributions from Cu atoms become the same sign back again. At midpoint, the spin density is negligibly small and the $\mathrm{s}(\mathbf{r})$ reconstruction in terms of $\mathrm{SF}_{\mathrm{S}}$ contributions is very delocalized with positive contributions from the two copper atoms (see Fig. 36).

(a)

(b)

(c)

Fig. 34: Atomic $\mathrm{SF}_{\text {S }}$ percentages electron spin density reconstructions along the $\mathrm{N} 2-\mathrm{N} 3$ bond for the EO molecular system. : at the N 2 nucleus (a), at the bcp (b) and at the N 3 nucleus (c). Atoms are portrayed as in Fig. 30 with same colour codes.


Fig. 35: (a) Electron spin density $\mathrm{s}(\mathbf{r})$ and (b) its Laplacian in the ( $\mathrm{z}, \mathrm{y}$ ) plane for symmetric EO di-nuclear copper azido bridged molecular system at UB3LYP/pob-TVPZ computational level. Atomic units (a.u.) are used throughout. Contour maps are drawn as in Fig. 27 with same colour codes.

Furthermore, it is worthy to note the substantial difference of the $\mathrm{SF}_{\mathrm{S}}$ contributions along this bond and along the one $\left(\mathrm{Cu}-\mathrm{N}_{\text {bridge }}\right)$ where spin delocalization occurs. Clearly, neither ferromagnetic coupling, nor spin delocalization occur through the $\mathrm{Cu}-\mathrm{Cu}$ ' internuclear axis and through their direct interaction (compare Fig. 27 with Fig. 35).

Considering the EE molecular system, about $64 \%$ of the unpaired electrons density is localized on the $\mathrm{Cu}(\mathrm{II})$ ions, slightly more than for the EO system (see spin atomic populations, Tab.16). The spin density population delocalized on the azide group is almost halved with respect to the EO system, while that on terminal ligands is increased (essentially, because for EE there is one more of them). A small negative spin density population is retrieved for the central nitrogen of the azido group.

(a)

(b)

(c)

Fig. 36: Atomic $\mathrm{SF}_{\mathrm{S}}$ percentages electron spin density reconstructions along the $\mathrm{Cu}-\mathrm{Cu}$ axis for the EO molecular system.: at the Cu nucleus (a); at $0.5 \AA$ from the Cu nucleus (b) and at the middle point along the $\mathrm{Cu}-\mathrm{Cu}$ axis (c).

Atoms are portrayed as in Fig. 30 with same colour codes.

The average beta effect for Cu atom is confirmed, being the integrated Laplacian of the spin density significantly positive. Such quantity, apart for the Cu atoms, is relevant only for the N 3 and N 4 atoms of the azido groups and for O1 (see Figure 40 a for the labels of atoms). The behaviour of the azide group N atoms closely resembles that of the corresponding N atoms in the E-O systems, taking into account that the N 3 atom in the EE system corresponds to the terminal azide N , because the shorter $\mathrm{Cu}-\mathrm{N}$ bond is formed with N 5 and the longer with N 3 .

| $\Omega$ | $\mathrm{q}(\Omega)$ | $\mathrm{s}(\Omega)$ | $\nabla^{2} \rho_{\alpha}(\Omega)$ | $\nabla^{2} \rho_{\beta}(\Omega)$ | $\nabla^{2} \mathrm{~s}(\Omega)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Cu | 1135 | +0.640 | +0.010 | -0.010 | +0.020 |
| N 1 | -0.890 | +0.084 | +0.000 | -0.002 | +0.002 |
| N 2 | -1078 | +0.075 | +0.000 | -0.000 | -0.001 |
| N 3 | -0.227 | +0.083 | +0.007 | -0.007 | +0.014 |
| N 4 | -0.134 | -0.004 | -0.007 | +0.007 | -0.013 |
| N 5 | -0.352 | +0.031 | -0.002 | +0.001 | -0.003 |
| N$)_{3}{ }^{-}$ | -0.713 | +0.110 | -0.002 | +0.001 | -0.003 |
| O 1 | -1074 | +0.070 | -0.003 | +0.003 | -0.006 |

Tab. 16: Atomic charges, electron spin populations, atomic Laplacians of electron spin density divided in $\alpha$ and $\beta$ counterparts and Atomic Laplacians of electron spin density in the EE molecular system and only for the atomic basins (copper and nitrogens) involved in the azido-bridge. All values are given in atomic units (a.u.).

Analogously to the EO system, in order to understand the spin density $\mathrm{SF}_{\mathrm{S}}$ contributions we must consider at first the aspherical $d$-electron distribution surrounding metal centers. In the EE system the Cu atom is five-fold coordinated in an almost square pyramidal arrangement of ligands. Once again, as for the EO system, the $\mathrm{d}_{\mathrm{x} 2-\mathrm{y} 2}$ orbital is the magnetic singly occupied orbital and the base of the pyramid corresponds to bonding with the three external ligand atoms ( $\mathrm{N} 1, \mathrm{~N} 2, \mathrm{O} 1$ ) and the N 5 atom of the azide group, in agreement with the crystal field theory and with a $d^{9}$ configuration on Cu atom (Fig.28b). The apical ligand N 3 , connected to the Cu by the longer $\mathrm{Cu}-\mathrm{N}$ bond is oriented approximatively along z (local coordinate system on the Cu ) and interacts with the almost doubly filled $\mathrm{Cu} \mathrm{d}_{22}$ orbital (providing so the reason why this bond is actually longer). As expected from orbital model and corraborated by the analysis of the Laplacian electron density, the CDs are found along Cu -dative bonds, with the Cu -ligand dative bonds of the base of the pyramid being greater than those retrieved along the apical bond. Moreover the CCs are accordingly located in between the ligands of the base pyramid. Another expected result was to find a relevant $\mathrm{s}(\mathbf{r})$ at the CD along the shorter $\mathrm{Cu}-\mathrm{N}$ azide bond ( $0.286 \mathrm{a} . \mathrm{u}$.) and a definitely smaller $\mathrm{s}(\mathbf{r})$ value $(\mathrm{s}(\mathbf{r})=0.005$ a.u.) at the CD of the longer, because of the single occupation of the $\mathrm{d}_{\mathrm{x} 2-\mathrm{y} 2}$ orbital and the almost double occupation of the $\mathrm{d}_{72}$ orbital. Indeed, the spin density at the CD along $\mathrm{Cu}-\mathrm{N} 5$ bond matches almost perfectly the one found for the bridging bond in the EO system, while the one along $\mathrm{Cu}-\mathrm{N} 3$ is two order of magnitude lower.


Fig. 37: Electron spin density $\mathrm{s}(\mathbf{r})$ and its Laplacian and Electron density Laplacian in the $\mathrm{Cu}-\mathrm{N} 5-\mathrm{O} 1$ plane for the asymmetric EE di-nuclear copper azido bridged molecular system at UB3LYP/pob-TVPZ computational levels Atomic units (a.u.) are used throughout. Contour maps are drawn as in Fig. 27 with same colour codes.


Fig. 38: Electron spin density $\mathrm{s}(\mathbf{r})$ and its Laplacian and Electron density Laplacian in the $\mathrm{Cu}-\mathrm{N} 3-\mathrm{O} 1$ plane for the asymmetric EE di-nuclear copper azido bridged molecular system at UB3LYP/pob-TVPZ computational level. Atomic units (a.u.) are used throughout. Contour maps are drawn as in Fig. 27 with same colour codes.

Comparing the spin density $\mathrm{SF}_{\text {S }}$ reconstructions at the CD along these two bonds (Fig. 39) brings further remarkable insights. In fact the $\mathrm{SF}_{\mathrm{S}}$ reconstruction along the $\mathrm{Cu}-\mathrm{N} 5$ bond is similar to the one of the $\mathrm{Cu}-\mathrm{N}_{\text {bridging }}$ bond in the EO system, while that for the $\mathrm{Cu}-\mathrm{N} 3$ bond is far different and endowed with much more delocalized sources. For both dative bonds, N3 atoms give a relevant contribution, enhancing the $\alpha$-spin density and the two metal centers also cooperate in such $\alpha$-spin density enhancement (see also the maps reported in Fig. 37 and Fig. 38).


Fig. 39: Atomic $\mathrm{SF}_{\mathrm{S}}$ percentages reconstructing the electron spin density at the $(3,+3) \mathrm{CD}$ along the $\mathrm{Cu}-\mathrm{N} 5$ (b) and the $\mathrm{Cu}-\mathrm{N} 3$ (c) bonds for the EE molecular system. Atoms are portrayed as in Fig. 30 with same colour codes.

The comparison of the reconstructions of $\mathrm{s}(\mathbf{r})$ in terms of $\mathrm{SF}_{\mathrm{S}}$ contributions for three similar reference points along the shorter and longer $\mathrm{Cu}-\mathrm{N}_{\mathrm{azi} \text { 栚 }}$ bonds, with the first point close to the spin density maximum nearby the Cu atom, the second located at the bcp and the third close to the N atom, reveals us that the shorter bond has definitely less delocalized sources (Fig. 40). ${ }^{\text {aa }}$ This holds true also at bcp but with the important difference that the two bonded atoms concur to enhance the bcp spin density for the longer bond, while have opposed contributions for the shorter $\mathrm{Cu}-\mathrm{N}$ bond as already found, discussed and interpreted for the Cu-N1 bond in the EO system. .


Fig. 40: Atomic $\mathrm{SF}_{\mathrm{S}}$ percentages reconstructing the electron spin density along the $\mathrm{Cu}-\mathrm{N} 5$ shorter bond of the EE molecular system: at the Cu nucleus (a), at the $\mathrm{Cu}-\mathrm{N} 5 \mathrm{bcp}$ (b) and at $0.05 \AA$ from N 5 nucleus (c). Atoms are portrayed as in Fig. 30 with same colour codes.

Finally, the analysis of the reconstruction of spin density in terms of $\mathrm{SF}_{\mathrm{S}}$ contributions along the two bonds of the azido group is discussed. Note first that the spin density on the N5 nucleus (Fig 41a) is only 0.063 a.u., to be compared with a value of about 5 times as big for the bridging $\mathrm{N}, \mathrm{N} 1$, in the EO system. As also shown by the far lower coupling constant, such behaviour denotes that in the EE system spin delocalization is less efficient than in the EO system.

[^27]
(a)

(b)

(c)

Fig. 41: Atomic $\mathrm{SF}_{\mathrm{S}}$ percentages reconstructing the electron spin density along the $\mathrm{N} 5-\mathrm{N} 4$ bond for the EE molecular system : at the N5 nucleus (a), at the N5-N4 bcp (b) and at the N4 nucleus(c). Atoms are portrayed as in Fig. 30 with same colour codes.

The role of N5 in the super-exchange mechanism is mediated through its influence on N4 and N3 and is thus less proficient. Actually, its spin distribution is shaped differently than the one of the bridging N in the EO system, while those of N 4 and N 3 atoms resemble more those of the corresponding N atoms in the EO system (compare Fig. 42 with Fig. 27).


Fig. 42: Electron spin density $s(\mathbf{r})$ and its Laplacian in the $\mathrm{Cu}-\mathrm{N} 3-\mathrm{N} 5$ plane for asymmetric EE di-nuclear copper azido bridged molecular system at UB3LYP/pob-TVPZ computational level. Atomic units (a.u.) are used throughout. Contour maps are drawn as in Fig. 27 with same colour codes.

Looking at the comparison between Fig. 41 (EE: N5-N4 bond) and Fig. 33 (EO: N1-N2 bond) , it is possible to note several common interesting features between the $\mathrm{SF}_{\mathrm{S}}$ reconstructions profiles along these two bonds. One may observe equal reconstructions at the N nucleus connected to Cu ( N 5 and N 1 , respectively), similar reconstruction patterns at the bcp but with much larger delocalization for the EE system, and a distinct reconstruction pattern nearby the central N ( N 4 and N 2 , respectively). The similar involvement from the two Cu atoms is confirmed, indicating a coupling between them realized through the azide non-innocent linker.. Similar considerations apply to the comparison
between the $\mathrm{SF}_{\text {S }}$ reconstructions profiles along the EE N4-N3 bond (Fig. 43) and the EO N2-N3 bond (Fig. 34)


Fig. 43: Atomic $\mathrm{SF}_{\mathrm{S}}$ percentages reconstructing the electron spin density along the N4-N3 bond for the EE molecular system.at the N4 nucleus (a), at the N4-N3 bcp (b) and at the N3 nucleus(c). Atoms are portrayed as in Fig. 30 with same colour codes.

Non-Innocent role of ligands in some Ni organometallic complexes as viewed through the Spin Density Source Function

Non-innocent metal ligand complexes are characterized by the ability to make the oxidation state of the central metal atom and the electronic structure of the ligands not a priori and unambiguously determined ${ }^{[24]}$. As showed by Cauchy et al in a study on the magnetic properties of a series of neutral $\mathrm{CpNi}(\text { dithiolene })^{\bullet}$ radical complexes ${ }^{[25]}$, even ligands that are classified as innocent may play a determinant role in the electron spin coupling phenomena. DFT $\boldsymbol{J}$ coupling constant calculations showed that spin density is strongly delocalized on the $\mathrm{NiS}_{2}$ moiety and, more importantly, up to $20 \%$ of $\mathrm{s}(\mathbf{r})$ is delocalized on the Cp rings. As a result, the intermolecular $\mathrm{Cp} \cdots \mathrm{Cp}$ and $\mathrm{Cp} \cdots$ dithiolene overlap interactions lead to anti-ferromagnetic couplings mediated by ligands that are commonly classified as innocent. In this subsection preliminary results regarding the reconstruction of spin density in terms of $\mathrm{SF}_{\mathrm{S}}$ applied on $\mathrm{CpNi}(\mathrm{adt})^{\bullet}$ radical complex (adt=acrylonitrile-2,3-dithiolate) (Fig. 44) are presented, to get insight on the factors that lead to ferro- or anti-ferro magnetic coupling behaviour in crystal and to quantitatively distinguish whether the ligands play a innocent or non-innocent role within these metal complexes. In table 17 are reported the values of atomic spin populations for all the atoms within molecular system $\mathrm{CpNi}(\mathrm{adt})^{\bullet}$. In table 18, these atomic spin populations are conveniently grouped to evince the contributions of the Ni , the dithiolene and the Cp moieties to the total spin population of the molecule. It is found that almost the $82 \%$ of $\mathrm{s}(\mathbf{r})$ is localized on the Ni atomic basin while, differently from the results of Cauchy et al, only the $11.5 \%$ of the spin density is delocalized on the Cp ligand and just the $6.5 \%$ is delocalized onto the dithiolene ligand.


Fig.44: adt $\mathrm{CpNi}(\text { dithiolene })^{\bullet}$ radical complex; $\nabla^{2} \rho(\mathbf{r})$ critical points are reported. The $\nabla^{2} \rho(\mathbf{r})$ critical points are denoted as follows: green points $(3,+3)$ charge concentrations $(C C)$, red points denote $(3,+1)$ saddle points, violet point $(3,-1)$ saddle points and orange point denote $(3,-3)$ charge depletions $(C D)$.

| $\Omega$ | $\mathrm{q}(\Omega)$ | $\mathrm{s}(\Omega)$ | $\nabla^{2} \rho_{\alpha}(\Omega)$ | $\nabla^{2} \rho_{\beta}(\Omega)$ | $\nabla^{2} \mathrm{~s}(\Omega)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ni1 | 1.1245 | 0.8192 | 0.0127 | -0.0123 | 0.0250 |
| S2 | 0.1266 | 0.0309 | -0.0026 | 0.0019 | -0.0046 |
| S3 | 0.0950 | 0.0325 | -0.0024 | 0.0020 | -0.0044 |
| C4 | -0.3280 | 0.0084 | -0.0004 | -0.0008 | 0.0003 |
| H5 | -0.1257 | 0.0003 | -0.0003 | 0.0003 | -0.0005 |
| C6 | -0.4295 | -0.0061 | -0.0007 | 0.0031 | -0.0038 |
| C7 | 1.0990 | 0.0032 | 0.0005 | -0.0010 | 0.0015 |
| C8 | 0.1355 | 0.0203 | -0.0015 | 0.0023 | -0.0038 |
| H9 | -0.1352 | 0.0012 | -0.0007 | 0.0007 | -0.0014 |
| C10 | 0.0670 | 0.0245 | 0.0025 | -0.0014 | 0.0039 |
| H11 | -0.1263 | 0.0002 | -0.0008 | 0.0008 | -0.0017 |
| C12 | 0.1659 | 0.0199 | -0.0035 | 0.0021 | -0.0056 |
| H13 | -0.1430 | 0.0016 | -0.0007 | 0.0007 | -0.0014 |
| C14 | 0.0692 | 0.0240 | 0.0011 | -0.0012 | 0.0023 |
| H15 | -0.1194 | 0.0003 | -0.0008 | 0.0008 | -0.0016 |
| C16 | 0.1018 | 0.0223 | -0.0004 | 0.0014 | -0.0018 |
| H17 | -0.1294 | 0.0009 | -0.0008 | 0.0008 | -0.0016 |
| N18 | -1.4463 | -0.0036 | -0.0004 | 0.0004 | -0.0008 |

Tab. 17: Atomic charge, electron spin populations, atomic Laplacians of electron spin density divided in $\alpha$ and $\beta$ counterparts and atomic Laplacians of electron spin density for each atoms within adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex. All values are given in atomic units (a.u.).

The spin population of the two sulfur atoms is slightly different (almost the $3.3 \%$ of the unpaired electron is delocalized on S 3 and slightly less, $3.1 \%$, on S 2 ). The difference is not due to a relevant structural difference between Ni-S2 $(2.131 \AA)$ and $\mathrm{Ni}-\mathrm{S} 3(2.132 \AA)$ bonds, rather it might be due to a non symmetric delocalization of the spin density on the dithiolene ligand because of the terminal -

CN group or, more likely, to the higher, by about $0.03 \mathrm{e}^{-}$, electron population, of S3 (S3: 31.905 $\mathrm{e}^{-}$ and S2: $31.873 \mathrm{e}^{-}$). The non negligible spin population on the S atoms reveals the non-innocent nature of the dithiolene ligand and highlights its capability to influence the oxidation state of the metal center in radical metal complexes.

|  | $\mathrm{q}(\Omega)$ | $\mathrm{s}(\Omega)$ | $\% \mathrm{~s}(\Omega)$ |
| :---: | :---: | :---: | :---: |
| Ni1 | 1,12 | 0,82 | 81,92 |
| Dithiolene | $-1,01$ | 0,07 | 6,55 |
| Cp | $-0,11$ | 0,12 | 11,53 |

Tab. 18: Atomic charge, electron spin population and electron spin population percentage for the Ni metal and both the ligands within adt $\mathrm{CpNi}(\text { dithiolene })^{\bullet}$ radical complex. All values are given in atomic units (a.u.).

On the other hand, in the case of Cp ligand the rationale behind differences in the spin density delocalization might be different. In fact spin population values show that almost the $2.5 \%$ of the unpaired electron distribution is delocalized on the C 10 atomic basin, a value quite similar to that delocalized on C14 (2.4\%) but larger than that delocalized on the C8 and C12 atoms (both around $2.0 \%$ ). The behaviour of $\mathrm{s}(\mathbf{r})$ in this case is mirrored by structural differences in terms of distances. In fact the Ni-C10 distance $(2.078 \AA)$ is very similar to the Ni-C14 one $(2.076 \AA)$ while it is different from the $\mathrm{Ni}-\mathrm{C} 8$ and $\mathrm{Ni}-\mathrm{C} 12$ distances, which are both somewhat longer (respectively $2.107 \AA$ and $2.112 \AA$ ). However, one should also note that larger spin populations correspond to larger electron populations (C10: 5.933; C14: 5.931; C8: 5.865; C12: 5.834). So, as in case of adt ligand, also the Cp ligand is non innocent. The analysis of the reconstructions of $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ in terms of SF and $\mathrm{SF}_{\mathrm{S}}$ contributions respectively reveals how the latter sources are more delocalized than the former within the whole molecule. The set of analysed reference points, along with their electron density and spin densitiy properties is collected in Table 19, whereas Fig. 44 illustrates pictorially their locations in the molecule. Interestingly, the application of $\mathrm{SF}_{S}$ permit us to distinguish the mechanism of the transmission of $\mathrm{s}(\mathbf{r})$ within the molecule; in fact it is possible to observe how $\mathrm{s}(\mathbf{r})$ is delocalized on the adt ligand through the covalent Ni-S bonds [see the reconstructions of $s(\mathbf{r})$ at lap7 and lap4 (Table 19), which are taken as reference points in Fig. 46 and 47]; this is not the case of Cp ligand where the spin density appears to be delocalized through space, via the $\pi$ framework of the ligand. Furthermore the application of $\mathrm{SF}_{\mathrm{S}}$ permits us to show in a quantitative way how $\mathrm{s}(\mathbf{r})$ is delocalized onto the Cp ligand; in this sense $\mathrm{SF}_{\mathrm{S}}$ is able to quantify how much a ligand is innocent or not. In the $\mathrm{CpNi}(\mathrm{adt})$ complex, the Cp ligand gives a $\beta$ effect to the delocalization of $\mathrm{s}(\mathbf{r})$ onto the Ni CD (lap7) and onto the adt ligand CC (lap 4) and a contribution to the spin density at lap7 (which lies onto Ni1-S2 bond) very similar with respect to the adt ligand $\left(\mathrm{SF}_{\mathrm{S}}(\mathrm{Cp}) \%=14.1\right.$ vs $\left.\mathrm{SF}_{\mathrm{S}}(\mathrm{adt}) \%=14.6\right)$.

|  | TYPE | $\rho(\mathbf{r})$ | $\mathrm{s}(\mathbf{r})$ | $\nabla^{2} \rho(\mathrm{r})$ | $\nabla^{2} \mathrm{~s}(\mathbf{r})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Lap1 | $(3,1)$ | $1,81 \mathrm{E}-01$ | $2,99 \mathrm{E}-03$ | $-3,52 \mathrm{E}-02$ | $-1,63 \mathrm{E}-02$ |
| Lap2 | $(3,-1)$ | $1,72 \mathrm{E}-01$ | $2,55 \mathrm{E}-03$ | $4,31 \mathrm{E}-02$ | $-1,78 \mathrm{E}-02$ |
| Lap3 | $(3,-1)$ | $1,76 \mathrm{E}-01$ | $1,60 \mathrm{E}-03$ | $6,94 \mathrm{E}-02$ | $-5,74 \mathrm{E}-03$ |
| Lap4 | $(3,3)$ | $1,64 \mathrm{E}-01$ | $1,81 \mathrm{E}-03$ | $-3,70 \mathrm{E}-01$ | $-1,08 \mathrm{E}-02$ |
| Lap5 | $(3,3)$ | $1,44 \mathrm{E}-01$ | $1,27 \mathrm{E}-03$ | $-3,02 \mathrm{E}-01$ | $-5,73 \mathrm{E}-03$ |
| Lap6 | $(3,-1)$ | $1,52 \mathrm{E}+00$ | $2,97 \mathrm{E}-01$ | $1,27 \mathrm{E}+01$ | $-3,64 \mathrm{E}+00$ |
| Lap7 | $(3,-3)$ | $1,59 \mathrm{E}+00$ | $-1,16 \mathrm{E}-02$ | $1,39 \mathrm{E}+01$ | $1,68 \mathrm{E}+00$ |
| Lap8 | $(3,1)$ | $4,59 \mathrm{E}+00$ | $9,05 \mathrm{E}-01$ | $-3,18 \mathrm{E}+01$ | $-4,13 \mathrm{E}+01$ |
| Lap9 | $(3,1)$ | $1,97 \mathrm{E}-01$ | $8,86 \mathrm{E}-04$ | $-5,08 \mathrm{E}-02$ | $-5,31 \mathrm{E}-03$ |
| lap10 | $(3,-1)$ | $1,60 \mathrm{E}-01$ | $7,28 \mathrm{E}-04$ | $8,13 \mathrm{E}-02$ | $-2,85 \mathrm{E}-03$ |
| lap11 | $(3,1)$ | $1,97 \mathrm{E}-01$ | $-9,27 \mathrm{E}-04$ | $-1,91 \mathrm{E}-01$ | $5,77 \mathrm{E}-03$ |
| lap12 | $(3,-1)$ | $1,80 \mathrm{E}-01$ | $-6,52 \mathrm{E}-04$ | $-2,30 \mathrm{E}-02$ | $3,06 \mathrm{E}-03$ |

Tab. 19: Electron density, electron spin density, Laplacian of $\rho(\mathbf{r})$ and Laplacian of $\mathrm{s}(\mathbf{r})$ for the selected $\nabla^{2} \rho(\mathbf{r})$ reference points in adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex (see Fig. 44). All values are given in atomic units (a.u.).

The analysis of the reconstruction of $\mathrm{s}(\mathbf{r})$ at CD along the $\mathrm{Ni}-\mathrm{S} 2$ bond in terms of $\mathrm{SF}_{\mathrm{S}}$ contributions from the magnetic part of the wave function and from the remaining (relaxation) part of it (relaxation term), allows us to get some more insight on the mechanisms of spin transmission within the molecular system.


Fig. 45: Electron density, spin density and Laplacian of $\mathrm{s}(\mathbf{r})$ in the $\mathrm{Ni}-\mathrm{S} 2-\mathrm{S} 3$ plane for adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex at UHF/pob-TVPZ computational levels. Atomic units (a.u.) are used throughout. Contour maps $\beta$ drawn as in Fig. 27 with same colour codes.

An $\alpha$, positive contribution to the spin density is expected and found from the single occupied atomic orbital of the Ni atomic basin (see Fig. 45b), while a negative contribution to the reconstruction of $s(\mathbf{r})$ is expected from the relaxation molecular orbitals due to polarization effects (see Fig. 45c). In terms of percentage contribution values, $\mathrm{SFs} \%$, these contributions from the Ni atom will be instead negative ( $-136.3 \%$ ) and positive ( $210 \%$ ) , respectively, as they oppose and
concur to the negative value of $s(\mathbf{r})$ at the CP lap 7. The percentage contribution to $s(\mathbf{r})$ given by the magnetic orbital is negative for the Ni atomic basin ( $\alpha$ effect), while it is positive for the ligands, both giving a $\beta$ effect. On the contrary, when the relaxation contributions to the spin density are considered, the metal center contributes with a positive value of $\mathrm{SF}_{\mathrm{S}}$ percentage, while both the ligands oppose to the globally negative value of $s(\mathbf{r})$ at the reference point. This is a clear effect of a spin polarization mechanism driving the electron spin density information transmission at CP lap 7.


Fig. 46: Atomic $\mathrm{SF}_{\text {s }}$ percentages at the CD lap 7 (Table 17 and Fig. 44) on the Ni1-S2 bond, as evaluated from (a) the total density, (b) the magnetic orbital and (c) the non-magnetic natural orbitals densities for adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex. Atoms are portrayed as spheres with volumes proportional to their source percentage contributions to $s(\mathbf{r})$ values at the critical points considered. Colour codes: green or red whether atoms represent positive ( $\alpha$ effect) or negative ( $\beta$ effect) sources for $s(\mathbf{r})$ at critical point considered. On the left is reported 3 D isosurface of $\mathrm{s}(\mathbf{r})$ at the value recovered at the CP considered.

The reconstruction of $\mathrm{s}(\mathrm{r})$ in terms of $\mathrm{SF}_{\mathrm{S}}$ contributions given by the magnetic singly occupied natural orbital and by the reaction or relaxation molecular orbitals, highlights how, as in the case of the ${ }^{3} \mathrm{~B}_{1}$ water triplet, the relaxation term essentially counteracts the contributions given by the magnetic orbital to the reconstruction of $\mathrm{s}(\mathbf{r})$ at the CC along the $\mathrm{Ni}-\mathrm{S} 2$ bond (Fig. 47). At this reference point the spin density is small and positive ( 0.0018 a.u.) and dominated by the overwhelming $\alpha$ contribution from Ni. The Cp ligand yields an overall $\beta$ effect (SFs\% = -57.3), opposing to such positive density with a global contribution which is almost ten times larger in magnitude than that given by the adt ligand ( $\mathrm{SFs} \%=-6.3$ ). In fact, in the case of the adt ligand the contribution from the $\beta$-effect due to the magnetic orbital is almost compensated for by the $\alpha$-effect brought in by the relaxation natural orbitals, while for the Cp ligand the global $\beta$-effect due to the magnetic orbital largely superceeds the small overall $\alpha$-effect caused by the relaxation natural orbitals.

Fig. 47: Atomic SF $_{\text {S }}$ percentages at the CC lap 4 (table 17 and Fig. 44) on the Ni1-S2 bond as evaluated from (a) the total density, (b) the magnetic natural orbital and (c) the non-magnetic natural orbital densities for adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex. Atoms are portrayed as in Fig. 45 with same colour codes. On the left is reported 3D isosurface of s(r) at the value recovered at the CP considered.

The reconstruction of $\mathbf{s}(\mathbf{r})$ at CP lap7 and CP lap 4 identifies two different mechanisms for spin information transmission. The main and overdetermining contribution to the positive spin density at the CC reference point is given by the Ni atom and by the magnetic natural orbital, localized principally on the $\mathrm{Ni}^{7}$ metal, with Cp partly opposing to such density and with adt playing only an almost neglible role. In the case of the negative spin density at the CP lap 7 reference point, it is still the Ni atom which gives the largest dominant contribution, (in this case a $\beta$-effect ) but this now it is the result of the dominance of the relaxation orbitals contribution over the opposing contribution from the magnetic orbital. The Cp and the adt ligands, in this case, slightly concur to the spin density at the CP , rather than opposing to it as it was in the case of reconstruction of the CP lap4 electron density.

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## GENERAL

## REMARKS AND <br> CONCLUSIONS:

The main purpose of this PhD thesis was the application of novel QTAIM-based chemical descriptors to different chemical problems. In particular, we performed a thorough experimental and theoretical study on a suitable test case to understand how electron delocalization in a conjugated system might be affected by the electric field due to strong crystal field effects (Chapter 1). We also succeeded in disentangling on a quantitative basis the various ways through which spin information is transmitted from one magnetic centre to another (Chapter 2).

In Chapter 1, we showed that local and non-local topological descriptors can be employed to understand which are the correlations between structure, electron delocalization and crystal field polarization effects. To this end, we obtained the charge density distribution of 3-diethylamino-4-(4-methoxyphenyl)-1,1-dioxo-4H-1 $\lambda^{6}, 2$-thiazete-4-carbonitrile (DTC) by both single-crystal Xray diffraction at $T=100(2) \mathrm{K}$ and quantum mechanical simulations. DTC is a synthetic compound that exhibits a significant similarity with $\beta$-sultamic drugs and its core moiety is a very rare $4-$ membered thiazete-1,1-dioxide heterocycle. Former analysis of DTC and of some structurally analogue compounds revealed that the single $\mathrm{C}-\mathrm{N}$ bond conjugated to the 4 -membered thiazete1,1 -dioxide heterocycle is shorter than the double $\mathrm{N}=\mathrm{C}$ bond within the ring. We found that this unusual and counterintuitive bond length alternation pattern is the consequence of a significant electronic rearrangement within the molecule. Indeed, there is a significant enhancement of the incrystal DTC dipole moment with respect to the in vacuo relaxed structure. We demonstrated that this enhanced polarization is due to both an increase of the charge transfer and a reduction in the magnitude of the atomic polarization term. However, the charge transfer contribution is the dominating one, i.e. the charge separation among bonded atoms significantly increases in the bulk. Since DTC does not show strong directional hydrogen bond networks, its packing is clearly dominated by electrostatics. As a consequence, the high in-crystal electric field due to cooperative alignment of the molecular dipoles enhances the charge separation through the molecule, increasing the importance of quantum states associated to highly polar resonance forms. At the same time, such an enhanced polarity reinforces the crystal field in a sort of positive feedback fashion, influencing the conjugated pattern until the formally $\mathrm{N}=\mathrm{C}$ double bond of the thiazete ring becomes longer than the adjacent, formally single, $\mathrm{C}-\mathrm{N}$ one.
DTC represents an interesting test case to understand the subtle interplay between crystal field effects and changes in the molecular structure. Methods that intrinsically neglect quantum effects (such as force fields methods) should be parametrized ad hoc to accurately describe crystalline matrix effects in the presence of strongly polarizable system, especially if the final goal is to predict crystal structures. Finally, it is worth noting that our joint theoretical and experimental approach allowed us to detect and rationalize even subtle and counterintuitive effects, even though it clearly lacks predictability. Anyhow, comparison with accurate single-crystal X-ray structures and
experimentally-derived charge densities is mandatory to improve accuracy and reliability of computational recipes for in silico modelling of crystalline materials.
In chapter 2 a new topological tool for the analysis of the electron spin density distribution $\mathrm{s}(\mathbf{r})$ in magnetic molecular systems based on QTAIM is presented. Such chemical descriptor is the Source Function for the spin density $\left(\mathrm{SF}_{\mathrm{S}}\right)$. Analogously to the case of the reconstruction of electron density $\rho(\mathbf{r})$ in terms of source function (SF) contributions for the electron density, the spin density source function $\left(\mathrm{SF}_{S}\right)$ reconstructs the electron spin density at a reference point in terms of separate atoms or group of atoms contributions. The large anisotropy of $s(\mathbf{r})$ and of $\nabla^{2} s(\mathbf{r})$ distributions within atomic basins makes the reconstruction of spin density strongly dependent on the choice of the reference point considered. Hence it may result that the spin density at a determined reference point be almost fully determined by the atomic basin to which the point belongs to as, for example, it occurs in the water triplet molecular system $\left({ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}\right)$ at the saddle points 4 and $4^{\prime}$ associated to the unpaired electrons in $\mathrm{O}\left(\mathrm{p}_{\mathrm{z}}\right)$ atomic orbital. But the opposite situation may also realize and even so in the case of reference points lying within the basin of the paramagnetic center, like for the case of the charge concentration maximum associated to the O atom lone pair in water triplet, when only the limited electron correlation enabled by the UHF model is included. The very low positive spin density value found at this point, lying only $0.33 \AA$ far away from the oxygen and on opposite side with respect to the hydrogen atoms, is even overdetermined $\left(\mathrm{SF}_{\mathrm{s}}\left(\mathrm{H}+\mathrm{H}^{\prime}\right) \%=108\right)$ by the two distant H atoms. The comparison between $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ reconstructions in terms of SF and $\mathrm{SF}_{\mathrm{S}}$ is illuminating about the different way the information about these scalar functions is transmitted. Furthermore, by comparing the transmission patterns at different reference points, further insight is gained on how such observables are transmitted as a function of the considered reference point.
Chemical interpretation of the $\mathrm{SF}_{S}$ atomic contributions is largely augmented when they are decomposed in a magnetic term due to the magnetic natural orbital(s) density and in a reaction or relaxation term due to the remaining natural orbitals density. Such a decomposition sheds also light on the causes leading to incorrect spin density distributions from low-level wavefunctions. As mentioned earlier, at the UHF level, the contribution given by the oxygen atomic basin to the spin density at the charge concentration (CC) associated to the lone pair is not dominant; such counterintuitive result disappears when electron correlation effects are introduced ( $\operatorname{CASSCF}(8,8)$ level of theory). The latter leave almost unaffected the O and H atoms magnetic contributions to the spin density at the lone pair CC , while they selectively increase the O relaxation contribution by one order of magnitude relative to the UHF model. In general, we could show that the magnetic term of the electron density is already well described and similar to that of an adequate CASSCF model, even in the case of UHF or ROHF wavefunctions. The introduction of electron correlation effects in the wavefunction evaluation has instead a noticeable effect on the reaction or relaxation molecular
orbitals, and particularly so in specific molecular regions, where the effect of relaxation is particularly high.

Interestingly it has been shown that the magnetic term can, in some case, cause a decrease of the local spin density ( $\beta$-effect), rather than determining a positive spin density at any reference point. Considering the relaxation term, it can either concur or counteract the magnetic term in determining the spin density at a given point, regardless its link to an orbital density integrating to a null spin population over the whole space. In fact, the SFs atomic contributions and their magnetic and reaction components, are all obtained through the atomic integration of the corresponding local source functions, which are given in terms of the related spin density Laplacians. We have shown that these latter may be locally positive or negative depending on the local concentration/dilution of the corresponding $\alpha$ - and $\beta$-densities, and independently from the sign of $s(\mathbf{r})$.

The perfect transferability of both the electron density and the electron spin density has been demonstrated to occur in a n-alkyl radicals series, as it was shown before for the case of the electron density in the corresponding $n$-alkanes. An almost perfect transferability for the spin density is also achieved at the terminal C-H bond bcp, despite its very low $\mathrm{s}(\mathbf{r})$ value, and through a combination of opposing $\alpha$ and $\beta \mathrm{SF}_{\mathrm{S}}$ cumulative effects of similar magnitude. Perfect transferability for the electron and the electron spin densities realizes in quite different ways and largely dependent on the selected reference point.

The spin density source function has also been applied to molecular systems in crystals, namely the $\mathrm{Cu}(\mathrm{II})$ azido and the $\mathrm{Ni}(\mathrm{II})$ dithiolene complexes. Concerning the former, we have considered two double azido bridged di-nuclear $\mathrm{Cu}(\mathrm{II})$ complexes in different structural configuration (End-End, EE, against End-On, EO, molecular structures). In both EO and EE systems, the bridge may be both symmetric when the two $\mathrm{N}-\mathrm{Cu}$ bonds are equivalent and short or asymmetric when the two $\mathrm{N}-\mathrm{Cu}$ bonds differ in distance. In general EO systems are symmetric while EE systems are asymmetric and, from a magnetic point of view, the EO coordination provides ferromagnetic $\mathrm{Cu}-\mathrm{Cu}$ interactions, while the magnetic interactions are null or weakly antiferromagnetic in the asymmetric EE systems even if it is possible to observe a ferromagnetic interaction in some cases. On the contrary, the few di-nuclear Cu (II) EE symmetric systems are strong anti-ferromagnetic in nature, with a very large coupling constant. The two double azido bridged di-nuclear Cu (II) metal complexes presented as examples in chapter 2, show ferromagnetic coupling between the two metal centers within the molecule and, as revealed by the comparison of atomic spin populations, the unpaired electrons density is slightly more localized on the $\mathrm{Cu}(\mathrm{II})$ ions in the EE than the EO molecular system while the delocalization of the unpaired electrons on the azide group is almost
halved in EE, relative to the EO system. In general for both the metal complexes the atomic spin density is relevant only on the metal centers and on the nitrogen atomic basins of the azido groups. More importantly, the corresponding azide nitrogen atoms of both EE and EO structures in the azido group have almost the same behaviour. In fact the spin density at the charge depletion (CD) along the shorter $\mathrm{Cu}-\mathrm{N} 5$ bond in EE molecular system matches almost perfectly with the corresponding one for the bridging $\mathrm{Cu}-\mathrm{N}$ bond in the EO system, while the one along the much longer $\mathrm{Cu}-\mathrm{N} 3$ bond is two order of magnitude lower. Comparing the spin density $\mathrm{SF}_{\mathrm{S}}$ reconstructions at the CD along these two bonds brings further remarkable insights. In fact the $\mathrm{SF}_{\mathrm{S}}$ reconstruction along the $\mathrm{Cu}-\mathrm{N} 5$ bond is similar to the one of the $\mathrm{Cu}-\mathrm{N}_{\text {bridging }}$ bond in the EO system, while that for the $\mathrm{Cu}-\mathrm{N} 3$ bond is far different and endowed with much more delocalized sources. For both dative bonds, N3 atoms give a relevant contribution, enhancing the $\alpha$-spin density and the two metal centers also cooperate in such $\alpha$-spin density enhancement. Moreover in case of EE molecular system the Cu spin density is not elongated along $\mathrm{Cu}-\mathrm{N} 3$ bond. The comparison of the reconstructions of $s(\mathbf{r})$ in terms of $\mathrm{SF}_{\mathrm{S}}$ contributions for three similar reference points along the shorter $\mathrm{Cu}-\mathrm{N} 5$ bond in EE and for the $\mathrm{Cu}-\mathrm{N}_{\text {azide }}$ bond in EO molecular system shows that the spin density on the N 5 nucleus is only 0.063 a.u. to be compared with a value about 5 times as large at the nucleus of the bridging N in the EO system. Such behaviour highlights a stronger magnetic interaction between the two Cu atoms in the EO system relative to the EE system, as also evidenced by the far lower coupling constant in the latter. In the EE system, differently from the $\mathrm{N}_{\text {bridge }}$ in the EO complex, the role of N5 in the super-exchange mechanism is mediated through its influence on N4 and N3 atoms and is thus less efficient. Actually, its spin distribution is shaped differently than the one of the bridging N in the EO system, while those of N 4 and N 3 atoms resemble more those of the corresponding N atoms in the EO system. The $\mathrm{SF}_{\mathrm{S}}$ reconstructions obtained on the two Cu azide complexes should be considered as preliminary results. Indeed, we expect that the decomposition of $\mathrm{SF}_{\mathrm{S}}$ contributions in magnetic and relaxation terms, as we have successfully proposed for the simpler case of the water triplet, may largely enhance the chemical interpretation of the SF patterns for these complexes.
Finally, in chapter 2, the ability of non-innocent ligands to make the oxidation state of the central metal atom not a priori and unambiguously determined is analyzed through the use of the $\mathrm{SF}_{\mathrm{S}}$ topological tool. To this aim the neutral $\mathrm{CpNi}(\mathrm{adt})^{\bullet}$ (adt=acrylonitrile-2,3-dithiolate) radical complex is chosen. This metal complex is quite interesting since, as showed by Cauchy et al, both its ligands play a determinant role in the electron spin coupling phenomena. DFT $\boldsymbol{J}$ coupling constant calculations showed that spin density is strongly delocalized on the $\mathrm{NiS}_{2}$ moiety and, more importantly, up to $20 \%$ of $\mathrm{s}(\mathbf{r})$ is delocalized on the Cp rings. As a result, the intermolecular $\mathrm{Cp} \cdots \mathrm{Cp}$ and $\mathrm{Cp} \cdots$ dithiolene overlap interactions in the crystal lead to anti-ferromagnetic couplings mediated
by ligands that are commonly classified as innocent. In chapter 2 preliminary results regarding the reconstruction of spin density in terms of $\mathrm{SF}_{\mathrm{S}}$ applied on $\mathrm{CpNi}(\mathrm{adt})^{\bullet}$ radical complex are presented. As expected, almost the $81.9 \%$ of $\mathrm{s}(\mathbf{r})$ is localized on the Ni atomic basin while, differently from the results of Cauchy et al, only the $11.5 \%$ of the spin density was found to be delocalized on the Cp ligand and just the $6.5 \%$ delocalized onto the dithiolene ligand. In the case of the Cp ligand, the spin density is not equally delocalized onto the five carbon atomic basins. Such behaviour of $\mathrm{s}(\mathbf{r})$ on the Cp ligand is linked to structural differences in terms of distances and electron populations. The analysis of the reconstructions of $\rho(\mathbf{r})$ and $\mathrm{s}(\mathbf{r})$ in terms of SF and $\mathrm{SF}_{S}$ contributions reveals how $s(\mathbf{r})$ sources are much more delocalized within the whole molecule with respect to those for $\rho(\mathbf{r})$. The application of the $\mathrm{SF}_{\mathrm{S}}$ analysis allows to distinguish the mechanism of transmission of $\mathrm{s}(\mathbf{r})$ within the molecule. In particular $\mathrm{s}(\mathbf{r})$ is delocalized on the adt ligand through the covalent $\mathrm{Ni}-\mathrm{S}$ bonds, while in the case of Cp ligand it is delocalized through space, by exploiting the $\pi$-orbital framework of the Cp ligand (which is an obvious result since the latter interacts with the Ni atom using such framework). Application of $\mathrm{SF}_{\mathrm{S}}$ permits us to show in a quantitative way how $\mathrm{s}(\mathbf{r})$ is delocalized onto the Cp ligand; in this sense $\mathrm{SF}_{\mathrm{S}}$ is able to quantify how much a ligand is innocent or not. The reconstruction of $\mathrm{s}(\mathbf{r})$ along the bond of Ni with the dithiolene ligand ( $\mathrm{Ni}-\mathrm{S} 2$ bond) identifies two different mechanisms for spin information transmission, depending on the selected reference point. The main and overdetermining contribution to the positive spin density at the bonded charge concentration (CC) reference point is given by the Ni atom and by the magnetic natural orbital, localized principally on the $\mathrm{Ni}^{7}$ metal, with the Cp ligand partly opposing to such density and with adt playing only an almost neglible role. In the case of the negative spin density at the charge depletion (CD) CP , close to the Ni atom, it is again the Ni atom which gives the largest dominant contribution (in this case a $\beta$-effect) but this now it is the result of the dominance of the relaxation orbitals contribution over the opposing contribution from the magnetic orbital. The Cp and the adt ligands, in this case, slightly concur to the spin density at the CP , rather than opposing to it as it was in the case of reconstruction at the CC critical point.

## APPENDIX A1

## A1. Experimental procedures: full discussion

A1.1 Specimens. We were provided with the original batch of the microcrystalline title compound by prof. F. Clerici, in 2002. The synthetic procedure have been reported in details in another paper. ${ }^{[1]}$ The formerly described X-ray analysis was performed with a good-quality selected crystal (hereinafter, sample \#1). ${ }^{[1]}$ Such crystal had been then preserved within a cupboard in the dark for $\approx$ 6 years, during which no significant deterioration of the diffraction intensities had occurred, as shown by preliminary X-ray data collections performed at RT on sample \#1 in 2008. During the same year, new crystallization tests had been also performed, with the purpose of getting higherquality crystals to employ in the experimental charge density investigation. Several solvents were tested, and slow evaporation from $n$-hexane ( 8 days) at room temperature provided some fitting specimens: one of them (hereinafter, sample \#2) was then elected for the current study (Table A1, Fig. A1).

## A1.2 X-ray diffraction.

The X-ray data collections were all lead in 2008-2009, by graphite-monochromated Mo $\mathrm{K} \alpha$ radiation $(\lambda=0.71073 \AA$ ) at the same nominal source power of $50 \mathrm{kV} \times 30 \mathrm{~mA}$, employing a threecircle Bruker SMART APEX II goniometer set with a CCD area detector and an Oxford Cryostream $\mathrm{N}_{2}$ gas blower. All data reductions were performed by The SAINT program package ${ }^{[2]}$.


Figure A1. Crystals \#1 (a) and \#2 (b) employed in the present analysis (see text). One small division on the scale corresponds to 0.025 mm .

In the beginning, we selected the larger \#1 specimen (Table A1, Figure A1a) for the low- $T$ data collection; namely, it was cooled down to $T=100 \mathrm{~K}$ under a $2 \mathrm{~K} / \mathrm{min}$ temperature gradient. Despite an overall $3.2 \%$ shrinkage of the cell volume, the temperature did not cause any structural changes. A total of $23 \omega$-scans ( 0.5 deg/frame, sweep 180 deg ) at fixed $\varphi$ and detector angles were identifyed at $T=100 \mathrm{~K}$, resulting in a $99.6 \%$ complete sphere of data up to a maximum resolution of $\sin \vartheta / \lambda=$ $0.9 \AA^{-1}$. We carefully screened the recorded frames, so not to include individual measures biased by
the shadows of the beamstop and/or of the cryostat nozzle. Deeply investigating the reciprocal lattice at 100 K , we detected weak off-lattice spots, caused by a minor epitaxial non-merohedral twin component of the same DTC polymorph. The data analysis executed by TWINABS ${ }^{[3]}$ revealed that the mass ratio of the parasite crystal was as low as $3.7 \%$ on the basis of several measures of strong reflections having equal indices between the two contrarily directed phases. At the same time, the value of the fraction of overlapped (and possibly problematic) reflections was expected to be as low as $\approx 15 \%$. Despite the accurate molecular structure could be obtained by easily treating the minor twinning of crystal \#1 in the beginning, we rather deleted partially overlapped reflections caused by the parasite crystal, since performing high-quality charge density studies requires an unbiased (or the least biased as possible) dataset. ${ }^{[4]}$ Note that the quality of the sample (in particular the low-order reflections one) may remarkably influence the point topological descriptors and specific qualities of the charge density distribution in the covalent bonds area. ${ }^{[4]}$

Table A1 Data collection statistics and relevant refinement details for the three 100 K datasets of the same 'A' polymorph of DTC $\left(\mathrm{C}_{14} \mathrm{H}_{17} \mathrm{~N}_{3} \mathrm{O}_{3} \mathrm{~S}\right.$, molecular weight $307.37 \mathrm{~g} \mathrm{~mol}^{-1}$, space group $\left.\mathrm{P} 2_{1} / \mathrm{n}, \mu=0.234 \mathrm{~mm}^{-1}, \mathrm{~F}_{000}=648 e\right)$.

| Crystal data | Sample \#1 | Sample \#2 | $F_{\text {exp }}$ |
| :---: | :---: | :---: | :---: |
| $a$ ( $\AA$ ) | 8.5395(3) ${ }^{\text {a }}$ | $8.5447(2){ }^{\text {b }}$ | 8.5421(26) ${ }^{\text {c }}$ |
| $b$ ( $\AA$ ) | $13.2383(4)^{\text {a }}$ | $13.2396(3){ }^{\text {b }}$ | 13.2390(6) ${ }^{\text {c }}$ |
| $c(\AA)$ | 13.0403(4) ${ }^{\text {a }}$ | 13.0483(3) ${ }^{\text {b }}$ | $13.0443(40)^{\text {c }}$ |
| $\beta$ (deg) | 95.105(2) ${ }^{\text {a }}$ | $95.053(1)^{\text {b }}$ | 95.079(26) ${ }^{\text {c }}$ |
| $V\left(\AA^{3}\right)$ | 1468.34(12) ${ }^{\text {a }}$ | 1470.39(7) ${ }^{\text {b }}$ | $1469.37(35){ }^{\text {c }}$ |
| Density ( $\mathrm{g} \cdot \mathrm{cm}^{-3}$ ) | 1.390 | 1.388 | 1.389 |
| Crystal size (mm) | $0.43 \times 0.33 \times 0.25$ | $0.23 \times 0.20 \times 0.13$ | // |
| Data collection $\left(\sin \vartheta / \lambda_{\text {MAX }}\right)=0.65 \AA^{-1} / 0.90 \AA^{-1}$ |  |  |  |
| Measured reflections | 39988 / 110586 | 46902 / 118397 | 86720 / 157389 |
| Unique reflections | 3365 / 8940 | 3376 / 8984 | 3375 / 8956 |
| $I>2 \sigma(I)$ reflections | 3128 / 7742 | 2962 / 6917 | 3117 / 7688 |
| Completeness (\%) | 99.7 / 99.6 | 100.0 / 100.0 | 100.0 / 99.7 |
| $R_{\text {int }}$ | 0.0217 / 0.0345 | $0.0496 / 0.0845$ | $0.0397 / 0.0441$ |
| Refinement |  |  |  |
| $R(F)$, wR( $F^{2}$, | 0.0300, 0.0800, | 0.0355, 0.0866, | 0.0297, 0.0798, 0.999 |
| Goodness-of-fit ${ }^{\text {d }}$ | 0.992 | 1.035 | 0.0168, 0.0290, 1.099 |
| $\Delta \rho_{\min }, \Delta \rho_{\max } \quad\left(\mathrm{e} \AA^{-3}\right)$, data-to-parameters ratio ${ }^{4}$ | $\begin{array}{ll} -0.340, & +0.370, \\ 11.81 \end{array}$ | $\begin{aligned} & -0.362, \quad+0.383, \\ & 13.80 \end{aligned}$ | $\begin{aligned} & -0.341,+0.372,13.80 \\ & -0.144,+0.151,13.37 \end{aligned}$ |

Experimental ( $F_{\text {exp }}$ ) spherical $(\zeta=\kappa \alpha)$ and deformation $\left(\zeta^{\prime}=\kappa^{\prime} \alpha^{\prime}\right) \mathrm{S}: \zeta=4.306, \zeta^{\prime}=4.26(2)$, exponents ${ }^{\text {e }}$
4.54(1)

O: $\zeta=4.345, \zeta^{\prime}=4.98(2)$
$\mathrm{N}: \zeta=3.797, \zeta^{\prime}=3.28(1)$
C: $\zeta=3.151, \zeta^{\prime}=2.667(3)$
$\mathrm{H}: \zeta=2.436(3), \zeta^{\prime}=3.00(2)$

[^28]As shown in Table A1, Figure A1b, Sample \#2 was untwinned. Though, it was also remarkably smaller than \#1 and - at least with the optics our lab is endowed with (detector, collimator and monochromator) - too small to provide satisfying high-order data ( $2 \vartheta>55^{\circ}, \lambda=\mathrm{Mo} \mathrm{K} \alpha$ ) useful by itself for the accurate charge density estimate. In order to obtain the least biased information as possible from both specimens, we proceeded as follows: (i) first, all the individual measurements of sample \#1 undergo to some extent of intensity superposition with the parasite crystal were removed; then (ii), a data collection on sample \#2 was performed, namely at the same nominal 100(2) K temperature, employing a similar approach (Table A1). The cell parameters of the two structures were affected by very small variations ( $\approx 0.06 \%$ ), although meaningful in terms of expected least-squares standard deviations (esd's): indeed, the unit cell of sample \#2 showed a slightly greater volume $(+0.1 \%)$ than sample \#1 (see chapter 1, Table 1). In our opinion, such divergence can be ascribed to slight disparities in the data collection temperatures and so we preferred employing the unweighted average of samples \#1 and \#2 as the least-biased estimate for the cell parameters of DTC at 100 K (see the third coloumn of table 1 in chapter 1). It is worth stressing that recently Kaminski et al. ${ }^{[5]}$ analysed the structure and charge density of $\alpha$-oxalic acid dehydrate as resulting from a series of 100 K high-resolution datasets. One of their main outcomes was that the variations of topological charge density descriptors for this sole crystal structure occur over quite a small range, even at the same temperature. Thus, we guess the minor incongruity retrieved in the refined cell parameters of the two specimens would not influence the charge density results examined in the current work. (iii) Moreover, the \#1 and \#2 sets of structure factor amplitudes were independently revised by SADABS ${ }^{[6]}$ for beam anisotropy and absorption effects and eventually scaled and merged together by XPREP. ${ }^{[7]}$ We also applied an 'instrumental instability' coefficient ${ }^{[8]}$ to the final expected standard deviations, according to $\sigma_{\text {corr }}^{2}=\sigma^{2}+\mathrm{k}_{\text {CPL }} \mathrm{F}_{\exp }{ }^{2}$, with $\mathrm{k}_{\text {CPL }}$ set to 0.1625 to attain sufficiently coherent probability plot statistics (Figure A3 below). The final dataset (hereinafter: $F_{\text {exp }}$ ) had a completeness of $99.7 \%$ and an overall internal agreement factor $R_{\text {int }}$ of 0.0443 (Table A1, third column), and the subsequent multipole analysis was performed throughout by it (see Section A.1.3 below).

## A1.3 Multipole Model.

The observed reflections ( $I>2 \sigma(I)$ ) were the only included in the refinement. Least-squares were performed against $F^{2}{ }_{\exp }$ with a statistical $1 / \sigma^{2}$ weighting scheme, as for the experimental dataset (see above), while the structure factor amplitudes $F_{\text {theo }}$ were used as observations together with unitary weights concerning synthetic data (see Chapter 1). The core building and valence monopole oneelectron density functions were performed by Hartree-Fock atomic neutral functions of Clementi \& Roetti ${ }^{[9]}$. We considered radial terms for higher poles as single-exponential forms, $r^{n} \exp (-k \alpha r)$, with $n$ being $2,2,3,4$ for $l=1,2,3,4$, respectively, for second-row atoms and hydrogen, while we
selected the $n=4,6,6,6$ scheme ${ }^{[10]}$ for sulphur ${ }^{[11]}$, since its providing the most fitting outcomes, concerning residual density and statistical agreement factors in preliminary refinements against experimental data. As suitable starting point for the radial exponents $\alpha$, we chose slightly adjusted values with respect to the exponents of single-zeta wavefunctions tabulated by Hehre et al ${ }^{[12]}$. Nevertheless, in order to portray contractions and expansions of the core and valence shells, a refinemet of a couple of radial scaling parameters $k^{\prime}$ and $k$ was also independently performed for each $\mathrm{C}, \mathrm{N}, \mathrm{O}$ and H atomic species during the late phases of the least-squares process. About sulphur, two different deformation scaling factors $\kappa^{\prime}$ were allowed to change for the even $(l=0,2,4)$ and odd $(l=$ 1,3 ) poles (Table A1). Dealing with heavy atoms, ${ }^{[13]}$ where the different radial extension of the valence and $4 s$ and $3 d$ orbitals are likely to cause problems during the refinement, an efficient strategy is treating even and odd poles with different basis functions. As for the title compound, such strategy is validated by the demand of more adaptable contraction/expansion shells surrounding this atom, since it presents a mixed hybridization state caused by its quite complicated covalent environment (2 oxidic $\mathrm{O}, 1 \mathrm{C}$ and 1 imminic N , the latter set in a 4 -membred cycle). The latter might (and actually) lead to slightly different contraction/expansion effects on the higher-order poles, because of the partial mixing of low-lying virtual $d$ orbitals with valence $s$ and $p$ wavefunctions. However, final $\kappa$ ' revealed to be as large as 1.07 (2) for even and 1.14(1) for odd poles, with a total Hansen-Coppens charge of $+0.75 e$ on the oxidized $S$ atom. Nevertheless, we are required to underline that the best assessment of the model against the $\rho_{\text {EXP }}$ distribution (see also the main text) is provided by the comparison with first-principle charge density. Besides (see Section A1.4 below), thermal motion is fully depicted by the current multipolar model, being the Hirshfeld rigid bond test completely satisfied. Some specific comments are required concerning the treatment of hydrogen atoms, As H atoms are critical for both the molecular electrostatic properties and the chemical reactivity, the model we selected to examine the measured X-ray intensities presents one key-feature in electron density studies of molecular crystals, namely the anisotropic vibrational motion also for H nuclei, In the beginning, the H atoms thermal motion was modelled as isotropic. In due course, i.e. after analyzing the behaviour of some preliminary multipole models, we included anisotropic displacement parameters in the model also for hydrogen atoms (ADPH), as computed by the SHADE2 server ${ }^{[14]}$. Thus, we followed the same method formerly portrayed in A. Ø. Madsen, J. Appl. Cryst. 2006, 39, 757-758 and in Saleh, G.; Soave, R.; Lo Presti, L.; Destro, R. Chem. Eur. J. 2013, 19, 3490-3503. Later, we tested other multipole models, changing all the parameters except the ADPH. As we assumed the ultimate multipole model for DTC was found, we ran the SHADE server once more, then the newly computed ADPH added in the model and never rifined. Finally, a refinement of multipolar and radial parameters of all the atoms was performed again for some cycles, till convergence fulfillment. The covalent $\mathrm{C}-\mathrm{H}$ bond distances were arranged to the matching neutron diffraction estimates. ${ }^{[15]}$ Besides a general
electroneutrality constraint on the entire asymmetric unit, the monopole populations of all the hydrogen atoms was treated with appropriate chemical constraints, forcing the H atoms in the same -$\mathrm{CH}_{2},-\mathrm{CH}_{3}$ and phenyl groups to assume the same charge. Eventually, the H-centred dipole and quadrupole terms oriented towards the bond direction were the only allowed to be populated. ${ }^{[16,17]}$ Reports of the charge density, Laplacian and ellipticity estimates as processed at all the bond and ring critical points (bcp, rcp) retrieved in the asymmetric unit, can be found in Tables A1 and A2.

A1.4. Accuracy of geometric and thermal parameters of DTC in the solid state at $T=100 \mathrm{~K}$.
A correct treatment of the thermal motion is essential in gaining sensible experimental estimates of the bond distances. ${ }^{[18,19]}$ The program THMA14c ${ }^{[20]}$ performed the Hirshfeld rigid bond test ${ }^{[21]}$ on the thermal parameters deriving from the final multipole model against the $F_{\text {exp }}$ dataset, so to check the quality of the refined anisotropic displacement parameters (ADP's) at $T=100 \mathrm{~K}$. The test computed the average mean-square displacements amplitude (<MSDA>) by the bond vectors being as low as $4(5) \cdot 10^{-4} \AA^{2}$ for the 22 covalent bonds involving non-H atoms, and thus was fully satisfied. The possible influence of rigid-body motion on the low-temperature geometric parameters in DTC was verified performing the rigid-body TLS analysis by Schomaker and Trueblood. ${ }^{[21-23]}$ As a result, we noticed the TLS decomposition conforms with the experimental Debye-Waller factors of non-H atoms, as the variances between experimental and computed $U_{\mathrm{ij}}$ elements of the atomic thermal tensors never exceeded $\pm 0.003 \AA^{2}$ within the bonded anisole and thiazete moieties. Quite the reverse occurs within those groups far from the two-ring backbone $\left(-\mathrm{CH}_{2} \mathrm{CH}_{3},-\mathrm{CN}\right.$ and sulphonyl oxygen atoms O 2 and O 3 ), where stronger incongruities were retrieved, as expected. These evidences lead to the conclusion that the bonded anisole and thiazete groups indeed create a rigid-body system, i.e. they collectively vibrate in the crystal, despite the very small amplitudes of their translations and librations. Actually, in the molecular inertial axes reference system the root-mean-square librations are comprised between 1.9 and 1.0 deg , and the related translations between 0.12 and 0.09 Á. Hence, rigid-body adjustments ${ }^{[6]}$ to covalent bond lengths concerning non-H atoms amount, on average, to $9.6(3) \cdot 10^{-4} \AA$ (corresponding to $0.066(2) \%$ ) and thus they can be safely omitted.

## A1.5. Statistical assessment of the weighting scheme.

The normal probability plot ${ }^{[24]}$ (Figure A2) resulting from the final multipole model (see Section A1.3 above) displays the slightly left-skewed normal distribution (Figure A3) followed by the deviations among empirical and computed squared structure factor amplitudes. At the same time, we can notice average scale factors are almost constant in $\sin \vartheta / \lambda$ (Figure A4), showing a maximum deviation not beyond $\approx 4 \%$ for high angle data. Such small discrepancies from the ideal results are probably due to slight inaccuracies concerning the merging of the two primary datasets. Actually, every data
manipulations require somehow the loss of a bit of information and thus are likely to systematic miscalculations. ${ }^{[25]}$, Moreover, adjusting by twinning during the rebuilding of a full dataset from two different samples is for sure the more awkward stage of the entire data reduction procedure. Nevertheless, the final model seems to be fully satisfactory in physical-chemical perspective. Indeed, the deformation density maps (Figure A5) are perfectly reasonable, showing the charge density mainly set along chemical bonds and N lone pairs well highlighted. The residual maps are essentially featureless, too (Figure A5 and A6). Besides, the thermal motion looks absolutely reasonable, complying with the Hirshfeld rigid bond test for every bonded pair of non-H atoms (see Section A1.4 above). Finally, the good quality of the $\rho_{\text {ExP }}$ distribution gained through this process is guaranteed by the perfect agreement between the low-order electrostatic moments as processed from the experimental multipole density and those resulting by DFT first-principle simulations in the bulk (see Chapter 1).


Figure A2. Normal probability plot of $F_{\text {exp }}^{2}$ dataset against the final multipole model. This picture has been realized with DRKPlot v. 1.00.012, © A. Stash, Moscow, 2007.


Figure A3. Distribution of the residual statistics corresponding to the plot in Figure A2.


Figure A4. Distribution of average scale factors as a function of $\sin \vartheta / \lambda$. This picture has been realized with DRKPlot v. 1.00.012, © A. Stash, Moscow, 2007.


Figure A5. Deformation (a), (c) and residual (b), (c) maps plotted in the phenyl (a), (b) and S1-N1-C9 (c), (d) planes. Contour lines are drawn among $\pm 1.0 \mathrm{e} \cdot \AA^{-3}$, at steps of $0.05 \mathrm{e} \cdot \AA^{-3}$ for deformation density maps while are drawn among $\pm 0.1 \mathrm{e} \cdot \AA^{-3}$, at steps of $0.05 \mathrm{e} \cdot \AA^{-3}$ for the residual density maps. Solid and dotted curves respresent positive and negative values respectively. Dashed lines: zero contour.


Figure A6. $4 \AA$ x 4 Å-wide residual experimental electron density map in the O2-S1-O3 plane of crystalline DTC at $T=100(2)$ K. See Figure 1 in the main text for the atom numbering. Contour lines are drawn among $\pm 0.1 \mathrm{e} \cdot \AA^{-3}$, at steps of $0.05 \mathrm{e} \cdot \AA^{-3}$. Solid lines: positive values. Dashed lines: zero contour. Dotted lines: negative values.

## A1.6 Correlations.

In order to accomplish the current investigation, we are required to wonder whether a maximum resolution of $0.9 \AA^{-1}$ in $\sin \vartheta / \lambda$ is enough to prevent the accurate estimate of the experimental charge density to be altered by correspondences among refined parameters. ${ }^{[26]}$ Assumed that no 'magic limits' could ever guarantee that a certain solution is 'absolutely' acceptable, in the case of DTC we found just 17 substantial ( $>0.7$ ) correlation coefficients $\rho_{\mathrm{ij}}$, in the final model ( 586 parameters) at the end of the multipole fine-tuning, with an average $\left\langle\rho_{\mathrm{ij}}\right\rangle=0.78(5)$, basically involving dipoles and quadrupoles of oxygen atoms relating with the matching positional and thermal parameters. Nevertheless, we can safely assess that reliability and accuracy of the multipole model within $\sin \vartheta / \lambda$ $\leq 0.9 \AA^{-1}$ are satisfactory for the purposes of the present study on the basis of what previously examined, and now recalled: featureless $\Delta \rho$ maps, reasonable deformation maps, conformity between experimental and theoretical models, fulfilled Hirshfeld test,.

## A2. Gas-phase optimized structures.

## A2.1 Bond polarization and bond strength.

Looking at Figure A7 and Table A2 we can see the dislocation of the bcp from the bond mid-point, $\Delta_{\mathrm{bcp}}=d /\left(0.5 \cdot \mathrm{R}_{\mathrm{e}}\right)$, expressed in percentage, for $\mathrm{C}-\mathrm{N}, \mathrm{C}=\mathrm{N}$ and $\mathrm{S}-\mathrm{N}$ bonds (dashed blue lines). Here, $d$ and $\mathrm{R}_{\mathrm{e}}$, indicate, respectively, the bcp distance from the bond midpoint and to the $\mathrm{X}-\mathrm{Y}$ bond distance; the sign of $d$ is considered as positive (negative) if the bcp is next to $\mathrm{Y}(\mathrm{X})$. A measure of the bond polarization can be deduced from the $\Delta_{\text {bcp }}$ parameter:, equal to zero for a fully homopolar
bond, divergent from zero and increasing in magnitude together with the enhanced polarity of the bond.

Table A2. Bond critical point displacement parameter, $\Delta_{\text {bcp }}{ }^{\text {a }}$ See Figure 1 and Scheme 2 in the main text for the atom numbering.

| System | C9-N1 | C9-N2 | S1-N2 | $(\mathbf{S 1 - O})_{\text {avg }}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | -24.8 | -25.2 | - | - |
| $\mathbf{2}$ | -27.0 | -25.4 | -10.9 | -23.9 |
| $\mathbf{3}$ | -26.5 | -23.1 | -4.7 | -21.5 |
| $\mathbf{4}$ | -25.9 | -22.8 | -6.5 | -21.4 |

${ }^{\text {a }}$ A negative value for an A-B bond means that the bcp is displaced towards A


Figure A7. As Figure 2 in the main text, showing the Bond Degree parameter (full red lines, left scale) and bond polarization (dotted blue lines, right scale) for the series of compound shown in the Scheme 2 in the main text.

Then, the increasing closeness of bcp to the more electropositive atom with growing bond polarity determines the sign of $\Delta_{\text {bcp }}$. In all compounds, both the $\mathrm{C}-\mathrm{N}$ bonds display a large bond polarity, with the C atom clearly performing as the electropositive partner of every CN pair. Considering the in vacuo systems with the sulphonyl group, $\mathbf{2}$ shows the largest $\mathrm{C} 9-\mathrm{N} 1$ and $\mathrm{C} 9=\mathrm{N} 2$ bond polarities and even the largest S-N polarity. Such features also conforms to the largest charge separations in the N1-C9=N2-S1 moiety (2: N1-C9, 2.23; C9=N2, 2.35; N2-S1, 3.92; 3: N1-C9, 2.22; C9=N2, 2.12; N2-S1, 3.70; 4: N1-C9, 2.19; C9=N2, 2.13; N2-S1, 3.72). The agreement between the largest negative atomic charge of N 2 in systems 2-4 (2: $-1.20 ; \mathbf{3}:-1.03,4:-1.06$ ) and the largest negative $\mathrm{C} 9=\mathrm{N} 2$ and $\mathrm{S} 1-\mathrm{N} 2 \Delta_{\mathrm{bcp}}$ values for compound $\mathbf{2}$, implies the relatively higher weight of resonance structures $f-h$ and $b$ (Scheme 3) in 2: this may shed light on the causes at the roots of the ellipticity minimum and the lowest Laplacian magnitude at the $\mathrm{C} 9=\mathrm{N} 2 \mathrm{bcp}$ retrieved in compound 2. A very
significant polarization increase in the crystal then occurs in the DTC molecule (see QTAIM atomic charges in Fig. 3), Details concerning this point will be discussed in section 3. A further meaningful insight is the gradual and systematic equalization of $\mathrm{C} 9-\mathrm{N} 1$ and $\mathrm{C} 9=\mathrm{N} 2$ bonds along the $\mathbf{1 - 4}$ series not being mirrored by the equalization of their $\Delta_{\text {bcp }}$ values (Table A2). Such values are almost equal in 1, but then diverge more and more along the series and in a direction opposite and even unexpected, if considering the $\mathrm{C} 9-\mathrm{N} 1$ and $\mathrm{C} 9=\mathrm{N} 2$ bonds respectively growing and reducing their bond order from 2 to 4 . Looking for a possible reason underlying such discrepancy, we sense that also the S-N bond performs so to influence the electron delocalization and polarization in the N $\mathrm{C}=\mathrm{N}$ moiety. The remarkable $\mathrm{S}-\mathrm{N}$ bond polarity reduction during the transition from $\mathbf{2}$ to $\mathbf{3}$ (Table A2) clearly affects the $\mathrm{N}-\mathrm{C}=\mathrm{N}$ moiety and it may be the symptom of a variation in the relative importance of the different resonance structures. Finally, the so-called bond degree (BD) parameter ${ }^{[27]}$ is portrayed in Figure A7 (full red lines). Described as the ratio $[H(\mathbf{r}) / \rho(\mathbf{r})]_{b c p}$, where $H(\mathbf{r})$ is the energy density at $\mathbf{r}$, such value is meant to measure the bond covalence on absolute footing. Essentially, BD is the expression of the total energy per electron at the bcp; the more negative is BD , the more the bond is covalent and stronger. As predictable, roughly opposite variations occurs for the conjugated $\mathrm{C}-\mathrm{N}$ bonds: $\mathrm{BD}_{\mathrm{C} 9=\mathrm{N} 2}$ (full red triangles) turns monotonically less negative, i.e. the double bond fades, while $\mathrm{BD}_{\mathrm{C}-\mathrm{N} 1}$ (full red circles) falls as adding the $\mathrm{SO}_{2}$ group (from 1 to 2), but then has no significant variation throughout the series 2-5, notwithstanding its bond length is more and more decreasing. Considering this parameter, a significant similarity occurs in the two bonds C9=N2 and C9-N1 for compounds 4 (DTC) and 5 (TAYCUR), complying with the performance of the bond length, $\rho_{\mathrm{bcp}}, \varepsilon$ and $\nabla^{2} \rho_{\mathrm{bcp}}$ parameters (see Figure 2 a and 2 b in the main text).

## A2.2 Delocalization indices.

The analysis of the delocalization index, $\delta(\mathrm{A}, \mathrm{B})$ represents for sure a useful complement to the current study. Despite the framework of the Kohn-Sham formalism does not strictly define the electron-pair density, in this case approximate $\delta(\mathrm{A}, \mathrm{B})$ values were directly drawn from the KohnSham orbitals and by employing an HF-like second order exchange density matrix. Generally, we know that delocalization indices derived by this method are slightly overestimated, as the electronic Coulomb correlation is not entirely considered by common exchange-correlation functionals. However, the current study mainly focuses on trends (not absolute values) of $\delta(\mathrm{A}, \mathrm{B})$, and this is the reason why we adopted the DFT methods in order to get the most rational and appropriate agreement - in terms of accuracy - among the selected topological descriptors. The delocalization indices among atoms belonging to the conjugated system (N1, C9, N2, S1, plus the sulphonyl
oxygen atoms O 2 and O 3 ) are reported in Table A 3 . At a first glance, we notice that the electronegative atoms directly bonded to sulphur ( $\mathrm{O} 2, \mathrm{O} 3$ and N 2 ) always share a remarkable quantity of electrons, yet with no significant variations through the series $\mathbf{2 - 5}$. The $\delta(\mathrm{N} 1, \mathrm{~N} 2)$, $\delta(\mathrm{N} 1, \mathrm{C} 9)$ and $\delta(\mathrm{N} 2, \mathrm{C} 9)$ descriptors seems to be more intriguing, because of their intimate correlation with the measure of electron delocalization throughout the $\mathrm{C}-\mathrm{N}$ chain: they are evidently different and far smaller when the conjugation ends, as occurring in the saturated thiazetidine ring 6 (last rows in Table A3). Considering systems 1-5, the $\delta$ values performs more constantly and their general trend is systematically decreasing throughout the series for both $\delta(\mathrm{N} 1, \mathrm{~N} 2)$ and $\delta(\mathrm{N} 2, \mathrm{C} 9)$ while, an increase occurs for $\delta(\mathrm{N} 1, \mathrm{C} 9)$.

Table A3. Delocalization indices $\delta(\mathrm{A}, \mathrm{B})$ for atom pairs within or near the $\mathrm{N}-\mathrm{C}=\mathrm{N}$ system in compounds 1-6, as evaluated from the gas-phase optimized structures at the B3LYP 6-311G(p,d) level. See Figure 1 and Scheme 2 for the atom numbering

| $\delta(\mathrm{A}, \mathrm{B})$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{A}=\mathrm{N} 1, \mathrm{~B}=$ | C 9 | N 2 | S 1 | O 2 | O 3 |
| 1 | 1.05 | 0.26 | $/ /$ | $/ /$ | I/ |
| 2 | 1.11 | 0.26 | 0.02 | 0.01 | 0.00 |
| 3 | 1.10 | 0.23 | 0.03 | 0.01 | 0.00 |
| 4 | 1.14 | 0.21 | 0.02 | 0.01 | 0.00 |
| 5 | 1.13 | 0.21 | 0.02 | 0.00 | 0.00 |
| 6 | 1.02 | 0.13 | 0.02 | 0.00 | 0.00 |
|  |  |  |  |  |  |
| $\mathrm{~A}=\mathrm{N} 2, \mathrm{~B}=$ | C 9 | S 1 | O 2 | O 3 |  |
| 1 | 1.59 | $/ /$ | $/ /$ | $/ /$ |  |
| 2 | 1.40 | 0.89 | 0.16 | 0.17 |  |
| 3 | 1.42 | 0.89 | 0.15 | 0.15 |  |
| 4 | 1.34 | 0.91 | 0.14 | 0.14 |  |
| 5 | 1.33 | 0.92 | 0.14 | 0.14 |  |
| 6 | 0.89 | 0.86 | 0.15 | 0.17 |  |
| $\mathrm{~A}=\mathrm{S} 1, \mathrm{~B}=$ | C 9 | O 2 | O 3 |  |  |
| 2 | 0.04 | 1.17 | 1.15 |  |  |
| 3 | 0.09 | 1.21 | 1.21 |  |  |
| 4 | 0.08 | 1.22 | 1.21 |  |  |
| 5 | 0.09 | 1.19 | 1.19 |  |  |
| 6 | 0.06 | 1.17 | 1.15 |  |  |
|  |  |  |  |  |  |
| $\mathrm{~A}=\mathrm{O} 2, \mathrm{~B}=$ | C 9 | O 3 |  |  |  |
| 2 | 0.02 | 0.24 |  |  |  |
| 3 | 0.03 | 0.26 |  |  |  |
| 4 | 0.02 | 0.25 |  |  |  |
| 5 | 0.02 | 0.25 |  |  |  |
| 6 | 0.02 | 0.26 |  |  |  |

Such values gets even more stable in the conjugated systems, as the sulphonyl group is present (2-5 series), and display not a prominent $\delta(\mathrm{N} 2, \mathrm{C} 9)$ peak and a shallow $\delta(\mathrm{N} 1, \mathrm{C} 9)$ minimum for compound $\mathbf{3}$, i.e. upon insertion of the thiazete ring and before substitution of the H atoms related to N1 by ethyl groups. Actually, the most relevant effects (in the 2-5 series) are due to this latter perturbation, leading to a more similar electron delocalization in the $\mathrm{N} 2=\mathrm{C} 9$ and $\mathrm{N} 1-\mathrm{C} 9$ bonds. The origins of such a performance can be found by inspecting the localization indices, or, more meaningfully, the percentage of localized electrons, $\delta(\Omega, \Omega) / \mathrm{N}(\Omega)$ Table S4, which show they are mostly steady for all atoms in systems $\mathbf{2 - 5}$, except quite a remarkable reduction upon H substitution with ethyl groups at this atom, namely from 0.81 to 0.77 of the percentage of electrons localized on N1.

Table A4. Percentage of localized electrons, $\delta(\Omega, \Omega) / \mathrm{N}(\Omega)$ in compounds $1-5$, as evaluated from the gas-phase optimized structures at the B3LYP 6-311G(p,d) level. See Figure 1 and Scheme 2 in the main text for the atom numbering.

| System | $\mathbf{N 1}$ | $\mathbf{N} \mathbf{2}$ | $\mathbf{S} 1$ | $\mathbf{C 9}$ | $(\mathbf{O})_{\text {avg }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 0.809 | 0.822 | - | 0.63 | - |
| $\mathbf{2}$ | 0.809 | 0.811 | 0.840 | 0.64 | 0.903 |
| $\mathbf{3}$ | 0.810 | 0.809 | 0.840 | 0.62 | 0.903 |
| $\mathbf{4}$ | 0.772 | 0.805 | 0.841 | 0.62 | 0.900 |
| $\mathbf{4}^{\text {a }}$ | 0.772 | 0.810 | 0.843 | 0.62 | 0.902 |
| $\mathbf{5}$ | 0.772 | 0.806 | 0.842 | 0.62 | 0.901 |
| Crystal geometry |  |  |  |  |  |
|  |  |  |  |  |  |

Since having a larger positive inductive ( +I ) effect than H atoms (their global positive charge in $\mathbf{4}$ is 0.927 e, compared to a value of only 0.828 for the two H atoms in 3: see Figure 3 in Chapter 1), ethyl groups spread more electrons than H to the N 1 atom that, instead, delocalizes them through the $\pi$-system, increasing the relative weight of resonance structure $b$. Actually, from $\mathbf{3}$ to $\mathbf{4}$ the negative charge on N 1 even slightly reduces by $0.005 e$, while the one on N 2 grows by six times more. The boost of the $\delta(\mathrm{N} 2, \mathrm{~S} 1)$ value transitioning from $\mathbf{3}$ to $\mathbf{4}-5$ provides a further validation to our analysis, implying an enhanced weight for resonance structures $c-e$, too.

## A2.3 Source function values.

The rising equalization of $\mathrm{N} 1-\mathrm{C} 9$ and $\mathrm{N} 2=\mathrm{C} 9$ bonds down the $\mathbf{1 - 4}$ series is confirmed by the SF data listed in Table A5, as the $\mathrm{SF}_{\mathrm{C}_{\mathrm{C}}+\mathrm{N} 2}$ value gets closer and closer to $\mathrm{SF} \%_{{ }_{\mathrm{C} 9+\mathrm{N} 1}}$ (their discrepancy reduces from 6.8 in $\mathbf{1}$ to $3.4 \%$ in 4). However, only $\mathrm{SF} \%_{\mathrm{C} 9+\mathrm{N} 2}$ is concerned in such variation, complying with the reduction occurring in the value of $\delta(\mathrm{N} 2, \mathrm{C} 9)$, that is larger than the growth in
$\delta(\mathrm{N} 1, \mathrm{C} 9)$. The reduction rather than the estimated increase of the N 1 and $\mathrm{N} 2 \mathrm{SF} \%$ contributions at their $\mathrm{C}-\mathrm{N}$ bond bcps denotes that electron delocalization in the $\mathrm{N}-\mathrm{C}=\mathrm{N}$ moiety does not enhance down the $\mathbf{2 - 4}$ series, notwithstanding bond lengths get more similar in value. This occurs either as the reference point is the bcp, either as it is dislocated from the bcp by $\pm 0.5 \AA$ along the $\lambda_{2}$ eigenvector to underline the impact of $\pi$-electrons. The decrease in $\mathrm{SF} \%_{\mathrm{N} 1}$ and $\mathrm{SF} \%_{\mathrm{N} 2}$ values mirrors what observed for $\delta(\mathrm{N} 2, \mathrm{~N} 1)$.

Table A5. Percentage Source Function values, $\operatorname{SF} \%(\Omega, b c p)$ in compounds $1-4$, as evaluated from the gas-phase optimized structures at the B3LYP 6-311G(p,d) level. See Figure 1 and Scheme 2 for the atom numbering.

|  | $\mathrm{N} 2=\mathrm{C} 9$ |  |  |  | $\mathrm{N} 2=\mathrm{C} 9$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| System | C9+N2 | N1 | N2 | C9 | C9+N2 | N1 | N2 | C9 | C8 | C7 |
| 1 | 90.0 | 4.1 | 48.9 | 41.1 | $\begin{aligned} & \hline 82.2 \\ & 82.2 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 6.9 \\ & 6.7 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 47.8 \\ & 47.9 \\ & \hline \end{aligned}$ | $\begin{array}{r} \hline 34.4 \\ 34.3 \\ \hline \end{array}$ | // | // |
| 2 | 88.2 | 5.0 | 48.0 | 40.2 | $\begin{aligned} & \hline 78.8 \\ & 78.8 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 8.3 \\ & 8.3 \\ & \hline \end{aligned}$ | $\begin{aligned} & 46.5 \\ & 46.6 \\ & \hline \end{aligned}$ | $\begin{array}{r} 32.3 \\ 32.2 \\ \hline \end{array}$ | $\begin{aligned} & \hline 0.1 \\ & 0.2 \\ & \hline \end{aligned}$ | // |
| 3 | 87.1 | 4.7 | 47.2 | 39.9 | $\begin{aligned} & \hline 77.2 \\ & 77.2 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 7.8 \\ & 7.8 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 45.3 \\ & 45.3 \\ & \hline \end{aligned}$ | $\begin{array}{r} 31.9 \\ 31.9 \\ \hline \end{array}$ | $\begin{aligned} & 3.7 \\ & 3.7 \\ & \hline \end{aligned}$ | // |
| 4 | 86.4 | 4.2 | 46.7 | 39.7 | $\begin{aligned} & 75.9 \\ & 75.9 \end{aligned}$ | $\begin{aligned} & \hline 6.7 \\ & 6.7 \end{aligned}$ | $\begin{aligned} & \hline 44.3 \\ & 44.2 \end{aligned}$ | $\begin{aligned} & 31.6 \\ & 31.7 \end{aligned}$ | $\begin{aligned} & 2.5 \\ & 2.6 \end{aligned}$ | $\begin{aligned} & \hline 0.3 \\ & 0.3 \end{aligned}$ |


|  | C9-N1 |  |  |  | $\mathrm{C} 9-\mathrm{N} 1$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| System | C9+N1 | N2 | C9 | N1 | C9+N1 | N2 | C9 | N1 | C8 | C7 |
| 1 | 83.2 | 8.2 | 38.6 | 44.6 | $\begin{aligned} & \hline 69.6 \\ & 70.0 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 14.1 \\ & 14.2 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 29.1 \\ & 28.6 \\ & \hline \end{aligned}$ | $\begin{aligned} & 40.5 \\ & 41.4 \\ & \hline \end{aligned}$ | // | // |
| 2 | 84.3 | 7.3 | 38.6 | 45.7 | $\begin{array}{r} 72.3 \\ 72.1 \\ \hline \end{array}$ | $\begin{aligned} & 12.3 \\ & 12.3 \\ & \hline \end{aligned}$ | $\begin{array}{r} 29.3 \\ 29.3 \\ \hline \end{array}$ | $\begin{array}{r} 43.0 \\ 42.8 \\ \hline \end{array}$ | $\begin{aligned} & 0.1 \\ & 0.1 \\ & \hline \end{aligned}$ | // |
| 3 | 84.4 | 6.9 | 38.5 | 45.9 | $\begin{aligned} & \hline 71.4 \\ & 71.4 \\ & \hline \end{aligned}$ | $\begin{aligned} & 11.9 \\ & 11.9 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 28.3 \\ & 28.3 \\ & \hline \end{aligned}$ | $\begin{aligned} & \hline 43.1 \\ & 43.1 \\ & \hline \end{aligned}$ | $\begin{aligned} & 3.6 \\ & 3.6 \end{aligned}$ | // |
| 4 | 83.0 | 6.3 | 38.8 | 44.2 | $\begin{aligned} & 69.3 \\ & 69.5 \end{aligned}$ | $\begin{aligned} & 10.6 \\ & 10.6 \end{aligned}$ | $\begin{aligned} & 29.7 \\ & 29.9 \end{aligned}$ | $\begin{aligned} & 39.6 \\ & 39.6 \end{aligned}$ | $\begin{aligned} & 2.2 \\ & 2.4 \end{aligned}$ | $\begin{gathered} -0.1 \\ 0.2 \end{gathered}$ |

## A3. Crystal field effects.



Figure A8. Wires diagram of the DTC molecule and part of its crystalline environment, with the relevant $\mathrm{CH} \cdots \mathrm{X}, \mathrm{X}=\mathrm{O}, \mathrm{N}$ intermolecular contacts (reported in bold in Table A10 below)
highlighted. Other hydrogen atoms are omitted for clarity. The molecule at the centre of the picture corresponds to the DTC asymmetric unit in the solid-state conformation (polymorph A) at T $=100$ K.

Table A6. Relevant $\left(d_{\mathrm{H} \cdots \mathrm{A}} \leq 3.1 \AA, \alpha_{\mathrm{D}-\mathrm{H} \cdots \mathrm{A}} \geq 120.0 \mathrm{deg}\right) \mathrm{CH} \cdots \mathrm{A}, \mathrm{A}=\mathrm{N}, \mathrm{O}$ hydrogen bonded contacts (in the form Donor-Acceptor $\cdots$ Hydrogen) in solid DTC at $T=100 \mathrm{~K}$ (polymorph A, this work), as computed from the final multiple model against measured X-ray structure factor amplitudes. The most significant contacts are highlighted in bold. When meaningful, estimated standard deviations are reported in parentheses. ${ }^{\text {a,b }}$

| D-H...A | $d_{\text {D-H }} / \AA^{\text {b }}$ | $d_{\mathrm{H} \cdots \mathrm{A}} / \AA$ | $d_{\text {D } \ldots \mathrm{A}} / \AA$ | $\alpha_{\text {D-H..A }} /$ deg | Symmetry ${ }^{\text {c }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Involving the thiazete: |  |  |  |  |  |
| C1-HC1 $\cdots$ N2 | 1.077 | 3.053 | 3.799(1) | 126.9 | 1/2-x, 1/2+y, 3/2-z |
| C5-H5..N2 | 1.083 | 2.538 | 3.593(1) | 164.3 | 1/2-x, 1/2+y, 3/2-z |
| C14-H4A $\cdots$ O3 | 1.077 | 2.776 | 3.614(1) | 134.6 | -1/2+x, 3/2-y, 1/2+z |
| C3-H3.03 | 1.083 | 2.574 | 3.604(1) | 158.6 | 1/2+x, 3/2-y, 1/2+z |
| C1-HA1...O3 | 1.077 | 2.862 | 3.577(1) | 124.0 | -1/2-x, 1/2+y, 3/2-z |
| C6-H6..O2 | 1.083 | 2.654 | 3.466(1) | 131.4 | 1/2-x, 1/2+y, 3/2-z |
| C4-H4..O2 | 1.083 | 2.407 | 3.460(1) | 163.6 | -x, 2-y, 1-z |
| C14-H4B $\cdots$ O2 | 1.077 | 2.838 | 3.505(1) | 120.1 | $1-\mathrm{x}, 2-\mathrm{y}, 1-\mathrm{z}$ |
| Other groups: |  |  |  |  |  |
| C14-H4C..N3 | 1.077 | 2.755 | 3.686(1) | 144.7 | $x, y, z$ (intramolecular) ${ }^{\text {d }}$ |
| C14-H4B ...N3 | 1.077 | 2.848 | 3.746(1) | 140.9 | $1-\mathrm{x}, 2-\mathrm{y}, 1-\mathrm{z}$ |
| C12-H2B $\cdots$ O1 | 1.077 | 2.887 | 3.728(1) | 135.2 | $-1+\mathrm{x}, \mathrm{y}, \mathrm{z}$ |
| C13-H3A $\cdots$ O1 | 1.092 | 3.066 | 4.129(1) | 164.6 | $-1+x, y, z$ |

[^29]
(a)

(b)

Figure A9. Contour plot of the $\rho(\mathbf{r})$ (left) and $-\nabla^{2} \rho(\mathbf{r})$ (right) functions in the $\mathrm{S} 1-\mathrm{N} 2-\mathrm{C} 9$ plane within the thiazete ring in DTC. For the charge density, 20 curves are plotted starting from 0.05 $\mathrm{e} \cdot \AA^{-3}$, at steps of $0.1 \mathrm{e} \cdot \AA^{-3}$. For the negative laplacian, 16 curves are drawn at variable intervals (dotted: negative values, full: positive values, dashed: zero line). (a) Multipole-projected charge density ( $\rho_{\text {Mм-PQM }}$ ) of the isolated DTC molecule optimized at the B3LYP 6-311G(p,d) theory level.
(b) Multipole charge density ( $\rho_{\text {ExPT }}$ ) of the DTC molecule extracted from the crystal, as refined against experimental structure factor amplitudes

Table A7. C-N and C=N distances as obtained for the gas-phase optimized geometries of DTC with different Hamiltonians, in conjunction with the same $6-311 \mathrm{G}(\mathrm{p}, \mathrm{d})$ basis set.

|  | $\mathrm{C}-\mathrm{N}, \mathrm{C}=\mathrm{N}$ distances |  |  |
| :--- | :---: | :---: | :---: |
|  | PBE0 | M06 | MP 2 |
| N1 - C9 | 1.3251 | 1.3266 | 1.3314 |
| N2 $=$ C9 | 1.3133 | 1.3106 | 1.3255 |

Table A8. Values of various bond descriptors for the DTC molecule from various theoretical models and experiment. ${ }^{\text {a }}$ See Figure 1 and Scheme 2 in the main text for the atom numbering.

| Density | C9-N1 |  |  | C9-N2 |  |  | S1-N2 |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{R}_{\mathrm{e}}$ | $\rho$ | $\Delta_{\text {bcp }}$ | $\mathrm{R}_{\mathrm{e}}$ | $\rho$ | $\Delta_{\text {bcp }}$ | $\mathrm{R}_{\mathrm{e}}$ | $\rho$ | $\Delta_{\text {bcp }}$ |
| $\rho_{\text {VQM }}$ | 1.333 | 2.274 | -25.9 | 1.316 | 2.463 | -22.8 | 1.701 | 1.552 | -6.5 |
| $\rho_{\mathrm{VQM}-\mathrm{FRO}}$ | 1.314 | 2.355 | -27.3 | 1.333 | 2.388 | -20.6 | 1.654 | 1.674 | -18.8 |
| $\rho_{\mathrm{PQM}}$ | - | 2.369 | -26.6 | - | 2.382 | -21.4 | - | 1.680 | -17.7 |
| $\rho_{\mathrm{MM}-\mathrm{PQM}}$ | - | 2.436 | -15.3 | - | 2.370 | -9.8 | - | 1.663 | -3.0 |
| $\rho_{\text {EXP }}$ | - | 2.553 | -23.6 | - | 2.510 | -11.5 | - | 1.752 | 3.8 |
|  |  |  |  |  |  |  |  |  |  |

${ }^{\text {a }}$ Units are $\AA$ for distances, e $\cdot \AA^{-3}$ for electron density $\rho ; \Delta_{\text {bcp }}$ is the bcp displacement parameter; a negative value for an A-B bond means that the bcp is displaced towards A

The $\rho(\mathbf{r})$ data at bcp's listed in Table A6 confirm that C9-N1 and S1-N2 are strengthened and $\mathrm{C} 9=\mathrm{N} 2$ is weakened upon crystallization, with the larger effect arising from the change of geometry. The displacement of the bcp from the bond mid-point towards the more electropositive atom (C) slightly increases for C9-N1 and similarly decreases for $\mathrm{C} 9=\mathrm{N} 2$, despite the enhancement of the charge separation for $\mathrm{C} 9=\mathrm{N} 2$ upon crystallization would predict an opposite behaviour for such a bond. However, it should be considered that the moderate shift of the bcp towards N 2 is but the consequence of the already noticed very large shift of the $\mathrm{S} 1-\mathrm{N} 2 \mathrm{bcp}$ towards the S atom, due to the great enhancement of the positive charge of S and charge separation between N 2 and S 1 .

Table A9. Source contributions at N1-C9, C9=N2 and N2-S1 bcp's for the DTC charge density in the gas-phase and in the solid-state.

| ATOM | SOURCE CONTRIBUTIONS AT BCP'S DTC CHARGE DENSITY |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | N1-C9 |  | $\mathrm{C} 9=\mathrm{N} 2$ |  | N2-S1 |  |
|  | gas-ph. | solid-st. | gas-ph. | solid-st. | gas-ph. | solid-st. |
| S1 | 0.20 | 0.21 | 0.81 | 1.10 | 35.93 | 34.27 |
| O1 | 0.15 | 0.12 | 0.14 | 0.12 | 0.21 | 0.17 |
| O3 | 0.71 | 0.71 | 1.19 | 1.37 | 6.93 | 6.22 |
| O2 | 0.70 | 0.67 | 1.20 | 1.33 | 6.98 | 6.02 |
| N1 | 44.16 | 45.01 | 4.22 | 3.84 | 1.23 | 1.21 |
| N2 | 6.31 | 5.04 | 46.70 | 47.83 | 40.79 | 43.73 |
| N3 | 1.16 | 1.04 | 1.07 | 1.04 | 1.50 | 1.34 |
| C1 | 0.01 | -0.02 | 0.01 | -0.02 | 0.02 | -0.03 |
| C2 | 0.06 | 0.12 | 0.06 | 0.13 | 0.09 | 0.16 |
| C5 | 0.19 | 0.18 | 0.18 | 0.18 | 0.25 | 0.22 |
| C6 | -0.04 | -0.02 | 0.01 | 0.02 | -0.02 | -0.01 |
| C3 | 0.13 | 0.14 | 0.12 | 0.14 | 0.18 | 0.19 |
| C4 | 0.17 | 0.21 | 0.17 | 0.21 | 0.21 | 0.25 |
| C7 | 0.04 | 0.18 | 0.16 | 0.28 | 0.14 | 0.30 |
| C8 | 1.43 | 1.22 | 1.62 | 1.44 | 0.87 | 0.95 |
| C9 | 38.80 | 39.27 | 39.71 | 39.05 | 2.90 | 3.19 |
| C10 | -0.11 | -0.10 | 0.02 | 0.01 | -0.05 | -0.02 |
| C11 | 0.66 | 0.57 | 0.09 | -0.03 | 0.03 | -0.07 |
| C12 | 0.13 | 0.13 | 0.07 | 0.06 | 0.07 | 0.05 |
| C13 | 0.66 | 0.74 | 0.19 | 0.22 | 0.10 | 0.12 |
| C14 | 0.13 | 0.16 | 0.05 | 0.07 | 0.04 | 0.06 |
| HB1 | 0.01 | -0.01 | 0.00 | -0.02 | -0.02 | -0.05 |
| HC1 | -0.02 | 0.00 | -0.01 | 0.00 | 0.01 | 0.02 |
| HA1 | 0.09 | 0.07 | 0.08 | 0.07 | 0.12 | 0.10 |
| H5 | 0.14 | 0.12 | 0.12 | 0.12 | 0.18 | 0.16 |
| H6 | -0.11 | -0.12 | -0.17 | -0.19 | -0.21 | -0.18 |
| H3 | 0.15 | 0.13 | 0.13 | 0.13 | 0.20 | 0.18 |
| H4 | 0.14 | 0.13 | 0.12 | 0.12 | 0.17 | 0.16 |
| H1A | 0.67 | 0.60 | 0.45 | 0.43 | 0.40 | 0.36 |
| H1B | 0.56 | 0.55 | 0.17 | 0.17 | -0.06 | -0.03 |
| H2C | 0.12 | 0.08 | -0.06 | -0.11 | -0.23 | -0.23 |
| H2A | 0.39 | 0.35 | 0.30 | 0.29 | 0.29 | 0.27 |
| H2B | 0.28 | 0.23 | 0.25 | 0.22 | 0.25 | 0.21 |
| H3B | 0.52 | 0.48 | 0.18 | 0.17 | 0.07 | 0.06 |
| H3A | 0.64 | 0.60 | 0.32 | 0.31 | 0.28 | 0.27 |
| H4B | 0.26 | 0.23 | 0.14 | 0.13 | 0.14 | 0.12 |
| H4C | 0.12 | 0.10 | 0.01 | 0.00 | -0.06 | -0.06 |
| H4A | 0.36 | 0.33 | 0.23 | 0.22 | 0.23 | 0.22 |

Table A10. Structural and topological point descriptors at the bond critical points for the $\rho_{\text {EXPT }}$ charge density distribution of DTC at $T=100(2) \mathrm{K}$. Units are $\AA, \mathrm{e} \cdot \AA^{-3}$ and $\mathrm{e} \cdot \AA^{-5}$. Least-squares estimated standard deviations are reported in parentheses.

| Bond |  | $d$ | $\rho(\mathrm{r})_{\text {bcp }}$ | $\nabla^{2} \rho()_{\text {bcp }}$ | $\varepsilon$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{S}(1)$ | $-\mathrm{N}(2)$ | $1.6539(4)$ | $1.752(22)$ | $-5.998(66)$ | 0.05 |
| $\mathrm{~S}(1)$ | $-\mathrm{O}(2)$ | $1.4367(5)$ | $2.462(30)$ | $-18.082(143)$ | 0.23 |
| $\mathrm{~S}(1)$ | $-\mathrm{O}(3)$ | $1.4318(6)$ | $2.566(30)$ | $-19.711(145)$ | 0.09 |
| $\mathrm{~S}(1)$ | $-\mathrm{C}(8)$ | $1.8960(6)$ | $1.116(15)$ | $-1.498(29)$ | 0.13 |
| $\mathrm{O}(1)$ | $-\mathrm{C}(1)$ | $1.4271(8)$ | $1.703(17)$ | $-8.116(66)$ | 0.09 |
| $\mathrm{O}(1)$ | $-\mathrm{C}(2)$ | $1.3551(7)$ | $2.092(16)$ | $-20.338(79)$ | 0.05 |
| $\mathrm{~N}(1)$ | $-\mathrm{C}(9)$ | $1.3144(5)$ | $2.553(16)$ | $-34.390(75)$ | 0.17 |
| $\mathrm{~N}(1)$ | $-\mathrm{C}(11)$ | $1.4741(7)$ | $1.698(14)$ | $-9.159(47)$ | 0.02 |
| $\mathrm{~N}(1)$ | $-\mathrm{C}(13)$ | $1.4693(5)$ | $1.755(14)$ | $-10.508(45)$ | 0.04 |
| $\mathrm{~N}(2)$ | $-\mathrm{C}(9)$ | $1.3325(5)$ | $2.510(15)$ | $-23.784(50)$ | 0.17 |
| $\mathrm{~N}(3)$ | $-\mathrm{C}(10)$ | $1.1569(5)$ | $3.356(21)$ | $-0.511(145)$ | 0.02 |
| $\mathrm{C}(1)$ | $-\mathrm{H}(\mathrm{A} 1)$ | $1.0770(5)$ | $1.782(27)$ | $-14.831(80)$ | 0.03 |
| $\mathrm{C}(1)$ | $-\mathrm{H}(\mathrm{B} 1)$ | $1.0770(5)$ | $1.823(28)$ | $-16.666(76)$ | 0.10 |
| $\mathrm{C}(1)$ | $-\mathrm{H}(\mathrm{C} 1)$ | $1.0770(5)$ | $1.828(25)$ | $-16.951(65)$ | 0.06 |
| $\mathrm{C}(2)$ | $-\mathrm{C}(3)$ | $1.4009(5)$ | $2.200(13)$ | $-21.167(33)$ | 0.21 |
| $\mathrm{C}(2)$ | $-\mathrm{C}(5)$ | $1.3996(5)$ | $2.208(13)$ | $-21.192(33)$ | 0.20 |
| $\mathrm{C}(3)$ | $-\mathrm{C}(4)$ | $1.3861(5)$ | $2.172(13)$ | $-19.754(32)$ | 0.18 |
| $\mathrm{C}(3)$ | $-\mathrm{H}(3)$ | $1.0830(4)$ | $1.857(24)$ | $-17.768(74)$ | 0.04 |
| $\mathrm{C}(4)$ | $-\mathrm{C}(7)$ | $1.4009(5)$ | $2.156(13)$ | $-19.559(31)$ | 0.18 |
| $\mathrm{C}(4)$ | $-\mathrm{H}(4)$ | $1.0830(4)$ | $1.858(24)$ | $-17.462(74)$ | 0.04 |
| $\mathrm{C}(5)$ | $-\mathrm{C}(6)$ | $1.3940(5)$ | $2.126(13)$ | $-18.711(33)$ | 0.17 |
| $\mathrm{C}(5)$ | $-\mathrm{H}(5)$ | $1.0830(4)$ | $1.856(23)$ | $-17.647(66)$ | 0.05 |
| $\mathrm{C}(6)$ | $-\mathrm{C}(7)$ | $1.3972(5)$ | $2.173(13)$ | $-20.098(32)$ | 0.17 |
| $\mathrm{C}(6)$ | $-\mathrm{H}(6)$ | $1.0830(4)$ | $1.848(23)$ | $-17.558(72)$ | 0.06 |
| $\mathrm{C}(7)$ | $-\mathrm{C}(8)$ | $1.5032(5)$ | $1.724(11)$ | $-12.179(27)$ | 0.12 |
| $\mathrm{C}(8)$ | $-\mathrm{C}(9)$ | $1.5343(5)$ | $1.648(11)$ | $-10.027(25)$ | 0.03 |
| $\mathrm{C}(8)$ | $-\mathrm{C}(10)$ | $1.4548(5)$ | $1.826(13)$ | $-12.624(32)$ | 0.04 |
| $\mathrm{C}(11)$ | $-\mathrm{C}(12)$ | $1.5173(6)$ | $1.696(13)$ | $-10.758(27)$ | 0.04 |
| $\mathrm{C}(11)$ | $-\mathrm{H}(1 \mathrm{~A})$ | $1.0920(4)$ | $1.847(23)$ | $-16.494(64)$ | 0.04 |
| $\mathrm{C}(11)$ | $-\mathrm{H}(1 \mathrm{~B})$ | $1.0920(4)$ | $1.840(24)$ | $-16.289(68)$ | 0.07 |
| $\mathrm{C}(12)$ | $-\mathrm{H}(2 \mathrm{~A})$ | $1.0770(5)$ | $1.792(27)$ | $-14.802(75)$ | 0.03 |
| $\mathrm{C}(12)$ | $-\mathrm{H}(2 \mathrm{~B})$ | $1.0770(5)$ | $1.733(29)$ | $-13.990(77)$ | 0.06 |
| $\mathrm{C}(12)$ | $-\mathrm{H}(2 \mathrm{C})$ | $1.0770(7)$ | $1.780(25)$ | $-14.903(67)$ | 0.02 |
| $\mathrm{C}(13)$ | $-\mathrm{C}(14)$ | $1.5211(6)$ | $1.667(12)$ | $-10.502(25)$ | 0.04 |
| $\mathrm{C}(13)$ | $-\mathrm{H}(3 \mathrm{~A})$ | $1.0920(4)$ | $1.838(23)$ | $-15.858(62)$ | 0.03 |
| $\mathrm{C}(13)$ | $-\mathrm{H}(3 \mathrm{~B})$ | $1.0920(4)$ | $1.861(23)$ | $-16.189(62)$ | 0.04 |
| $\mathrm{C}(14)$ | $-\mathrm{H}(4 \mathrm{~A})$ | $1.0770(4)$ | $1.810(24)$ | $-15.363(59)$ | 0.03 |
| $\mathrm{C}(14)$ | $-\mathrm{H}(4 \mathrm{~B})$ | $1.0770(5)$ | $1.838(24)$ | $-16.013(65)$ | 0.03 |
| $\mathrm{C}(14)$ | $-\mathrm{H}(4 \mathrm{C})$ | $1.0770(4)$ | $1.821(26)$ | $-15.546(69)$ | 0.04 |
| $\mathrm{C}(10)$ | $-\mathrm{H}(4 \mathrm{C})$ | 2.8247 | $0.044(2)$ | $0.525(1)$ | 0.33 |

Table A11. Topological point descriptors at the ring critical points for the $\rho_{\text {EXPT }}$ charge density distribution of DTC at $\mathrm{T}=100(2) \mathrm{K}$. Units are $\mathrm{e} \cdot \AA^{-3}$ and $\mathrm{e} \cdot \AA^{-5}$.

| Ring | $\rho(\mathbf{r})_{\text {bcp }}$ | $\nabla^{2} \rho(\mathbf{r})_{\text {bcp }}$ |
| :---: | :---: | :---: |
| $\mathrm{S}(1)-\mathrm{N}(2)-\mathrm{C}(9)-\mathrm{C}(8)$ | 0.5767 | 8.5 |
| $\mathrm{C}(2)-\mathrm{C}(3)-\mathrm{C}(4)-\mathrm{C}(5)-\mathrm{C}(6)-\mathrm{C}(7)$ | 0.0816 | 4.5 |
| $\mathrm{H}(4 \mathrm{C})-\mathrm{C}(14)-\mathrm{C}(13)-\mathrm{N}(1)-\mathrm{C}(9)-\mathrm{C}(8)-\mathrm{C}(10)$ | 0.0280 | 0.5 |

Table A12. Relevant bond distances ( $\AA$ ) as obtained for DTC and related compounds from B3LYP $6-311 \mathrm{G}(\mathrm{p}, \mathrm{d})$ calculations in the gas-phase, compared with multipole-derived experimental estimates at $\mathrm{T}=100$ (2) K (last column). See Scheme 2 in the main text for the meaning of the various labels. 5A and 5B refer to the two independent molecules in the asymmetric unit of TAYCUR, whereas '4froz.' refers to gas-phase DTC at frozen solid-state geometry.

| BOND | BOND LENGTH |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5A | 5B | 6 | 4-froz. | Expt. |
| S1 - N2 | // | 1.6916 | 1.7277 | 1.7013 | 1.6965 | 1.6960 | 1.7149 | 1.6539 | 1.6539(4) |
| N2 - C9 | 1.2721 | 1.2896 | 1.3048 | 1.3159 | 1.3209 | 1.3215 | 1.5109 | 1.3325 | 1.3325(5) |
| C9 - C8 | // | // | 1.5125 | 1.5407 | 1.5352 | 1.5346 | 1.5486 | 1.5343 | 1.5343(5) |
| C8 - S1 | // | 1.7992 | 1.8577 | 1.9686 | 1.9468 | 1.9461 | 1.8251 | 1.8960 | 1.8960(6) |
| C9 - N1 | 1.3799 | 1.3434 | 1.3401 | 1.3330 | 1.3329 | 1.3325 | 1.4312 | 1.3144 | 1.3144(5) |
| C8 - C10 | // | // | // | 1.4466 | 1.4997 | 1.4984 | // | 1.4548 | 1.4548(5) |
| C10-N3 | // | // | // | 1.1539 | 1.2701 | 1.2707 | // | 1.1569 | 1.3144(5) |
| C8 - C7 | // | // | // | 1.5031 | 1.5065 | 1.5042 | // | 1.5032 | 1.5032(5) |
| S1-O2 | // | 1.4585 | 1.4538 | 1.4542 | 1.4599 | 1.4618 | 1.4535 | 1.4367 | 1.4367(5) |
| S1-O3 | // | 1.4693 | 1.4538 | 1.4555 | 1.4611 | 1.4600 | 1.4625 | 1.4318 | 1.4318(6) |

Table A13. Same as Table A12 above, for charge density estimates at the bcp's (e $\AA^{-3}$ ).

|  | ELECTRON DENSITY AT BCP |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| BOND | 1 | 2 | 3 | 4 | 5A | 5B | 6 | 4-froz. | Expt. |
| S1 - N2 | // | 1.53 | 1.49 | 1.55 | 1.57 | 1.57 | 1.48 | 1.67 | 1.75(2) |
| N2 - C9 | 2.63 | 2.52 | 2.53 | 2.46 | 2.44 | 2.43 | 1.62 | 2.39 | 2.51(2) |
| C9 - C8 | // | // | 1.72 | 1.63 | 1.65 | 1.65 | 1.63 | 1.65 | 1.65(1) |
| C8 - S1 | // | 1.36 | 1.22 | 0.97 | 1.02 | 1.02 | 1.30 | 1.12 | 1.12(2) |
| C9 - N1 | 2.05 | 2.21 | 2.22 | 2.27 | 2.27 | 2.27 | 1.94 | 2.35 | 2.55(2) |
| C8 - C10 | // | // | // | 1.83 | 1.74 | 1.75 | // | 1.80 | 1.83(1) |
| C10-N3 | // | // | // | 3.23 | 2.57 | 2.57 | // | 3.21 | 3.36(2) |
| C8 - C7 | // | // | // | 1.69 | 1.68 | 1.69 | // | 1.69 | 1.72(1) |
| S1-O2 | // | 1.98 | 1.98 | 1.97 | 1.95 | 1.94 | 1.98 | 2.03 | 2.46 (3) |
| S1-O3 | // | 1.94 | 1.98 | 1.96 | 1.95 | 1.95 | 1.95 | 2.04 | 2.57(3) |
| $\begin{aligned} & \mathrm{rcp}_{\text {(1-N2-C9- }} \\ & \mathrm{c}) \end{aligned}$ | // | // | 0.54 | 0.49 | 0.50 | 0.50 | 0.46 | 0.53 | 0.58 |

Table A14. Same as Table A12 above, for the charge density laplacian at the bcp's $\left(e^{-5}\right)$.

|  | CHARGE DENSITY LAPLACIAN AT BCP |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| BOND | 1 | 2 | 3 | 4 | 5A | 5B | 6 | 4-froz. | Expt. |
| S1 - N2 | // | -14.2 | -11.5 | -13.3 | -13.8 | -13.8 | -12.8 | -14.6 | -6.00(7) |
| N2 - C9 | -27.0 | -25.4 | -27.8 | -26.9 | -26.6 | -26.6 | -13.0 | -25.8 | -23.78(5) |
| C9 - C8 | // | // | -14.3 | -12.7 | -13.0 | -13.1 | -13.0 | -13.0 | -10.03(3) |
| C8 - S1 | // | -9.2 | -6.6 | -2.9 | -3.5 | -3.5 | -8.1 | -5.0 | -1.50(3) |
| C9 - N1 | -20.7 | -21.6 | -22.3 | -22.7 | -22.6 | -22.6 | -19.4 | -22.3 | -34.39(8) |
| C8 - C10 | // | // | // | -17.0 | -15.0 | -15.0 | // | -16.4 | -12.62(3) |
| C10-N3 | // | // | // | -5.8 | -19.6 | -19.8 | // | -6.1 | -0.5(1) |
| C8 - C7 | // | // | // | -13.9 | -13.8 | -13.9 | // | -13.9 | -12.18(3) |
| S1-O2 | // | 22.2 | 23.6 | 23.8 | 22.6 | 22.1 | 23.7 | 28.5 | -18.1(1) |
| S1 - O3 | // | 20.1 | 23.6 | 23.6 | 22.3 | 22.6 | 21.4 | 30.0 | -19.7(1) |
| $\mathrm{rcp}_{(\mathrm{S} 1-\mathrm{N} 2-\mathrm{C} 9}$ <br> C8) | // | // | 9.3 | 8.5 | 8.7 | 8.7 | 8.7 | 9.2 | 8.5 |

Table A15. Same as Table A12 above, for the ellipticity estimates at the bcp's (dimensionless).

|  | ELLIPTICITY |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| BOND | 1 | 2 | 3 | 4 | 5A | 5B | 6 | 4-froz. | Expt. |
| S1 - N2 | // | 0.04 | 0.04 | 0.03 | 0.04 | 0.04 | 0.08 | 0.04 | 0.05 |
| N2 - C9 | 0.25 | 0.15 | 0.23 | 0.22 | 0.20 | 0.20 | 0.03 | 0.21 | 0.17 |
| C9 - C8 | // | // | 0.01 | 0.01 | 0.02 | 0.02 | 0.01 | 0.01 | 0.03 |
| C8 - S1 | // | 0.00 | 0.02 | 0.03 | 0.02 | 0.02 | 0.01 | 0.03 | 0.13 |
| C9 - N1 | 0.07 | 0.09 | 0.11 | 0.19 | 0.17 | 0.17 | 0.04 | 0.19 | 0.17 |
| C8 - C10 | // | // | // | 0.03 | 0.07 | 0.07 | // | 0.03 | 0.04 |
| C10-N3 | // | // | // | 0.01 | 0.23 | 0.23 | // | 0.01 | 0.02 |
| C8 - C7 | // | // | // | 0.10 | 0.07 | 0.07 | // | 0.09 | 0.12 |
| S1-O2 | // | 0.03 | 0.07 | 0.09 | 0.08 | 0.08 | 0.07 | 0.08 | 0.23 |
| S1-O3 | // | 0.05 | 0.07 | 0.09 | 0.09 | 0.09 | 0.08 | 0.08 | 0.09 |
| $\begin{aligned} & \mathrm{rcp}_{\text {(S1-N2-C9- }} \\ & \mathrm{C}^{2} \end{aligned}$ | // | // | 0.16 | 0.18 | 0.20 | 0.20 | 0.17 | 0.15 | 0.33 |

Table A16. Same as Table A12 above, for the bond degree parameter at the bcp (atomic units).

|  | BOND DEGREE PARAMETER |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| BOND | 1 | 2 | 3 | 4 | 5 A | 5 B | 6 | 4-froz. |  |
| $\mathrm{S} 1-\mathrm{N} 2$ | $/ /$ | -1.10 | -0.93 | -1.01 | -1.02 | -1.02 | -1.03 | -1.32 |  |
| $\mathrm{~N} 2-\mathrm{C} 9$ | -1.54 | -1.51 | -1.46 | -1.43 | -1.42 | -1.42 | -0.97 | -1.36 |  |
| $\mathrm{C} 9-\mathrm{C} 8$ | $/ /$ | $/ /$ | -0.84 | -0.79 | -0.80 | -0.80 | -0.79 | -0.80 |  |
| $\mathrm{C} 8-\mathrm{S} 1$ | $/ /$ | -0.71 | -0.64 | -0.50 | -0.52 | -0.52 | -0.68 | -0.59 |  |
| $\mathrm{C} 9-\mathrm{N} 1$ | -1.33 | -1.43 | -1.42 | -1.43 | -1.43 | -1.43 | -1.10 | -1.48 |  |
| $\mathrm{C} 8-\mathrm{C} 10$ | $/ /$ | $/ /$ | $/ /$ | -0.94 | -0.84 | -0.84 | $/ /$ | -0.93 |  |
| $\mathrm{C} 10-\mathrm{N} 3$ | $/ /$ | $/ /$ | $/ /$ | -1.80 | -1.58 | -1.58 | $/ /$ | -1.80 |  |
| $\mathrm{C} 8-\mathrm{C} 7$ | $/ /$ | $/ /$ | $/ /$ | -0.83 | -0.82 | -0.83 | $/ /$ | -0.83 |  |
| $\mathrm{~S} 1-\mathrm{O} 2$ | $/ /$ | -1.22 | -1.21 | -1.20 | -1.20 | -1.20 | -1.21 | -1.19 |  |
| $\mathrm{~S} 1-\mathrm{O} 3$ | $/ /$ | -1.22 | -1.21 | -1.20 | -1.20 | -1.20 | -1.21 | -1.18 |  |

Table A17. Distance of the bcp's of the N1-C9, N2=C9 and N2-S1 bonds from the corresponding N atoms for the compounds described in the caption of Table A8.

|  | N-BCP DISTANCES |  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| BOND | 1 | 2 | 3 | 4 | $5 A$ | $5 B$ | 6 | 4-froz. | Expt. |
| N1 - C9 | 0.86370 | 0.85315 | 0.84779 | 0.83925 | 0.84107 | 0.84093 | 0.83767 | 0.83623 | 0.8120 |
| N2 - C9 | 0.79762 | 0.80859 | 0.80308 | 0.80803 | 0.81005 | 0.81008 | 0.88361 | 0.80376 | 0.7428 |
| N2 - S1 | $/ /$ | 0.93920 | 0.90337 | 0.90577 | 0.90659 | 0.90564 | 0.93759 | 0.98213 | 0.7959 |

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APPENDIX A2

| $\Omega$ | LS | SF\% | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | SFs\% | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {FSS }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1 | 1.899 | 98.291 | 1.093 | 0.806 | 0.286 | 101.430 | 0.497 | 0.502 |
| N1 | 0.000 | 0.013 | -0.001 | 0.001 | -0.001 | -0.458 | 0.026 | -0.083 |
| N2 | 0.002 | 0.120 | 0.001 | 0.002 | -0.001 | -0.376 | 0.053 | -0.078 |
| N3 | 0.003 | 0.158 | 0.002 | 0.001 | 0.001 | 0.269 | 0.058 | 0.070 |
| N5 | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | -0.102 | -0.014 | -0.050 |
| N4 | -0.001 | -0.026 | 0.000 | 0.000 | 0.000 | -0.067 | -0.032 | -0.044 |
| C14 | 0.001 | 0.054 | 0.000 | 0.001 | 0.000 | -0.084 | 0.041 | -0.047 |
| C13 | 0.001 | 0.046 | 0.000 | 0.000 | 0.000 | 0.021 | 0.039 | 0.030 |
| C12 | 0.000 | 0.025 | 0.000 | 0.000 | 0.000 | -0.019 | 0.031 | -0.029 |
| C11 | 0.001 | 0.043 | 0.000 | 0.000 | 0.000 | 0.024 | 0.038 | 0.031 |
| C10 | 0.001 | 0.056 | 0.000 | 0.001 | 0.000 | -0.089 | 0.041 | -0.048 |
| C15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.005 | 0.016 |
| C17 | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | 0.000 | 0.017 | -0.007 |
| C16 | 0.000 | 0.006 | 0.000 | 0.000 | 0.000 | 0.000 | 0.019 | -0.006 |
| C16 | 0.000 | 0.006 | 0.000 | 0.000 | 0.000 | 0.000 | 0.020 | -0.005 |
| C1 | 0.001 | 0.031 | 0.000 | 0.000 | 0.000 | -0.064 | 0.034 | -0.043 |
| C2 | 0.001 | 0.039 | 0.000 | 0.000 | 0.000 | 0.018 | 0.036 | 0.028 |
| C3 | 0.000 | 0.020 | 0.000 | 0.000 | 0.000 | -0.015 | 0.029 | -0.026 |
| C4 | 0.001 | 0.038 | 0.000 | 0.000 | 0.000 | 0.017 | 0.036 | 0.028 |
| C5 | 0.001 | 0.040 | 0.000 | 0.000 | 0.000 | -0.069 | 0.037 | -0.044 |
| C6 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.003 | 0.009 | 0.015 |
| C9 | 0.000 | 0.006 | 0.000 | 0.000 | 0.000 | 0.000 | 0.019 | -0.006 |
| C8 | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | 0.000 | 0.017 | -0.006 |
| C7 | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | 0.000 | 0.017 | -0.006 |
| Cu1' | 0.001 | 0.053 | 0.001 | 0.000 | 0.001 | 0.449 | 0.040 | 0.083 |
| N1' | 0.005 | 0.233 | 0.001 | 0.003 | -0.002 | -0.728 | 0.066 | -0.097 |
| N2' | 0.003 | 0.178 | 0.001 | 0.002 | -0.001 | -0.463 | 0.061 | -0.083 |
| N3' | 0.004 | 0.223 | 0.003 | 0.002 | 0.001 | 0.331 | 0.065 | 0.075 |
| N5' | -0.001 | -0.034 | 0.000 | 0.000 | 0.000 | 0.003 | -0.035 | 0.016 |
| N4' | -0.001 | -0.034 | 0.000 | 0.000 | 0.000 | 0.000 | -0.035 | -0.008 |
| C14' | 0.000 | 0.005 | 0.000 | 0.000 | 0.000 | -0.047 | 0.018 | -0.039 |
| C13' | 0.000 | 0.013 | 0.000 | 0.000 | 0.000 | 0.013 | 0.026 | 0.026 |
| C12' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | -0.013 | 0.023 | -0.025 |
| C11' | 0.000 | 0.013 | 0.000 | 0.000 | 0.000 | 0.015 | 0.025 | 0.027 |
| C10' | 0.000 | 0.005 | 0.000 | 0.000 | 0.000 | -0.050 | 0.019 | -0.040 |
| C15' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | 0.002 | -0.010 | 0.014 |
| C17' | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | 0.000 | 0.016 | -0.007 |
| C16' | 0.000 | 0.005 | 0.000 | 0.000 | 0.000 | 0.000 | 0.018 | -0.005 |
| C16' | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | 0.000 | 0.018 | -0.005 |
| C1' | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | -0.039 | 0.021 | -0.037 |
| C2' | 0.000 | 0.015 | 0.000 | 0.000 | 0.000 | 0.012 | 0.027 | 0.025 |
| C3' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | -0.011 | 0.023 | -0.024 |
| C4' | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | 0.013 | 0.027 | 0.025 |
| C5' | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | -0.049 | 0.015 | -0.039 |
| C6' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | 0.002 | -0.009 | 0.014 |
| C9' | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | 0.000 | 0.017 | -0.006 |


| C8' | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | 0.000 | 0.016 | -0.005 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C7' | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | 0.000 | 0.016 | -0.005 |
| H1 | 0.000 | 0.015 | 0.000 | 0.000 | 0.000 | 0.000 | 0.026 | 0.003 |
| H2 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | -0.005 |
| H3 | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.000 | -0.012 | -0.006 |
| H4 | 0.000 | 0.015 | 0.000 | 0.000 | 0.000 | 0.000 | 0.027 | -0.004 |
| H5 | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.000 | -0.014 | -0.006 |
| H6 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.009 | 0.005 |
| H7 | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | 0.000 | 0.027 | -0.004 |
| H8 | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.000 | -0.014 | -0.005 |
| H9 | 0.000 | -0.003 | 0.000 | 0.000 | 0.000 | 0.000 | -0.015 | 0.006 |
| H10 | 0.000 | 0.017 | 0.000 | 0.000 | 0.000 | 0.000 | 0.027 | 0.003 |
| H11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | -0.006 |
| H12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.007 | -0.006 |
| H13 | 0.000 | 0.017 | 0.000 | 0.000 | 0.000 | 0.000 | 0.028 | -0.004 |
| H14 | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.009 | 0.006 |
| H15 | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.010 | -0.006 |
| H16 | 0.000 | 0.017 | 0.000 | 0.000 | 0.000 | 0.000 | 0.028 | -0.005 |
| H17 | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.000 | -0.013 | -0.006 |
| H18 | 0.000 | -0.004 | 0.000 | 0.000 | 0.000 | 0.000 | -0.016 | 0.005 |
| H19 | 0.000 | 0.019 | 0.000 | 0.000 | 0.000 | 0.021 | 0.029 | 0.030 |
| H20 | 0.001 | 0.033 | 0.000 | 0.000 | 0.000 | 0.001 | 0.035 | 0.009 |
| H21 | 0.001 | 0.032 | 0.000 | 0.000 | 0.000 | 0.001 | 0.034 | 0.011 |
| H22 | 0.000 | 0.018 | 0.000 | 0.000 | 0.000 | 0.020 | 0.028 | 0.029 |
| H23 | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | 0.016 | 0.025 | 0.027 |
| H24 | 0.001 | 0.027 | 0.000 | 0.000 | 0.000 | 0.001 | 0.032 | 0.009 |
| H25 | 0.001 | 0.027 | 0.000 | 0.000 | 0.000 | 0.001 | 0.032 | 0.011 |
| H26 | 0.000 | 0.007 | 0.000 | 0.000 | 0.000 | 0.014 | 0.021 | 0.026 |
| H1' | 0.000 | 0.011 | 0.000 | 0.000 | 0.000 | 0.000 | 0.024 | 0.002 |
| H2' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | -0.005 |
| H3' | 0.000 | -0.006 | 0.000 | 0.000 | 0.000 | 0.000 | -0.019 | -0.006 |
| H4' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | 0.000 | 0.023 | -0.004 |
| H5' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | -0.005 |
| H6' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.009 | 0.004 |
| H7' | 0.000 | 0.011 | 0.000 | 0.000 | 0.000 | 0.000 | 0.024 | -0.004 |
| H8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.005 |
| H9' | 0.000 | -0.006 | 0.000 | 0.000 | 0.000 | 0.000 | -0.020 | 0.005 |
| H10' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | 0.000 | 0.023 | 0.003 |
| H11' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.011 | -0.006 |
| H12' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.000 | -0.014 | -0.005 |
| H13' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | 0.000 | 0.023 | -0.004 |
| H14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.008 | 0.005 |
| H15' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.011 | -0.005 |
| H16' | 0.000 | 0.011 | 0.000 | 0.000 | 0.000 | 0.000 | 0.024 | -0.004 |
| H17' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.000 | -0.014 | -0.006 |
| H18' | 0.000 | -0.005 | 0.000 | 0.000 | 0.000 | 0.000 | -0.018 | 0.004 |
| H19' | 0.000 | -0.006 | 0.000 | 0.000 | 0.000 | 0.012 | -0.019 | 0.025 |
| H20' | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | 0.000 | 0.026 | 0.008 |
| H21' | 0.000 | 0.013 | 0.000 | 0.000 | 0.000 | 0.001 | 0.025 | 0.010 |


| H22' $^{\prime}$ | 0.000 | -0.007 | 0.000 | 0.000 | 0.000 | 0.011 | -0.020 | 0.024 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H23 $^{\prime}$ | 0.000 | 0.007 | 0.000 | 0.000 | 0.000 | 0.009 | 0.021 | 0.023 |
| H24' $^{\prime}$ | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | 0.000 | 0.027 | 0.008 |
| H25 $^{\prime}$ | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | 0.001 | 0.024 | 0.011 |
| H26 $^{\prime}$ | 0.000 | -0.023 | 0.000 | 0.000 | 0.000 | 0.011 | -0.030 | 0.024 |

Table A2.1: Contributions at the CD near to the Cu 1 atomic basin along on the $\mathrm{Cu}-\mathrm{N} 1$ bond for the EO molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r})$.
$\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FS}}\right)$ are the ray of the sphere that are proportional to the atomic contribution to $\rho(\mathbf{r})(\mathrm{s}(\mathbf{r})$ ) evaluated as

$$
\begin{aligned}
\mathrm{R}_{\mathrm{SF}} & =0.5 *(\mathrm{SF} \% / 100)^{1 / 3} \\
\mathrm{R}_{\mathrm{SFs}} & =0.5 *\left(\mathrm{SF}_{\mathrm{S}} \% / 100\right)^{1 / 3}
\end{aligned}
$$

All the reported quantity are reported in a.u.

| $\Omega$ | LS | SF\% | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | SFs\% | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {FSS }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1 | 6,473 | 99,509 | 3,249 | 3,224 | 0,025 | 118,959 | 0,499 | 0,530 |
| N1 | 0,002 | 0,025 | 0,000 | 0,002 | -0,002 | -7,676 | 0,031 | -0,212 |
| N2 | 0,003 | 0,043 | 0,001 | 0,002 | -0,001 | -5,454 | 0,038 | -0,190 |
| N3 | 0,003 | 0,054 | 0,002 | 0,001 | 0,001 | 3,890 | 0,041 | 0,169 |
| N5 | 0,000 | -0,004 | 0,000 | 0,000 | 0,000 | -1,161 | -0,017 | -0,113 |
| N4 | 0,000 | -0,002 | 0,000 | 0,000 | 0,000 | -1,213 | -0,014 | -0,115 |
| C14 | 0,001 | 0,014 | 0,000 | 0,001 | 0,000 | -1,063 | 0,026 | -0,110 |
| C13 | 0,001 | 0,013 | 0,000 | 0,000 | 0,000 | 0,273 | 0,025 | 0,070 |
| C12 | 0,000 | 0,007 | 0,000 | 0,000 | 0,000 | -0,240 | 0,020 | -0,067 |
| C11 | 0,001 | 0,012 | 0,000 | 0,000 | 0,000 | 0,312 | 0,024 | 0,073 |
| C10 | 0,001 | 0,014 | 0,000 | 0,001 | 0,000 | -1,125 | 0,026 | -0,112 |
| C15 | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | 0,039 | -0,003 | 0,036 |
| C17 | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,004 | 0,011 | -0,017 |
| C16 | 0,000 | 0,002 | 0,000 | 0,000 | 0,000 | -0,002 | 0,012 | -0,013 |
| C16 | 0,000 | 0,002 | 0,000 | 0,000 | 0,000 | -0,002 | 0,013 | -0,013 |
| C1 | 0,001 | 0,012 | 0,000 | 0,000 | 0,000 | -0,909 | 0,025 | -0,104 |
| C2 | 0,001 | 0,013 | 0,000 | 0,000 | 0,000 | 0,251 | 0,025 | 0,068 |
| C3 | 0,000 | 0,007 | 0,000 | 0,000 | 0,000 | -0,206 | 0,020 | -0,064 |
| C4 | 0,001 | 0,013 | 0,000 | 0,000 | 0,000 | 0,247 | 0,025 | 0,068 |
| C5 | 0,001 | 0,015 | 0,000 | 0,001 | 0,000 | -1,005 | 0,026 | -0,108 |
| C6 | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | 0,036 | 0,007 | 0,036 |
| C9 | 0,000 | 0,002 | 0,000 | 0,000 | 0,000 | -0,003 | 0,013 | -0,015 |
| C8 | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,002 | 0,011 | -0,014 |
| C7 | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,002 | 0,011 | -0,014 |
| Cu1' | 0,001 | 0,015 | 0,001 | 0,000 | 0,001 | 5,954 | 0,027 | 0,195 |
| N1' | 0,002 | 0,029 | 0,000 | 0,002 | -0,002 | -7,305 | 0,033 | -0,209 |
| N2' | 0,003 | 0,041 | 0,001 | 0,002 | -0,001 | -5,626 | 0,037 | -0,192 |
| N3' | 0,004 | 0,056 | 0,002 | 0,001 | 0,001 | 4,036 | 0,041 | 0,172 |
| N5' | -0,001 | -0,011 | 0,000 | 0,000 | 0,000 | 0,051 | -0,024 | 0,040 |
| N4' | -0,001 | -0,010 | 0,000 | 0,000 | 0,000 | -0,012 | -0,023 | -0,025 |
| C14' | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,639 | 0,012 | -0,093 |
| C13' | 0,000 | 0,004 | 0,000 | 0,000 | 0,000 | 0,182 | 0,017 | 0,061 |


| C12' | 0,000 | 0,003 | 0,000 | 0,000 | 0,000 | -0,172 | 0,016 | -0,060 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C11' | 0,000 | 0,004 | 0,000 | 0,000 | 0,000 | 0,210 | 0,017 | 0,064 |
| C10' | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,685 | 0,012 | -0,095 |
| C15' | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | 0,030 | -0,007 | 0,033 |
| C17' | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,003 | 0,010 | -0,016 |
| C16' | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,002 | 0,012 | -0,012 |
| C16' | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,001 | 0,012 | -0,012 |
| C1' | 0,000 | 0,002 | 0,000 | 0,000 | 0,000 | -0,518 | 0,014 | -0,087 |
| C2' | 0,000 | 0,004 | 0,000 | 0,000 | 0,000 | 0,160 | 0,018 | 0,059 |
| C3' | 0,000 | 0,003 | 0,000 | 0,000 | 0,000 | -0,146 | 0,015 | -0,057 |
| C4' | 0,000 | 0,005 | 0,000 | 0,000 | 0,000 | 0,169 | 0,018 | 0,060 |
| C5' | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,633 | 0,011 | -0,092 |
| C6' | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | 0,028 | -0,006 | 0,033 |
| C9' | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,002 | 0,011 | -0,014 |
| C8' | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,001 | 0,010 | -0,012 |
| C7' | 0,000 | 0,001 | 0,000 | 0,000 | 0,000 | -0,002 | 0,011 | -0,013 |
| H1 | 0,000 | 0,005 | 0,000 | 0,000 | 0,000 | 0,000 | 0,018 | 0,006 |
| H2 | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | -0,002 | 0,007 | -0,013 |
| H3 | 0,000 | -0,001 | 0,000 | 0,000 | 0,000 | -0,002 | -0,009 | -0,014 |
| H4 | 0,000 | 0,005 | 0,000 | 0,000 | 0,000 | -0,001 | 0,018 | -0,010 |
| H5 | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | -0,002 | -0,008 | -0,013 |
| H6 | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | 0,001 | 0,007 | 0,012 |
| H7 | 0,000 | 0,005 | 0,000 | 0,000 | 0,000 | -0,001 | 0,018 | -0,011 |
| H8 | 0,000 | -0,001 | 0,000 | 0,000 | 0,000 | -0,002 | -0,009 | -0,013 |
| H9 | 0,000 | -0,001 | 0,000 | 0,000 | 0,000 | 0,002 | -0,010 | 0,013 |
| H10 | 0,000 | 0,005 | 0,000 | 0,000 | 0,000 | 0,000 | 0,018 | 0,008 |
| H11 | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | -0,003 | -0,006 | -0,015 |
| H12 | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | -0,002 | 0,004 | -0,014 |
| H13 | 0,000 | 0,005 | 0,000 | 0,000 | 0,000 | -0,001 | 0,018 | -0,011 |
| H14 | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | 0,002 | -0,008 | 0,014 |
| H15 | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | -0,002 | -0,007 | -0,013 |
| H16 | 0,000 | 0,005 | 0,000 | 0,000 | 0,000 | -0,001 | 0,018 | -0,011 |
| H17 | 0,000 | -0,001 | 0,000 | 0,000 | 0,000 | -0,002 | -0,009 | -0,015 |
| H18 | 0,000 | -0,001 | 0,000 | 0,000 | 0,000 | 0,001 | -0,010 | 0,012 |
| H19 | 0,000 | 0,004 | 0,000 | 0,000 | 0,000 | 0,273 | 0,016 | 0,070 |
| H20 | 0,001 | 0,009 | 0,000 | 0,000 | 0,000 | 0,008 | 0,022 | 0,021 |
| H21 | 0,001 | 0,009 | 0,000 | 0,000 | 0,000 | 0,015 | 0,022 | 0,027 |
| H22 | 0,000 | 0,004 | 0,000 | 0,000 | 0,000 | 0,252 | 0,016 | 0,068 |
| H23 | 0,000 | 0,006 | 0,000 | 0,000 | 0,000 | 0,219 | 0,020 | 0,065 |
| H24 | 0,001 | 0,009 | 0,000 | 0,000 | 0,000 | 0,008 | 0,022 | 0,022 |
| H25 | 0,001 | 0,009 | 0,000 | 0,000 | 0,000 | 0,017 | 0,022 | 0,028 |
| H26 | 0,000 | 0,003 | 0,000 | 0,000 | 0,000 | 0,206 | 0,016 | 0,064 |
| H1' | 0,000 | 0,003 | 0,000 | 0,000 | 0,000 | 0,000 | 0,016 | 0,006 |
| H2' | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | -0,001 | 0,006 | -0,012 |
| H3' | 0,000 | -0,001 | 0,000 | 0,000 | 0,000 | -0,002 | -0,012 | -0,013 |
| H4' | 0,000 | 0,003 | 0,000 | 0,000 | 0,000 | -0,001 | 0,015 | -0,010 |
| H5' | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | -0,001 | 0,006 | -0,012 |
| H6' | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | 0,001 | 0,006 | 0,011 |
| H7' | 0,000 | 0,003 | 0,000 | 0,000 | 0,000 | -0,001 | 0,016 | -0,010 |


| H8' | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | -0,001 | -0,004 | -0,012 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H9' | 0,000 | -0,002 | 0,000 | 0,000 | 0,000 | 0,002 | -0,013 | 0,012 |
| H10' | 0,000 | 0,003 | 0,000 | 0,000 | 0,000 | 0,000 | 0,016 | 0,007 |
| H11' | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | -0,002 | 0,008 | -0,013 |
| H12' | 0,000 | -0,001 | 0,000 | 0,000 | 0,000 | -0,002 | -0,010 | -0,013 |
| H13' | 0,000 | 0,003 | 0,000 | 0,000 | 0,000 | -0,001 | 0,015 | -0,010 |
| H14' | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | 0,001 | 0,007 | 0,012 |
| H15' | 0,000 | 0,000 | 0,000 | 0,000 | 0,000 | -0,001 | -0,007 | -0,012 |
| H16' | 0,000 | 0,003 | 0,000 | 0,000 | 0,000 | -0,001 | 0,016 | -0,010 |
| H17' | 0,000 | -0,001 | 0,000 | 0,000 | 0,000 | -0,002 | -0,009 | -0,013 |
| H18' | 0,000 | -0,002 | 0,000 | 0,000 | 0,000 | 0,001 | -0,013 | 0,011 |
| H19' | 0,000 | -0,001 | 0,000 | 0,000 | 0,000 | 0,162 | -0,012 | 0,059 |
| H20' | 0,000 | 0,004 | 0,000 | 0,000 | 0,000 | 0,006 | 0,017 | 0,019 |
| H21' | 0,000 | 0,004 | 0,000 | 0,000 | 0,000 | 0,011 | 0,017 | 0,024 |
| H22' | 0,000 | -0,002 | 0,000 | 0,000 | 0,000 | 0,155 | -0,013 | 0,058 |
| H23' | 0,000 | 0,002 | 0,000 | 0,000 | 0,000 | 0,122 | 0,013 | 0,053 |
| H24' | 0,000 | 0,004 | 0,000 | 0,000 | 0,000 | 0,006 | 0,018 | 0,019 |
| H25' | 0,000 | 0,003 | 0,000 | 0,000 | 0,000 | 0,012 | 0,016 | 0,025 |
| H26' | 0,000 | -0,006 | 0,000 | 0,000 | 0,000 | 0,137 | -0,020 | 0,056 |

Table A2.2: Contributions at the CC near to the Cu 1 atomic basin along on the $\mathrm{Cu} 1-\mathrm{Cu} 1$ ' internuclear axis for the EO
molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic
percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage
for $s(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A 2.1 .

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FSS}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 79.040 | 0.489 | 89.503 | 89.537 | -0.034 | 90.425 | 0.085 | 0.484 |
| N 1 | 0.001 | 0.000 | 0.000 | 0.001 | -0.001 | 3.504 | 0.002 | 0.164 |
| N 2 | 0.002 | 0.000 | 0.000 | 0.002 | -0.001 | 2.910 | 0.003 | 0.154 |
| N 3 | 0.003 | 0.000 | 0.002 | 0.001 | 0.001 | -2.085 | 0.003 | -0.138 |
| N 5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.935 | 0.001 | 0.105 |
| N 4 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.958 | 0.002 | 0.106 |
| C 14 | 0.001 | 0.000 | 0.000 | 0.001 | 0.000 | 0.629 | 0.002 | 0.092 |
| C 13 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.159 | 0.002 | -0.058 |
| C 12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.139 | 0.002 | 0.056 |
| C 11 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.181 | 0.002 | -0.061 |
| C 10 | 0.001 | 0.000 | 0.000 | 0.001 | 0.000 | 0.662 | 0.002 | 0.094 |
| C 15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.022 | 0.000 | -0.030 |
| C 17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.001 | 0.014 |
| C 16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.011 |
| C 16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.011 |
| C 1 | 0.001 | 0.000 | 0.000 | 0.001 | 0.000 | 0.547 | 0.002 | 0.088 |
| C 2 | 0.001 | 0.000 | 0.001 | 0.000 | 0.000 | -0.148 | 0.002 | -0.057 |
| C 3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.119 | 0.002 | 0.053 |
| C 4 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.142 | 0.002 | -0.056 |
| C 5 | 0.001 | 0.000 | 0.000 | 0.001 | 0.000 | 0.581 | 0.002 | 0.090 |
| C 6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.021 | 0.001 | -0.030 |
| C 9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.012 |


| C8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.010 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.012 |
| Cu1' | 0.001 | 0.000 | 0.001 | 0.000 | 0.001 | -2.975 | 0.002 | -0.155 |
| N1' | 0.001 | 0.000 | 0.000 | 0.001 | -0.001 | 3.333 | 0.002 | 0.161 |
| N2' | 0.002 | 0.000 | 0.000 | 0.002 | -0.001 | 3.028 | 0.002 | 0.156 |
| N3' | 0.003 | 0.000 | 0.002 | 0.001 | 0.001 | -2.183 | 0.003 | -0.140 |
| N5' | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.039 | -0.002 | -0.037 |
| N4' | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | -0.002 | -0.018 |
| C14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.338 | 0.001 | 0.075 |
| C13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.097 | 0.001 | -0.050 |
| C12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.092 | 0.001 | 0.049 |
| C11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.112 | 0.001 | -0.052 |
| C10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.363 | 0.001 | 0.077 |
| C15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.016 | 0.000 | -0.027 |
| C17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.001 | 0.013 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.010 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.010 |
| C1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.274 | 0.001 | 0.070 |
| C2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.085 | 0.001 | -0.047 |
| C3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.078 | 0.001 | 0.046 |
| C4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.090 | 0.001 | -0.048 |
| C5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.335 | 0.001 | 0.075 |
| C6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.015 | 0.000 | -0.026 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.011 |
| C8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.009 |
| C7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.011 |
| H1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.005 |
| H2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.010 |
| H3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | 0.012 |
| H4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.009 |
| H5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | 0.011 |
| H6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.001 | -0.010 |
| H7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.009 |
| H8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | 0.011 |
| H9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -0.001 | -0.011 |
| H10 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.007 |
| H11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | 0.012 |
| H12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.000 | 0.012 |
| H13 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.009 |
| H14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -0.001 | -0.011 |
| H15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | 0.011 |
| H16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.009 |
| H17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | 0.012 |
| H18 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -0.001 | -0.010 |
| H19 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.160 | 0.001 | -0.059 |
| H20 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.002 | -0.018 |
| H21 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.009 | 0.002 | -0.022 |
| H22 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.147 | 0.001 | -0.057 |
| H23 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.133 | 0.002 | -0.055 |


| H24 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.002 | -0.018 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H25 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.010 | 0.002 | -0.023 |
| H26 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.117 | 0.001 | -0.053 |
| H1 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.005 |
| H2 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.000 | 0.009 |
| H3 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | 0.011 |
| H4 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.008 |
| H5 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.000 | 0.010 |
| H6 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.000 | -0.009 |
| H7 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.008 |
| H8 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.000 | 0.010 |
| H9 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -0.001 | -0.010 |
| H10 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.006 |
| H11 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.011 |
| H12 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | 0.011 |
| H13 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.008 |
| H14 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.001 | -0.010 |
| H15 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | 0.010 |
| H16 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.001 | 0.009 |
| H17 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | 0.011 |
| H18 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -0.001 | -0.009 |
| H19 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.085 | -0.001 | -0.047 |
| H20 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.001 | -0.016 |
| H21 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.006 | 0.001 | -0.019 |
| H22' $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.082 | -0.001 | -0.047 |
| H23 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.064 | 0.001 | -0.043 |
| H24 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.001 | -0.016 |
| H25 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.007 | 0.001 | -0.020 |
| H26' $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.072 | -0.001 | -0.045 |
|  |  |  |  |  |  |  |  |  |

Table A2.3: Contributions at the Cu1 atomic basin along on the $\mathrm{Cu}-\mathrm{N} 1$ bond for the EO molecular system; $\mathrm{LS}, \mathrm{SF} \%$,
$\mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are
evaluated as in tab A2.1.

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FS}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 0.003 | 0.002 | 0.003 | 0.001 | 0.002 | 0.797 | 0.013 | 0.100 |
| N 1 | 98.301 | 49.554 | 99.272 | 99.028 | 0.244 | 99.532 | 0.396 | 0.499 |
| N 2 | 0.044 | 0.022 | 0.021 | 0.023 | -0.002 | -0.915 | 0.030 | -0.105 |
| N 3 | 0.011 | 0.006 | 0.006 | 0.005 | 0.001 | 0.602 | 0.019 | 0.091 |
| N 5 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.006 | -0.008 | -0.019 |
| N 4 | -0.001 | -0.001 | -0.001 | -0.001 | 0.000 | -0.006 | -0.009 | -0.019 |
| C 14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.058 | 0.005 | -0.042 |
| C 13 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.016 | 0.006 | 0.027 |
| C 12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.015 | 0.005 | -0.027 |
| C 11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.019 | 0.006 | 0.029 |
| C 10 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.062 | 0.005 | -0.043 |
| C 15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.002 | 0.015 |


| C17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.007 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.005 |
| C16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.005 |
| C1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.061 | 0.007 | -0.042 |
| C2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.018 | 0.007 | 0.028 |
| C3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.017 | 0.006 | -0.028 |
| C4 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.021 | 0.007 | 0.030 |
| C5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.084 | -0.002 | -0.047 |
| C6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.001 | 0.016 |
| C9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.007 |
| C8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.005 |
| C7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.006 |
| Cu1' | 0.003 | 0.002 | 0.003 | 0.001 | 0.002 | 0.748 | 0.013 | 0.098 |
| N1' | -0.001 | -0.001 | -0.001 | 0.000 | -0.001 | -0.332 | -0.009 | -0.075 |
| N2' | 0.002 | 0.001 | 0.000 | 0.001 | -0.001 | -0.360 | 0.010 | -0.077 |
| N3' | 0.002 | 0.001 | 0.001 | 0.001 | 0.001 | 0.259 | 0.011 | 0.069 |
| N5' | -0.002 | -0.001 | -0.001 | -0.001 | 0.000 | 0.002 | -0.010 | 0.014 |
| N4' | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.011 | -0.008 | -0.024 |
| C14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.079 | 0.004 | -0.046 |
| C13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.021 | 0.007 | 0.030 |
| C12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.020 | 0.006 | -0.029 |
| C11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.025 | 0.007 | 0.031 |
| C10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.084 | 0.005 | -0.047 |
| C15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.002 | 0.016 |
| C17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.007 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.006 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.006 |
| C1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.050 | 0.004 | -0.040 |
| C2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.015 | 0.006 | 0.027 |
| C3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.013 | 0.005 | -0.025 |
| C4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.015 | 0.006 | 0.026 |
| C5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.055 | 0.005 | -0.041 |
| C6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | -0.002 | 0.014 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.006 |
| C8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.005 |
| C7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.006 |
| H1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | 0.003 |
| H2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.006 |
| H3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | -0.006 |
| H4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.004 |
| H5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.006 |
| H6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.005 |
| H7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.005 |
| H8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.006 |
| H9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.006 |
| H10 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.003 |
| H11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.006 |
| H12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.006 |
| H13 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.004 |


| H14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.006 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.005 |
| H16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.005 |
| H17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.006 |
| H18 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.005 |
| H19 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.015 | -0.004 | 0.027 |
| H20 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | 0.008 |
| H21 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.011 |
| H22 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.014 | -0.005 | 0.026 |
| H23 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.013 | 0.006 | 0.026 |
| H24 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.007 | 0.009 |
| H25 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.012 |
| H26 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.019 | -0.007 | 0.029 |
| H1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.002 |
| H2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.005 |
| H3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.006 |
| H4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.004 |
| H5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.005 |
| H6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.005 |
| H7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.004 |
| H8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.005 |
| H9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.005 |
| H10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | 0.003 |
| H11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.006 |
| H12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.006 |
| H13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.005 |
| H14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.006 |
| H15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.006 |
| H16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.005 |
| H17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.006 |
| H18' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.005 |
| H19' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.019 | 0.005 | 0.029 |
| H20' | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.007 | 0.009 |
| H21' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.007 | 0.012 |
| H22' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.019 | 0.005 | 0.029 |
| H23' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.012 | -0.002 | 0.025 |
| H24' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.009 |
| H25' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.011 |
| H26' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.012 | -0.005 | 0.024 |

Table A2.4: Contributions at the N 1 atomic basin along on the $\mathrm{Cu}-\mathrm{N} 1$ bond for the EO molecular system; $\mathrm{LS}, \mathrm{SF} \%$,
$\mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | SF\% | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | SFs\% | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {SFs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1 | 87.346 | 99.962 | 44.070 | 43.275 | 0.795 | 100.377 | 0.500 | 0.501 |
| N1 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | -0.154 | 0.008 | -0.058 |
| N2 | 0.002 | 0.002 | 0.000 | 0.001 | -0.001 | -0.135 | 0.014 | -0.055 |
| N3 | 0.003 | 0.003 | 0.002 | 0.001 | 0.001 | 0.097 | 0.016 | 0.050 |
| N5 | 0.001 | 0.001 | 0.000 | 0.001 | 0.000 | -0.053 | 0.011 | -0.041 |
| N4 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | -0.045 | 0.009 | -0.038 |
| C14 | 0.001 | 0.001 | 0.000 | 0.001 | 0.000 | -0.031 | 0.012 | -0.034 |
| C13 | 0.001 | 0.001 | 0.001 | 0.000 | 0.000 | 0.008 | 0.011 | 0.021 |
| C12 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | -0.007 | 0.009 | -0.020 |
| C11 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.009 | 0.011 | 0.022 |
| C10 | 0.001 | 0.001 | 0.001 | 0.001 | 0.000 | -0.033 | 0.012 | -0.034 |
| C15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.002 | 0.011 |
| C17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.005 |
| C16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.004 |
| C16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.004 |
| C1 | 0.001 | 0.001 | 0.000 | 0.001 | 0.000 | -0.026 | 0.011 | -0.032 |
| C2 | 0.001 | 0.001 | 0.001 | 0.000 | 0.000 | 0.007 | 0.011 | 0.021 |
| C3 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.006 | 0.009 | -0.019 |
| C4 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.007 | 0.011 | 0.020 |
| C5 | 0.001 | 0.001 | 0.000 | 0.001 | 0.000 | -0.027 | 0.012 | -0.032 |
| C6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.003 | 0.011 |
| C9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.004 |
| C8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.004 |
| C7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.004 |
| Cu1' | 0.001 | 0.001 | 0.001 | 0.000 | 0.001 | 0.139 | 0.010 | 0.056 |
| N1' | 0.001 | 0.001 | 0.000 | 0.001 | -0.001 | -0.158 | 0.011 | -0.058 |
| N2' | 0.002 | 0.002 | 0.000 | 0.001 | -0.001 | -0.147 | 0.014 | -0.057 |
| N3' | 0.003 | 0.004 | 0.002 | 0.001 | 0.001 | 0.106 | 0.017 | 0.051 |
| N5' | -0.001 | -0.001 | 0.000 | 0.000 | 0.000 | 0.002 | -0.010 | 0.013 |
| N4' | -0.001 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.009 | 0.008 |
| C14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.016 | 0.004 | -0.027 |
| C13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.007 | 0.018 |
| C12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.006 | -0.018 |
| C11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.007 | 0.019 |
| C10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.017 | 0.005 | -0.028 |
| C15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.003 | 0.010 |
| C17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.005 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.004 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.003 |
| C1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.013 | 0.005 | -0.025 |
| C2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | 0.007 | 0.017 |
| C3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.006 | -0.017 |
| C4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | 0.007 | 0.018 |
| C5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.016 | 0.004 | -0.027 |
| C6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.003 | 0.010 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.004 |
| C8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.003 |
| C7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.004 |


| H1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.008 | 0.002 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.004 |
| H3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.004 |
| H4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.008 | -0.003 |
| H5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.004 |
| H6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.004 |
| H7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.008 | -0.003 |
| H8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.004 |
| H9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.004 |
| H10 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.008 | 0.002 |
| H11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.004 |
| H12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.004 |
| H13 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.008 | -0.003 |
| H14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.004 |
| H15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.004 |
| H16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.008 | -0.003 |
| H17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.004 |
| H18 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.004 |
| H19 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.008 | 0.009 | 0.021 |
| H20 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | 0.006 |
| H21 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | 0.008 |
| H22 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.007 | 0.009 | 0.021 |
| H23 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.006 | 0.009 | 0.020 |
| H24 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | 0.007 |
| H25 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | 0.008 |
| H26 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.008 | 0.019 |
| H1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | 0.002 |
| H2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.003 |
| H3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | -0.004 |
| H4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.003 |
| H5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.004 |
| H6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.003 |
| H7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | -0.003 |
| H8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.003 |
| H9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 |
| H10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | 0.002 |
| H11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.004 |
| H12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.004 |
| H13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.003 |
| H14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.004 |
| H15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.004 |
| H16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | -0.003 |
| H17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.004 |
| H18' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.003 |
| H19' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.005 | 0.017 |
| H20' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | 0.006 |
| H21' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | 0.007 |
| H22' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.006 | 0.017 |
| H23' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.005 | 0.016 |


| $\mathrm{H} 24^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | 0.006 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{H} 25^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | 0.007 |
| $\mathrm{H}^{\prime} 6^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.008 | 0.016 |

Table A2.5: Contributions at the Cu atomic basin along on the $\mathrm{Cu}-\mathrm{N} 5$ bond for the EO molecular system; $\mathrm{LS}, \mathrm{SF} \%$,
$\mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r})$. $\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | SF\% | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | SFs\% | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {FSs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1 | 0.047 | 47.486 | 0.027 | 0.020 | 0.008 | 311.676 | 0.390 | 0.730 |
| N1 | -0.001 | -0.638 | -0.001 | 0.000 | -0.001 | -29.112 | -0.093 | -0.331 |
| N2 | 0.001 | 0.848 | 0.000 | 0.001 | -0.001 | -35.386 | 0.102 | -0.354 |
| N3 | 0.002 | 2.039 | 0.001 | 0.001 | 0.001 | 25.636 | 0.137 | 0.318 |
| N5 | 0.022 | 22.416 | 0.010 | 0.013 | -0.003 | -116.287 | 0.304 | -0.526 |
| N4 | -0.001 | -0.980 | -0.001 | 0.000 | 0.000 | -7.826 | -0.107 | -0.214 |
| C14 | 0.003 | 3.481 | 0.002 | 0.002 | 0.000 | -13.328 | 0.163 | -0.255 |
| C13 | 0.002 | 1.620 | 0.001 | 0.001 | 0.000 | 3.124 | 0.127 | 0.157 |
| C12 | 0.001 | 0.743 | 0.000 | 0.000 | 0.000 | -2.625 | 0.098 | -0.149 |
| C11 | 0.001 | 1.503 | 0.001 | 0.001 | 0.000 | 3.572 | 0.123 | 0.165 |
| C10 | 0.003 | 3.510 | 0.002 | 0.002 | 0.000 | -13.873 | 0.164 | -0.259 |
| C15 | 0.000 | 0.025 | 0.000 | 0.000 | 0.000 | 0.402 | 0.031 | 0.080 |
| C17 | 0.000 | 0.082 | 0.000 | 0.000 | 0.000 | -0.040 | 0.047 | -0.037 |
| C16 | 0.000 | 0.117 | 0.000 | 0.000 | 0.000 | -0.019 | 0.053 | -0.029 |
| C16 | 0.000 | 0.152 | 0.000 | 0.000 | 0.000 | -0.017 | 0.057 | -0.028 |
| C1 | 0.000 | 0.482 | 0.000 | 0.000 | 0.000 | -8.462 | 0.084 | -0.220 |
| C2 | 0.001 | 0.951 | 0.001 | 0.000 | 0.000 | 2.284 | 0.106 | 0.142 |
| C3 | 0.000 | 0.440 | 0.000 | 0.000 | 0.000 | -1.761 | 0.082 | -0.130 |
| C4 | 0.001 | 0.750 | 0.000 | 0.000 | 0.000 | 1.980 | 0.098 | 0.135 |
| C5 | 0.001 | 0.986 | 0.000 | 0.001 | 0.000 | -7.717 | 0.107 | -0.213 |
| C6 | 0.000 | 0.019 | 0.000 | 0.000 | 0.000 | 0.311 | 0.029 | 0.073 |
| C9 | 0.000 | 0.120 | 0.000 | 0.000 | 0.000 | -0.022 | 0.053 | -0.030 |
| C8 | 0.000 | 0.069 | 0.000 | 0.000 | 0.000 | -0.013 | 0.044 | -0.025 |
| C7 | 0.000 | 0.084 | 0.000 | 0.000 | 0.000 | -0.019 | 0.047 | -0.029 |
| Cu1' | 0.000 | 0.451 | 0.001 | 0.000 | 0.001 | 37.058 | 0.083 | 0.359 |
| N1' | 0.000 | 0.308 | 0.000 | 0.001 | -0.001 | -36.146 | 0.073 | -0.356 |
| N2' | 0.000 | 0.208 | -0.001 | 0.001 | -0.001 | -50.432 | 0.064 | -0.398 |
| N3' | 0.003 | 3.359 | 0.002 | 0.001 | 0.001 | 36.779 | 0.161 | 0.358 |
| N5' | 0.000 | -0.466 | 0.000 | 0.000 | 0.000 | 0.706 | -0.084 | 0.096 |
| N4' | 0.000 | -0.480 | 0.000 | 0.000 | 0.000 | 0.470 | -0.084 | 0.084 |
| C14' | 0.000 | 0.047 | 0.000 | 0.000 | 0.000 | -4.505 | 0.039 | -0.178 |
| C13' | 0.000 | 0.179 | 0.000 | 0.000 | 0.000 | 1.317 | 0.061 | 0.118 |
| C12' | 0.000 | 0.151 | 0.000 | 0.000 | 0.000 | -1.259 | 0.057 | -0.116 |
| C11' | 0.000 | 0.169 | 0.000 | 0.000 | 0.000 | 1.512 | 0.060 | 0.124 |
| C10' | 0.000 | 0.051 | 0.000 | 0.000 | 0.000 | -4.830 | 0.040 | -0.182 |
| C15' | 0.000 | -0.016 | 0.000 | 0.000 | 0.000 | 0.222 | -0.027 | 0.065 |
| C17' | 0.000 | 0.053 | 0.000 | 0.000 | 0.000 | -0.023 | 0.040 | -0.031 |
| C16' | 0.000 | 0.084 | 0.000 | 0.000 | 0.000 | -0.012 | 0.047 | -0.024 |
| C16' | 0.000 | 0.074 | 0.000 | 0.000 | 0.000 | -0.010 | 0.045 | -0.023 |


| C1' | 0.000 | 0.096 | 0.000 | 0.000 | 0.000 | -3.900 | 0.049 | -0.170 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C2' | 0.000 | 0.221 | 0.000 | 0.000 | 0.000 | 1.234 | 0.065 | 0.116 |
| C3' | 0.000 | 0.151 | 0.000 | 0.000 | 0.000 | -1.164 | 0.057 | -0.113 |
| C4' | 0.000 | 0.202 | 0.000 | 0.000 | 0.000 | 1.337 | 0.063 | 0.119 |
| C5' | 0.000 | -0.027 | 0.000 | 0.000 | 0.000 | -4.899 | -0.032 | -0.183 |
| C6' | 0.000 | -0.016 | 0.000 | 0.000 | 0.000 | 0.223 | -0.027 | 0.065 |
| C9' | 0.000 | 0.071 | 0.000 | 0.000 | 0.000 | -0.017 | 0.045 | -0.028 |
| C8' | 0.000 | 0.059 | 0.000 | 0.000 | 0.000 | -0.010 | 0.042 | -0.023 |
| C7' | 0.000 | 0.057 | 0.000 | 0.000 | 0.000 | -0.014 | 0.041 | -0.026 |
| H1 | 0.000 | 0.292 | 0.000 | 0.000 | 0.000 | 0.001 | 0.071 | 0.012 |
| H2 | 0.000 | 0.011 | 0.000 | 0.000 | 0.000 | -0.013 | 0.024 | -0.025 |
| H3 | 0.000 | 0.020 | 0.000 | 0.000 | 0.000 | -0.018 | 0.029 | -0.028 |
| H4 | 0.000 | 0.329 | 0.000 | 0.000 | 0.000 | -0.008 | 0.074 | -0.021 |
| H5 | 0.000 | -0.088 | 0.000 | 0.000 | 0.000 | -0.018 | -0.048 | -0.028 |
| H6 | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | 0.011 | 0.014 | 0.024 |
| H7 | 0.000 | 0.320 | 0.000 | 0.000 | 0.000 | -0.008 | 0.074 | -0.022 |
| H8 | 0.000 | -0.082 | 0.000 | 0.000 | 0.000 | -0.016 | -0.047 | -0.027 |
| H9 | 0.000 | 0.006 | 0.000 | 0.000 | 0.000 | 0.016 | 0.020 | 0.027 |
| H10 | 0.000 | 0.407 | 0.000 | 0.000 | 0.000 | 0.004 | 0.080 | 0.017 |
| H11 | 0.000 | -0.004 | 0.000 | 0.000 | 0.000 | -0.026 | -0.018 | -0.032 |
| H12 | 0.000 | 0.040 | 0.000 | 0.000 | 0.000 | -0.022 | 0.037 | -0.030 |
| H13 | 0.000 | 0.419 | 0.000 | 0.000 | 0.000 | -0.009 | 0.081 | -0.023 |
| H14 | 0.000 | -0.026 | 0.000 | 0.000 | 0.000 | 0.020 | -0.032 | 0.029 |
| H15 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.019 | 0.012 | -0.029 |
| H16 | 0.000 | 0.416 | 0.000 | 0.000 | 0.000 | -0.011 | 0.080 | -0.024 |
| H17 | 0.000 | -0.019 | 0.000 | 0.000 | 0.000 | -0.025 | -0.029 | -0.031 |
| H18 | 0.000 | -0.030 | 0.000 | 0.000 | 0.000 | 0.013 | -0.034 | 0.025 |
| H19 | 0.002 | 1.628 | 0.001 | 0.001 | 0.000 | 3.049 | 0.127 | 0.156 |
| H20 | 0.001 | 0.974 | 0.000 | 0.000 | 0.000 | 0.085 | 0.107 | 0.047 |
| H21 | 0.001 | 0.942 | 0.000 | 0.000 | 0.000 | 0.162 | 0.106 | 0.059 |
| H22 | 0.002 | 1.577 | 0.001 | 0.001 | 0.000 | 2.836 | 0.125 | 0.152 |
| H23 | 0.000 | 0.037 | 0.000 | 0.000 | 0.000 | 2.260 | 0.036 | 0.141 |
| H24 | 0.001 | 0.585 | 0.000 | 0.000 | 0.000 | 0.070 | 0.090 | 0.044 |
| H25 | 0.001 | 0.572 | 0.000 | 0.000 | 0.000 | 0.139 | 0.089 | 0.056 |
| H26 | 0.000 | 0.457 | 0.000 | 0.000 | 0.000 | 1.497 | 0.083 | 0.123 |
| H1' | 0.000 | 0.195 | 0.000 | 0.000 | 0.000 | 0.001 | 0.063 | 0.011 |
| H2' | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | -0.010 | 0.027 | -0.024 |
| H3' | 0.000 | -0.123 | 0.000 | 0.000 | 0.000 | -0.015 | -0.054 | -0.027 |
| H4' | 0.000 | 0.167 | 0.000 | 0.000 | 0.000 | -0.006 | 0.059 | -0.019 |
| H5' | 0.000 | 0.025 | 0.000 | 0.000 | 0.000 | -0.011 | 0.031 | -0.024 |
| H6' | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | 0.008 | 0.026 | 0.021 |
| H7' | 0.000 | 0.197 | 0.000 | 0.000 | 0.000 | -0.006 | 0.063 | -0.020 |
| H8' | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | -0.011 | 0.026 | -0.024 |
| H9' | 0.000 | -0.132 | 0.000 | 0.000 | 0.000 | 0.013 | -0.055 | 0.025 |
| H10' | 0.000 | 0.165 | 0.000 | 0.000 | 0.000 | 0.002 | 0.059 | 0.015 |
| H11' | 0.000 | 0.017 | 0.000 | 0.000 | 0.000 | -0.015 | 0.028 | -0.026 |
| H12' | 0.000 | -0.046 | 0.000 | 0.000 | 0.000 | -0.013 | -0.039 | -0.026 |
| H13' | 0.000 | 0.159 | 0.000 | 0.000 | 0.000 | -0.006 | 0.058 | -0.019 |
| H14' | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | 0.011 | 0.021 | 0.024 |


| H15' | 0.000 | -0.019 | 0.000 | 0.000 | 0.000 | -0.011 | -0.029 | -0.024 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H16' | 0.000 | 0.179 | 0.000 | 0.000 | 0.000 | -0.007 | 0.061 | -0.021 |
| H17' | 0.000 | -0.039 | 0.000 | 0.000 | 0.000 | -0.015 | -0.036 | -0.026 |
| H18' | 0.000 | -0.089 | 0.000 | 0.000 | 0.000 | 0.007 | -0.048 | 0.021 |
| H19' | 0.000 | -0.116 | 0.000 | 0.000 | 0.000 | 1.136 | -0.053 | 0.112 |
| H20' | 0.000 | 0.200 | 0.000 | 0.000 | 0.000 | 0.041 | 0.063 | 0.037 |
| H21' | 0.000 | 0.189 | 0.000 | 0.000 | 0.000 | 0.081 | 0.062 | 0.047 |
| H22' | 0.000 | -0.131 | 0.000 | 0.000 | 0.000 | 1.090 | -0.055 | 0.111 |
| H23' | 0.000 | 0.121 | 0.000 | 0.000 | 0.000 | 0.894 | 0.053 | 0.104 |
| H24' | 0.000 | 0.257 | 0.000 | 0.000 | 0.000 | 0.045 | 0.068 | 0.038 |
| H25' | 0.000 | 0.150 | 0.000 | 0.000 | 0.000 | 0.101 | 0.057 | 0.050 |
| H26' | 0.000 | -0.427 | 0.000 | 0.000 | 0.000 | 1.063 | -0.081 | 0.110 |

Table A2.6: Contributions at bcp along on the $\mathrm{Cu}-\mathrm{N} 5$ bond for the EO molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}$,
$\mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | SF\% | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | SFs\% | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {FSS }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1 | 0.004 | 0.002 | 0.003 | 0.001 | 0.001 | 1.032 | 0.013 | 0.109 |
| N1 | -0.001 | 0.000 | -0.001 | 0.000 | 0.000 | -0.314 | -0.007 | -0.073 |
| N2 | 0.000 | 0.000 | 0.000 | 0.001 | -0.001 | -0.482 | 0.006 | -0.084 |
| N3 | 0.001 | 0.001 | 0.001 | 0.000 | 0.001 | 0.352 | 0.009 | 0.076 |
| N5 | 98.174 | 49.524 | 99.159 | 99.014 | 0.145 | 100.197 | 0.396 | 0.500 |
| N4 | -0.001 | -0.001 | -0.001 | -0.001 | 0.000 | -0.023 | -0.009 | -0.031 |
| C14 | 0.015 | 0.008 | 0.007 | 0.008 | 0.000 | -0.343 | 0.021 | -0.075 |
| C13 | 0.003 | 0.002 | 0.002 | 0.002 | 0.000 | 0.077 | 0.013 | 0.046 |
| C12 | 0.001 | 0.001 | 0.001 | 0.001 | 0.000 | -0.063 | 0.010 | -0.043 |
| C11 | 0.003 | 0.002 | 0.002 | 0.002 | 0.000 | 0.089 | 0.013 | 0.048 |
| C10 | 0.016 | 0.008 | 0.008 | 0.008 | -0.001 | -0.349 | 0.021 | -0.076 |
| C15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.009 | 0.004 | 0.022 |
| C17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.004 | -0.010 |
| C16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.008 |
| C16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.008 |
| C1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.129 | -0.005 | -0.054 |
| C2 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.037 | 0.008 | 0.036 |
| C3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.028 | 0.006 | -0.033 |
| C4 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.029 | 0.007 | 0.033 |
| C5 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.108 | 0.007 | -0.051 |
| C6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.002 | 0.018 |
| C9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.008 |
| C8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.006 |
| C7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.007 |
| Cu1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.500 | 0.005 | 0.086 |
| N1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.317 | 0.006 | -0.073 |
| N2' | -0.001 | -0.001 | -0.001 | 0.000 | -0.001 | -0.854 | -0.010 | -0.102 |
| N3' | 0.002 | 0.001 | 0.002 | 0.001 | 0.001 | 0.638 | 0.011 | 0.093 |
| N5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.013 | -0.006 | 0.026 |
| N4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.013 | -0.006 | 0.025 |


| C14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.066 | 0.003 | -0.044 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.020 | 0.004 | 0.029 |
| C12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.019 | 0.004 | -0.029 |
| C11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.023 | 0.004 | 0.030 |
| C10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.071 | 0.003 | -0.045 |
| C15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.002 | 0.016 |
| C17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.008 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.006 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.006 |
| C1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.060 | 0.004 | -0.042 |
| C2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.019 | 0.005 | 0.029 |
| C3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.019 | 0.004 | -0.029 |
| C4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.021 | 0.004 | 0.030 |
| C5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.077 | -0.004 | -0.046 |
| C6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.002 | 0.017 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.007 |
| C8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.006 |
| C7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.007 |
| H1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.003 |
| H2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.006 |
| H3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.007 |
| H4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.005 |
| H5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | -0.007 |
| H6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.006 |
| H7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.005 |
| H8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.007 |
| H9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.007 |
| H10 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | 0.005 |
| H11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.003 | -0.009 |
| H12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.008 |
| H13 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | -0.006 |
| H14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.008 |
| H15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.008 |
| H16 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | -0.007 |
| H17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.003 | -0.009 |
| H18 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.007 |
| H19 | 0.004 | 0.002 | 0.002 | 0.002 | 0.000 | 0.058 | 0.014 | 0.042 |
| H20 | 0.002 | 0.001 | 0.001 | 0.001 | 0.000 | 0.002 | 0.010 | 0.014 |
| H21 | 0.002 | 0.001 | 0.001 | 0.001 | 0.000 | 0.004 | 0.010 | 0.017 |
| H22 | 0.004 | 0.002 | 0.002 | 0.002 | 0.000 | 0.058 | 0.014 | 0.042 |
| H23 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.037 | -0.007 | 0.036 |
| H24 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.011 |
| H25 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.007 | 0.014 |
| H26 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.020 | 0.006 | 0.029 |
| H1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.003 |
| H2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | -0.006 |
| H3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | -0.007 |
| H4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.005 |
| H5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.006 |


| H6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.005 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.005 |
| H8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.006 |
| H9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.006 |
| H10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | 0.004 |
| H11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | -0.007 |
| H12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.006 |
| H13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.005 |
| H14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 |
| H15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.006 |
| H16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.005 |
| H17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.007 |
| H18' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.005 |
| H19' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.017 | -0.004 | 0.027 |
| H20' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.009 |
| H21' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.012 |
| H22' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.016 | -0.004 | 0.027 |
| H23' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.014 | 0.004 | 0.026 |
| H24' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.010 |
| H25' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.004 | 0.013 |
| H26' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.017 | -0.006 | 0.027 |

Table A2.7: Contributions at the N5 atomic basin along on the Cu-N5 bond for the EO molecular system; LS, SF\%,
$\mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{s}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local
source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FS}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 0.002 | 0.364 | 0.002 | 0.000 | 0.002 | 219.550 | 0.077 | 0.650 |
| N 1 | 0.233 | 50.306 | 0.117 | 0.116 | 0.001 | 166.644 | 0.398 | 0.593 |
| N 2 | 0.199 | 43.000 | 0.097 | 0.101 | -0.004 | -555.920 | 0.377 | -0.886 |
| N 3 | 0.020 | 4.331 | 0.011 | 0.009 | 0.002 | 286.863 | 0.176 | 0.710 |
| N 5 | -0.001 | -0.130 | 0.000 | 0.000 | 0.000 | -0.551 | -0.055 | -0.088 |
| N 4 | -0.001 | -0.292 | -0.001 | -0.001 | 0.000 | 1.705 | -0.071 | 0.129 |
| C 14 | 0.000 | 0.035 | 0.000 | 0.000 | 0.000 | -18.887 | 0.035 | -0.287 |
| C 13 | 0.000 | 0.064 | 0.000 | 0.000 | 0.000 | 5.375 | 0.043 | 0.189 |
| C 12 | 0.000 | 0.045 | 0.000 | 0.000 | 0.000 | -5.007 | 0.038 | -0.184 |
| C 11 | 0.000 | 0.058 | 0.000 | 0.000 | 0.000 | 6.162 | 0.042 | 0.197 |
| C 10 | 0.000 | 0.034 | 0.000 | 0.000 | 0.000 | -20.360 | 0.035 | -0.294 |
| C 15 | 0.000 | -0.003 | 0.000 | 0.000 | 0.000 | 0.865 | -0.016 | 0.103 |
| C 17 | 0.000 | 0.011 | 0.000 | 0.000 | 0.000 | -0.089 | 0.024 | -0.048 |
| C 16 | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | -0.044 | 0.027 | -0.038 |
| C 16 | 0.000 | 0.019 | 0.000 | 0.000 | 0.000 | -0.039 | 0.029 | -0.037 |
| C 1 | 0.000 | 0.095 | 0.000 | 0.000 | 0.000 | -21.177 | 0.049 | -0.298 |
| C 2 | 0.000 | 0.100 | 0.000 | 0.000 | 0.000 | 6.423 | 0.050 | 0.200 |
| C 3 | 0.000 | 0.068 | 0.000 | 0.000 | 0.000 | -6.059 | 0.044 | -0.196 |
| C 4 | 0.001 | 0.124 | 0.000 | 0.000 | 0.000 | 7.667 | 0.054 | 0.212 |
| C 5 | 0.000 | -0.075 | 0.000 | 0.000 | 0.000 | -30.455 | -0.045 | -0.336 |


| C6 | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | 1.098 | -0.010 | 0.111 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C9 | 0.000 | 0.022 | 0.000 | 0.000 | 0.000 | -0.084 | 0.030 | -0.047 |
| C8 | 0.000 | 0.021 | 0.000 | 0.000 | 0.000 | -0.049 | 0.030 | -0.039 |
| C7 | 0.000 | 0.015 | 0.000 | 0.000 | 0.000 | -0.065 | 0.026 | -0.043 |
| Cu1' | 0.002 | 0.421 | 0.002 | 0.000 | 0.001 | 212.758 | 0.081 | 0.643 |
| N1' | -0.001 | -0.232 | -0.001 | 0.000 | -0.001 | -92.506 | -0.066 | -0.487 |
| N2' | 0.001 | 0.222 | 0.000 | 0.001 | -0.001 | -112.821 | 0.065 | -0.521 |
| N3' | 0.002 | 0.389 | 0.001 | 0.001 | 0.001 | 81.723 | 0.079 | 0.467 |
| N5' | -0.002 | -0.471 | -0.001 | -0.001 | 0.000 | 5.143 | -0.084 | 0.186 |
| N4' | -0.001 | -0.140 | 0.000 | 0.000 | 0.000 | -2.534 | -0.056 | -0.147 |
| C14' | 0.000 | -0.012 | 0.000 | 0.000 | 0.000 | -29.178 | -0.025 | -0.332 |
| C13' | 0.000 | 0.094 | 0.000 | 0.000 | 0.000 | 7.937 | 0.049 | 0.215 |
| C12' | 0.000 | 0.064 | 0.000 | 0.000 | 0.000 | -7.301 | 0.043 | -0.209 |
| C11' | 0.000 | 0.092 | 0.000 | 0.000 | 0.000 | 9.148 | 0.049 | 0.225 |
| C10' | 0.000 | 0.007 | 0.000 | 0.000 | 0.000 | -30.607 | 0.021 | -0.337 |
| C15' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 1.203 | -0.013 | 0.115 |
| C17' | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | -0.120 | 0.027 | -0.053 |
| C16' | 0.000 | 0.030 | 0.000 | 0.000 | 0.000 | -0.061 | 0.034 | -0.042 |
| C16' | 0.000 | 0.023 | 0.000 | 0.000 | 0.000 | -0.049 | 0.031 | -0.039 |
| C1' | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | -16.634 | 0.026 | -0.275 |
| C2' | 0.000 | 0.069 | 0.000 | 0.000 | 0.000 | 5.046 | 0.044 | 0.185 |
| C3' | 0.000 | 0.043 | 0.000 | 0.000 | 0.000 | -4.346 | 0.038 | -0.176 |
| C4' | 0.000 | 0.069 | 0.000 | 0.000 | 0.000 | 4.825 | 0.044 | 0.182 |
| C5' | 0.000 | 0.042 | 0.000 | 0.000 | 0.000 | -17.919 | 0.037 | -0.282 |
| C6' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.816 | -0.013 | 0.101 |
| C9' | 0.000 | 0.017 | 0.000 | 0.000 | 0.000 | -0.060 | 0.028 | -0.042 |
| C8' | 0.000 | 0.011 | 0.000 | 0.000 | 0.000 | -0.035 | 0.024 | -0.035 |
| C7' | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | -0.052 | 0.026 | -0.040 |
| H1 | 0.000 | 0.070 | 0.000 | 0.000 | 0.000 | 0.006 | 0.044 | 0.019 |
| H2 | 0.000 | 0.013 | 0.000 | 0.000 | 0.000 | -0.050 | 0.025 | -0.040 |
| H3 | 0.000 | -0.043 | 0.000 | 0.000 | 0.000 | -0.075 | -0.038 | -0.046 |
| H4 | 0.000 | 0.057 | 0.000 | 0.000 | 0.000 | -0.026 | 0.042 | -0.032 |
| H5 | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | -0.052 | 0.025 | -0.040 |
| H6 | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | 0.036 | 0.025 | 0.035 |
| H7 | 0.000 | 0.072 | 0.000 | 0.000 | 0.000 | -0.030 | 0.045 | -0.033 |
| H8 | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | -0.051 | 0.024 | -0.040 |
| H9 | 0.000 | -0.047 | 0.000 | 0.000 | 0.000 | 0.063 | -0.039 | 0.043 |
| H10 | 0.000 | 0.042 | 0.000 | 0.000 | 0.000 | 0.009 | 0.037 | 0.023 |
| H11 | 0.000 | -0.006 | 0.000 | 0.000 | 0.000 | -0.058 | -0.019 | -0.042 |
| H12 | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | -0.051 | -0.013 | -0.040 |
| H13 | 0.000 | 0.042 | 0.000 | 0.000 | 0.000 | -0.022 | 0.038 | -0.030 |
| H14 | 0.000 | -0.008 | 0.000 | 0.000 | 0.000 | 0.045 | -0.021 | 0.038 |
| H15 | 0.000 | -0.005 | 0.000 | 0.000 | 0.000 | -0.043 | -0.018 | -0.038 |
| H16 | 0.000 | 0.042 | 0.000 | 0.000 | 0.000 | -0.026 | 0.037 | -0.032 |
| H17 | 0.000 | -0.007 | 0.000 | 0.000 | 0.000 | -0.055 | -0.020 | -0.041 |
| H18 | 0.000 | -0.009 | 0.000 | 0.000 | 0.000 | 0.028 | -0.022 | 0.033 |
| H19 | 0.000 | -0.031 | 0.000 | 0.000 | 0.000 | 4.872 | -0.034 | 0.183 |
| H20 | 0.000 | 0.057 | 0.000 | 0.000 | 0.000 | 0.161 | 0.042 | 0.059 |
| H21 | 0.000 | 0.054 | 0.000 | 0.000 | 0.000 | 0.321 | 0.041 | 0.074 |


| H22 | 0.000 | -0.037 | 0.000 | 0.000 | 0.000 | 4.660 | -0.036 | 0.180 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H23 | 0.000 | 0.100 | 0.000 | 0.000 | 0.000 | 4.549 | 0.050 | 0.178 |
| H24 | 0.001 | 0.110 | 0.000 | 0.000 | 0.000 | 0.226 | 0.052 | 0.066 |
| H25 | 0.000 | 0.094 | 0.000 | 0.000 | 0.000 | 0.534 | 0.049 | 0.087 |
| H26 | -0.001 | -0.146 | 0.000 | 0.000 | 0.000 | 6.757 | -0.057 | 0.204 |
| H1' | 0.000 | 0.041 | 0.000 | 0.000 | 0.000 | 0.004 | 0.037 | 0.017 |
| H2' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | -0.036 | -0.010 | -0.036 |
| H3' | 0.000 | -0.006 | 0.000 | 0.000 | 0.000 | -0.050 | -0.019 | -0.040 |
| H4' | 0.000 | 0.043 | 0.000 | 0.000 | 0.000 | -0.021 | 0.038 | -0.030 |
| H5' | 0.000 | -0.008 | 0.000 | 0.000 | 0.000 | -0.045 | -0.022 | -0.038 |
| H6' | 0.000 | -0.003 | 0.000 | 0.000 | 0.000 | 0.029 | -0.016 | 0.033 |
| H7' | 0.000 | 0.044 | 0.000 | 0.000 | 0.000 | -0.022 | 0.038 | -0.030 |
| H8' | 0.000 | -0.009 | 0.000 | 0.000 | 0.000 | -0.040 | -0.023 | -0.037 |
| H9' | 0.000 | -0.008 | 0.000 | 0.000 | 0.000 | 0.043 | -0.022 | 0.038 |
| H10' | 0.000 | 0.067 | 0.000 | 0.000 | 0.000 | 0.012 | 0.044 | 0.025 |
| H11' | 0.000 | 0.021 | 0.000 | 0.000 | 0.000 | -0.074 | 0.030 | -0.045 |
| H12' | 0.000 | -0.019 | 0.000 | 0.000 | 0.000 | -0.070 | -0.029 | -0.044 |
| H13' | 0.000 | 0.061 | 0.000 | 0.000 | 0.000 | -0.028 | 0.042 | -0.033 |
| H14' | 0.000 | 0.017 | 0.000 | 0.000 | 0.000 | 0.056 | 0.028 | 0.041 |
| H15' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | -0.056 | -0.013 | -0.041 |
| H16' | 0.000 | 0.079 | 0.000 | 0.000 | 0.000 | -0.036 | 0.046 | -0.036 |
| H17' | 0.000 | -0.012 | 0.000 | 0.000 | 0.000 | -0.080 | -0.025 | -0.046 |
| H18' | 0.000 | -0.047 | 0.000 | 0.000 | 0.000 | 0.041 | -0.039 | 0.037 |
| H19' | 0.000 | 0.064 | 0.000 | 0.000 | 0.000 | 6.970 | 0.043 | 0.206 |
| H20' | 0.001 | 0.118 | 0.000 | 0.000 | 0.000 | 0.244 | 0.053 | 0.067 |
| H21' | 0.001 | 0.113 | 0.000 | 0.000 | 0.000 | 0.452 | 0.052 | 0.083 |
| H22' | 0.000 | 0.064 | 0.000 | 0.000 | 0.000 | 6.584 | 0.043 | 0.202 |
| H23' | 0.000 | -0.016 | 0.000 | 0.000 | 0.000 | 4.185 | -0.027 | 0.174 |
| H24' | 0.000 | 0.057 | 0.000 | 0.000 | 0.000 | 0.170 | 0.042 | 0.060 |
| H25' | 0.000 | 0.055 | 0.000 | 0.000 | 0.000 | 0.358 | 0.041 | 0.077 |
| H26' | 0.000 | -0.027 | 0.000 | 0.000 | 0.000 | 3.722 | -0.032 | 0.167 |

Table A2.8: Contributions at the bcp along on the $\mathrm{N} 1-\mathrm{N} 2$ bond for the EO molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}$,
$\mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r})$. $\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FSs}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 0.001 | 0.000 | 0.001 | 0.000 | 0.001 | 15.280 | 0.008 | 0.267 |
| N 1 | 0.044 | 0.022 | 0.022 | 0.022 | 0.001 | 8.058 | 0.030 | 0.216 |
| N 2 | 98.305 | 49.547 | 99.154 | 99.151 | 0.003 | 34.376 | 0.396 | 0.350 |
| N 3 | 0.054 | 0.027 | 0.029 | 0.025 | 0.003 | 44.342 | 0.032 | 0.381 |
| N 5 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.075 | -0.007 | 0.045 |
| N 4 | -0.001 | -0.001 | -0.001 | -0.001 | 0.000 | 0.491 | -0.009 | 0.085 |
| C 14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.551 | 0.004 | -0.125 |
| C 13 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.449 | 0.005 | 0.082 |
| C 12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.423 | 0.005 | -0.081 |
| C 11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.515 | 0.005 | 0.086 |


| C10 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.681 | 0.004 | -0.128 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.074 | -0.002 | 0.045 |
| C17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.008 | 0.003 | -0.021 |
| C16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.004 | -0.017 |
| C16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.004 | -0.016 |
| C1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.855 | 0.006 | -0.132 |
| C2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.577 | 0.006 | 0.090 |
| C3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.564 | 0.006 | -0.089 |
| C4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.714 | 0.006 | 0.096 |
| C5 | -0.001 | 0.000 | -0.001 | 0.000 | 0.000 | -2.759 | -0.008 | -0.151 |
| C6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.103 | -0.002 | 0.050 |
| C9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.008 | 0.004 | -0.022 |
| C8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.018 |
| C7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.006 | 0.004 | -0.020 |
| Cu1' | 0.001 | 0.000 | 0.001 | 0.000 | 0.001 | 15.083 | 0.008 | 0.266 |
| N1' | -0.001 | 0.000 | -0.001 | 0.000 | -0.001 | -6.549 | -0.008 | -0.202 |
| N2' | 0.001 | 0.000 | 0.000 | 0.001 | -0.001 | -8.985 | 0.007 | -0.224 |
| N3' | 0.001 | 0.001 | 0.001 | 0.000 | 0.001 | 6.543 | 0.010 | 0.201 |
| N5' | -0.002 | -0.001 | -0.001 | -0.001 | 0.000 | 0.897 | -0.011 | 0.104 |
| N4' | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.097 | -0.007 | -0.050 |
| C14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -2.705 | -0.006 | -0.150 |
| C13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.751 | 0.006 | 0.098 |
| C12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.700 | 0.005 | -0.096 |
| C11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.857 | 0.006 | 0.102 |
| C10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -2.792 | -0.005 | -0.152 |
| C15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.115 | -0.002 | 0.052 |
| C17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.011 | 0.004 | -0.024 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.006 | 0.005 | -0.019 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.018 |
| C1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.398 | 0.002 | -0.120 |
| C2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.429 | 0.006 | 0.081 |
| C3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.370 | 0.005 | -0.077 |
| C4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.404 | 0.006 | 0.080 |
| C5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.477 | 0.005 | -0.123 |
| C6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.070 | -0.002 | 0.044 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.019 |
| C8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.003 | -0.016 |
| C7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.003 | -0.018 |
| H1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.009 |
| H2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.018 |
| H3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.007 | -0.006 | -0.021 |
| H4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.006 | -0.014 |
| H5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.018 |
| H6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.004 | 0.016 |
| H7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.006 | -0.015 |
| H8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.018 |
| H9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | -0.006 | 0.020 |
| H10 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.010 |
| H11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | -0.003 | -0.018 |


| H12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.001 | -0.018 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H13 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.005 | -0.013 |
| H14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.003 | 0.017 |
| H15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.002 | -0.017 |
| H16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.005 | -0.014 |
| H17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | -0.003 | -0.018 |
| H18 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | -0.003 | 0.014 |
| H19 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.397 | -0.004 | 0.079 |
| H20 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.014 | 0.005 | 0.026 |
| H21 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.027 | 0.005 | 0.032 |
| H22 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.384 | -0.005 | 0.078 |
| H23 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.389 | 0.007 | 0.079 |
| H24 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.021 | 0.007 | 0.030 |
| H25 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.051 | 0.006 | 0.040 |
| H26 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.603 | -0.008 | 0.091 |
| H1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.008 |
| H2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.002 | -0.016 |
| H3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.002 | -0.017 |
| H4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.005 | -0.013 |
| H5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.003 | -0.017 |
| H6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.002 | 0.015 |
| H7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.005 | -0.013 |
| H8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.003 | -0.016 |
| H9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.002 | 0.017 |
| H10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.011 |
| H11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.007 | 0.004 | -0.021 |
| H12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.007 | -0.004 | -0.020 |
| H13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.006 | -0.015 |
| H14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.004 | 0.019 |
| H15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | -0.001 | -0.019 |
| H16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.006 | -0.016 |
| H17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.008 | -0.003 | -0.021 |
| H18' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.006 | 0.017 |
| H19' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.623 | 0.006 | 0.092 |
| H20' | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.024 | 0.007 | 0.031 |
| H21' | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.043 | 0.007 | 0.038 |
| H22' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.579 | 0.006 | 0.090 |
| H23' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.354 | -0.004 | 0.076 |
| H24' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.015 | 0.005 | 0.026 |
| H25' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.030 | 0.005 | 0.034 |
| H26' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.304 | -0.004 | 0.072 |

Table A2.9: Contributions at the N2 atomic basin along on the N1-N2 bond for the EO molecular system; LS, SF\%,
$\mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local
source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r})$. $\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | SF\% | $\mathrm{LS}_{\alpha}$ | LS ${ }_{\beta}$ | LSs | SFs\% | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {FSs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1 | 0.000 | 0.081 | 0.001 | 0.000 | 0.001 | 87.276 | 0.047 | 0.478 |
| N1 | 0.016 | 3.094 | 0.008 | 0.008 | 0.000 | 9.512 | 0.157 | 0.228 |
| N2 | 0.232 | 45.300 | 0.113 | 0.119 | -0.006 | -579.053 | 0.384 | -0.898 |
| N3 | 0.260 | 50.777 | 0.133 | 0.127 | 0.006 | 598.104 | 0.399 | 0.908 |
| N5 | 0.000 | -0.086 | 0.000 | 0.000 | 0.000 | 1.082 | -0.048 | 0.111 |
| N4 | -0.001 | -0.137 | 0.000 | 0.000 | 0.000 | 4.736 | -0.056 | 0.181 |
| C14 | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | -9.963 | 0.027 | -0.232 |
| C13 | 0.000 | 0.039 | 0.000 | 0.000 | 0.000 | 2.921 | 0.037 | 0.154 |
| C12 | 0.000 | 0.030 | 0.000 | 0.000 | 0.000 | -2.779 | 0.033 | -0.151 |
| C11 | 0.000 | 0.034 | 0.000 | 0.000 | 0.000 | 3.360 | 0.035 | 0.161 |
| C10 | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | -10.833 | 0.026 | -0.238 |
| C15 | 0.000 | -0.003 | 0.000 | 0.000 | 0.000 | 0.490 | -0.016 | 0.085 |
| C17 | 0.000 | 0.009 | 0.000 | 0.000 | 0.000 | -0.051 | 0.023 | -0.040 |
| C16 | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | -0.025 | 0.025 | -0.032 |
| C16 | 0.000 | 0.015 | 0.000 | 0.000 | 0.000 | -0.023 | 0.027 | -0.030 |
| C1 | 0.000 | 0.055 | 0.000 | 0.000 | 0.000 | -12.356 | 0.041 | -0.249 |
| C2 | 0.000 | 0.063 | 0.000 | 0.000 | 0.000 | 3.945 | 0.043 | 0.170 |
| C3 | 0.000 | 0.044 | 0.000 | 0.000 | 0.000 | -3.994 | 0.038 | -0.171 |
| C4 | 0.000 | 0.023 | 0.000 | 0.000 | 0.000 | 4.972 | 0.030 | 0.184 |
| C5 | -0.001 | -0.208 | -0.001 | 0.000 | 0.000 | -18.511 | -0.064 | -0.285 |
| C6 | 0.000 | -0.004 | 0.000 | 0.000 | 0.000 | 0.739 | -0.018 | 0.097 |
| C9 | 0.000 | 0.022 | 0.000 | 0.000 | 0.000 | -0.058 | 0.030 | -0.042 |
| C8 | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | -0.043 | 0.026 | -0.038 |
| C7 | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | -0.043 | 0.026 | -0.038 |
| Cu1' | 0.001 | 0.104 | 0.001 | 0.000 | 0.001 | 87.037 | 0.051 | 0.477 |
| N1' | -0.001 | -0.138 | -0.001 | 0.000 | 0.000 | -37.742 | -0.056 | -0.361 |
| N2' | 0.000 | 0.087 | 0.000 | 0.001 | -0.001 | -56.554 | 0.048 | -0.413 |
| N3' | 0.001 | 0.221 | 0.001 | 0.000 | 0.000 | 41.353 | 0.065 | 0.373 |
| N5' | -0.002 | -0.351 | -0.001 | -0.001 | 0.000 | 8.029 | -0.076 | 0.216 |
| N4' | -0.001 | -0.098 | 0.000 | 0.000 | 0.000 | -0.020 | -0.050 | -0.029 |
| C14' | -0.001 | -0.131 | 0.000 | 0.000 | 0.000 | -18.760 | -0.055 | -0.286 |
| C13' | 0.000 | 0.009 | 0.000 | 0.000 | 0.000 | 5.372 | 0.022 | 0.189 |
| C12' | 0.000 | 0.022 | 0.000 | 0.000 | 0.000 | -5.121 | 0.030 | -0.186 |
| C11' | 0.000 | 0.025 | 0.000 | 0.000 | 0.000 | 6.075 | 0.031 | 0.197 |
| C10' | 0.000 | -0.072 | 0.000 | 0.000 | 0.000 | -19.119 | -0.045 | -0.288 |
| C15' | 0.000 | -0.003 | 0.000 | 0.000 | 0.000 | 0.852 | -0.015 | 0.102 |
| C17' | 0.000 | 0.015 | 0.000 | 0.000 | 0.000 | -0.083 | 0.026 | -0.047 |
| C16' | 0.000 | 0.033 | 0.000 | 0.000 | 0.000 | -0.044 | 0.035 | -0.038 |
| C16' | 0.000 | 0.021 | 0.000 | 0.000 | 0.000 | -0.032 | 0.030 | -0.034 |
| C1' | 0.000 | -0.003 | 0.000 | 0.000 | 0.000 | -9.121 | -0.015 | -0.225 |
| C2' | 0.000 | 0.044 | 0.000 | 0.000 | 0.000 | 2.836 | 0.038 | 0.152 |
| C3' | 0.000 | 0.030 | 0.000 | 0.000 | 0.000 | -2.453 | 0.033 | -0.145 |
| C4' | 0.000 | 0.044 | 0.000 | 0.000 | 0.000 | 2.636 | 0.038 | 0.149 |
| C5' | 0.000 | 0.024 | 0.000 | 0.000 | 0.000 | -9.519 | 0.031 | -0.228 |
| C6' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.469 | -0.013 | 0.084 |
| C9' | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | -0.034 | 0.026 | -0.035 |
| C8' | 0.000 | 0.009 | 0.000 | 0.000 | 0.000 | -0.020 | 0.022 | -0.029 |
| C7' | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | -0.030 | 0.024 | -0.034 |


| H1 | 0.000 | 0.071 | 0.000 | 0.000 | 0.000 | 0.004 | 0.045 | 0.017 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H2 | 0.000 | 0.022 | 0.000 | 0.000 | 0.000 | -0.034 | 0.030 | -0.035 |
| H3 | 0.000 | -0.067 | 0.000 | 0.000 | 0.000 | -0.055 | -0.044 | -0.041 |
| H4 | 0.000 | 0.051 | 0.000 | 0.000 | 0.000 | -0.017 | 0.040 | -0.028 |
| H5 | 0.000 | 0.020 | 0.000 | 0.000 | 0.000 | -0.033 | 0.029 | -0.035 |
| H6 | 0.000 | 0.017 | 0.000 | 0.000 | 0.000 | 0.023 | 0.028 | 0.031 |
| H7 | 0.000 | 0.071 | 0.000 | 0.000 | 0.000 | -0.020 | 0.045 | -0.029 |
| H8 | 0.000 | 0.022 | 0.000 | 0.000 | 0.000 | -0.033 | 0.030 | -0.035 |
| H9 | 0.000 | -0.069 | 0.000 | 0.000 | 0.000 | 0.044 | -0.044 | 0.038 |
| H10 | 0.000 | 0.031 | 0.000 | 0.000 | 0.000 | 0.005 | 0.034 | 0.019 |
| H11 | 0.000 | -0.008 | 0.000 | 0.000 | 0.000 | -0.034 | -0.021 | -0.035 |
| H12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.029 | -0.007 | -0.033 |
| H13 | 0.000 | 0.032 | 0.000 | 0.000 | 0.000 | -0.013 | 0.034 | -0.025 |
| H14 | 0.000 | -0.010 | 0.000 | 0.000 | 0.000 | 0.026 | -0.023 | 0.032 |
| H15 | 0.000 | -0.004 | 0.000 | 0.000 | 0.000 | -0.025 | -0.017 | -0.031 |
| H16 | 0.000 | 0.031 | 0.000 | 0.000 | 0.000 | -0.015 | 0.034 | -0.027 |
| H17 | 0.000 | -0.005 | 0.000 | 0.000 | 0.000 | -0.031 | -0.018 | -0.034 |
| H18 | 0.000 | -0.005 | 0.000 | 0.000 | 0.000 | 0.016 | -0.018 | 0.027 |
| H19 | 0.000 | -0.023 | 0.000 | 0.000 | 0.000 | 2.530 | -0.031 | 0.147 |
| H20 | 0.000 | 0.038 | 0.000 | 0.000 | 0.000 | 0.089 | 0.036 | 0.048 |
| H21 | 0.000 | 0.034 | 0.000 | 0.000 | 0.000 | 0.180 | 0.035 | 0.061 |
| H22 | 0.000 | -0.033 | 0.000 | 0.000 | 0.000 | 2.464 | -0.035 | 0.145 |
| H23 | 0.000 | 0.091 | 0.000 | 0.000 | 0.000 | 2.552 | 0.048 | 0.147 |
| H24 | 0.000 | 0.096 | 0.000 | 0.000 | 0.000 | 0.146 | 0.049 | 0.057 |
| H25 | 0.000 | 0.063 | 0.000 | 0.000 | 0.000 | 0.363 | 0.043 | 0.077 |
| H26 | -0.001 | -0.111 | 0.000 | 0.000 | 0.000 | 3.943 | -0.052 | 0.170 |
| H1' | 0.000 | 0.031 | 0.000 | 0.000 | 0.000 | 0.002 | 0.034 | 0.015 |
| H2' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | -0.021 | -0.015 | -0.030 |
| H3' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | -0.028 | -0.011 | -0.033 |
| H4' | 0.000 | 0.033 | 0.000 | 0.000 | 0.000 | -0.013 | 0.035 | -0.025 |
| H5' | 0.000 | -0.010 | 0.000 | 0.000 | 0.000 | -0.027 | -0.023 | -0.032 |
| H6' | 0.000 | -0.005 | 0.000 | 0.000 | 0.000 | 0.017 | -0.019 | 0.028 |
| H7' | 0.000 | 0.032 | 0.000 | 0.000 | 0.000 | -0.013 | 0.034 | -0.025 |
| H8' | 0.000 | -0.009 | 0.000 | 0.000 | 0.000 | -0.023 | -0.023 | -0.031 |
| H9' | 0.000 | -0.003 | 0.000 | 0.000 | 0.000 | 0.025 | -0.015 | 0.031 |
| H10' | 0.000 | 0.067 | 0.000 | 0.000 | 0.000 | 0.009 | 0.044 | 0.022 |
| H11' | 0.000 | 0.036 | 0.000 | 0.000 | 0.000 | -0.050 | 0.036 | -0.040 |
| H12' | 0.000 | -0.028 | 0.000 | 0.000 | 0.000 | -0.050 | -0.033 | -0.040 |
| H13' | 0.000 | 0.059 | 0.000 | 0.000 | 0.000 | -0.019 | 0.042 | -0.029 |
| H14' | 0.000 | 0.029 | 0.000 | 0.000 | 0.000 | 0.037 | 0.033 | 0.036 |
| H15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.039 | -0.006 | -0.036 |
| H16' | 0.000 | 0.089 | 0.000 | 0.000 | 0.000 | -0.027 | 0.048 | -0.032 |
| H17' | 0.000 | -0.015 | 0.000 | 0.000 | 0.000 | -0.059 | -0.027 | -0.042 |
| H18' | 0.000 | -0.078 | 0.000 | 0.000 | 0.000 | 0.029 | -0.046 | 0.033 |
| H19' | 0.000 | 0.092 | 0.000 | 0.000 | 0.000 | 4.180 | 0.049 | 0.174 |
| H20' | 0.001 | 0.114 | 0.000 | 0.000 | 0.000 | 0.176 | 0.052 | 0.060 |
| H21' | 0.001 | 0.110 | 0.000 | 0.000 | 0.000 | 0.311 | 0.052 | 0.073 |
| H22' | 0.000 | 0.097 | 0.000 | 0.000 | 0.000 | 3.849 | 0.049 | 0.169 |
| H23' | 0.000 | -0.027 | 0.000 | 0.000 | 0.000 | 2.319 | -0.032 | 0.143 |


| H24' | 0.000 | 0.037 | 0.000 | 0.000 | 0.000 | 0.097 | 0.036 | 0.049 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| H25' | 0.000 | 0.039 | 0.000 | 0.000 | 0.000 | 0.201 | 0.037 | 0.063 |
| H26' | 0.000 | -0.014 | 0.000 | 0.000 | 0.000 | 1.944 | -0.026 | 0.134 |

Table A2.10: Contributions at the bcp along on the $\mathrm{N} 2-\mathrm{N} 3$ bond for the EO molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}$,
$\mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FS}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | SF\% | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | SFs\% | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\mathrm{FS}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1 | 0.000 | 0.000 | 0.001 | 0.000 | 0.001 | 11.902 | 0.006 | 0.246 |
| N1 | 0.009 | 0.004 | 0.004 | 0.004 | 0.000 | -0.596 | 0.018 | -0.091 |
| N2 | 0.055 | 0.027 | 0.026 | 0.029 | -0.004 | -54.314 | 0.033 | -0.408 |
| N3 | 99.204 | 49.784 | 99.607 | 99.597 | 0.010 | 145.460 | 0.396 | 0.567 |
| N5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.216 | -0.006 | 0.065 |
| N4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.815 | -0.007 | 0.101 |
| C14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.460 | 0.003 | -0.122 |
| C13 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.432 | 0.005 | 0.081 |
| C12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.414 | 0.004 | -0.080 |
| C11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.497 | 0.005 | 0.085 |
| C10 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.590 | 0.003 | -0.126 |
| C15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.073 | -0.002 | 0.045 |
| C17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.008 | 0.003 | -0.021 |
| C16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.003 | -0.017 |
| C16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.004 | -0.016 |
| C1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.838 | 0.005 | -0.132 |
| C2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.599 | 0.006 | 0.091 |
| C3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.622 | 0.005 | -0.092 |
| C4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.757 | -0.004 | 0.098 |
| C5 | -0.001 | -0.001 | -0.001 | 0.000 | 0.000 | -2.733 | -0.009 | -0.151 |
| C6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.117 | -0.003 | 0.053 |
| C9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.009 | 0.004 | -0.023 |
| C8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.019 |
| C7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.007 | 0.004 | -0.020 |
| Cu1' | 0.000 | 0.000 | 0.001 | 0.000 | 0.001 | 11.921 | 0.006 | 0.246 |
| N1' | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -5.161 | -0.007 | -0.186 |
| N2' | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -8.188 | 0.006 | -0.217 |
| N3' | 0.001 | 0.000 | 0.001 | 0.000 | 0.000 | 6.003 | 0.008 | 0.196 |
| N5' | -0.001 | -0.001 | -0.001 | -0.001 | 0.000 | 1.350 | -0.009 | 0.119 |
| N4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.057 | -0.007 | 0.042 |
| C14' | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -2.838 | -0.008 | -0.153 |
| C13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.838 | -0.005 | 0.102 |
| C12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.817 | -0.002 | -0.101 |
| C11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.940 | -0.002 | 0.106 |
| C10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -2.875 | -0.006 | -0.153 |
| C15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.138 | -0.002 | 0.056 |
| C17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.013 | 0.004 | -0.026 |
| C16' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.007 | 0.005 | -0.021 |


| C16 ${ }^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.019 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.348 | -0.003 | -0.119 |
| C2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.423 | 0.005 | 0.081 |
| C3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.367 | 0.004 | -0.077 |
| C4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.390 | 0.005 | 0.079 |
| C5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.397 | 0.004 | -0.120 |
| C6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.071 | -0.002 | 0.045 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.003 | -0.019 |
| C8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.003 | -0.016 |
| C7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.003 | -0.018 |
| H1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.009 |
| H2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.019 |
| H3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.009 | -0.006 | -0.022 |
| H4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.005 | -0.015 |
| H5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.019 |
| H6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | 0.004 | 0.016 |
| H7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.006 | -0.016 |
| H8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.004 | -0.019 |
| H9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | -0.006 | 0.021 |
| H10 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.010 |
| H11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | -0.003 | -0.018 |
| H12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.000 | -0.018 |
| H13 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.005 | -0.013 |
| H14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.003 | 0.017 |
| H15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.002 | -0.017 |
| H16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.004 | -0.014 |
| H17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | -0.002 | -0.018 |
| H18 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | -0.002 | 0.014 |
| H19 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.369 | -0.004 | 0.077 |
| H20 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.013 | 0.005 | 0.026 |
| H21 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.027 | 0.005 | 0.032 |
| H22 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.360 | -0.005 | 0.077 |
| H23 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.377 | 0.007 | 0.078 |
| H24 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.023 | 0.007 | 0.031 |
| H25 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.057 | 0.005 | 0.041 |
| H26 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.569 | -0.007 | 0.089 |
| H1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | 0.008 |
| H2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | -0.002 | -0.016 |
| H3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.001 | -0.017 |
| H4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.005 | -0.013 |
| H5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.003 | -0.017 |
| H6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | -0.003 | 0.015 |
| H7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.005 | -0.014 |
| H8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | -0.003 | -0.016 |
| H9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.004 | -0.002 | 0.017 |
| H10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.012 |
| H11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.008 | 0.005 | -0.021 |
| H12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.008 | -0.005 | -0.022 |
| H13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.006 | -0.016 |


| H14 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.006 | 0.005 | 0.019 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| H15 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.006 | 0.001 | -0.020 |
| H16 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.007 | -0.018 |
| H17 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.010 | -0.004 | -0.023 |
| H18' $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.005 | -0.007 | 0.018 |
| H19 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.620 | 0.007 | 0.092 |
| H20 $^{\prime}$ | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.028 | 0.007 | 0.033 |
| H21 $^{\prime}$ | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.049 | 0.007 | 0.040 |
| H22 $^{\prime}$ | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.568 | 0.007 | 0.089 |
| H23 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.343 | -0.005 | 0.075 |
| H24' $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.014 | 0.005 | 0.026 |
| H25 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.030 | 0.005 | 0.033 |
| H26' $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.284 | -0.003 | 0.071 |

Table A2.11: Contributions at the N3 atomic basin along on the N2-N3 bond for the EO molecular system; LS, SF\%,
$\mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FSs}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 0.001 | 0.004 | 0.001 | 0.000 | 0.001 | 4.510 | 0.017 | 0.178 |
| N 1 | 0.001 | 0.007 | 0.000 | 0.001 | -0.001 | -5.339 | 0.020 | -0.188 |
| N 2 | 0.002 | 0.010 | 0.001 | 0.002 | -0.001 | -4.420 | 0.023 | -0.177 |
| N 3 | 0.003 | 0.016 | 0.002 | 0.001 | 0.001 | 3.178 | 0.027 | 0.158 |
| N 5 | -0.001 | -0.003 | 0.000 | 0.000 | 0.000 | 0.048 | -0.015 | 0.039 |
| N 4 | -0.001 | -0.003 | 0.000 | 0.000 | 0.000 | -0.002 | -0.015 | -0.013 |
| C 14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.497 | 0.008 | -0.085 |
| C 13 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.142 | 0.011 | 0.056 |
| C 12 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.134 | 0.010 | -0.055 |
| C 11 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.164 | 0.011 | 0.059 |
| C 10 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.533 | 0.007 | -0.087 |
| C 15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.023 | -0.004 | 0.031 |
| C 17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.007 | -0.014 |
| C 16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.008 | -0.011 |
| C 16 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.008 | -0.011 |
| C 1 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.404 | 0.010 | -0.080 |
| C 2 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.125 | 0.012 | 0.054 |
| C 3 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.115 | 0.010 | -0.052 |
| C 4 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.132 | 0.012 | 0.055 |
| C 5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.493 | 0.007 | -0.085 |
| C 6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.022 | -0.003 | 0.030 |
| C 9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.008 | -0.013 |
| C 8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.007 | -0.011 |
| C 7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.007 | -0.012 |
| Cu1 | 22.414 | 99.866 | 11.222 | 11.192 | 0.030 | 114.287 | 0.500 | 0.523 |
| $\mathrm{~N} 1{ }^{\prime}$ | 0.001 | 0.005 | 0.000 | 0.001 | -0.001 | -5.586 | 0.019 | -0.191 |
| N2' | 0.002 | 0.011 | 0.001 | 0.002 | -0.001 | -4.260 | 0.024 | -0.175 |


| N3' | 0.003 | 0.015 | 0.002 | 0.001 | 0.001 | 3.045 | 0.027 | 0.156 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| N5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.101 | 0.006 | -0.111 |
| N4' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -1.132 | 0.009 | -0.112 |
| C14' | 0.001 | 0.004 | 0.000 | 0.001 | 0.000 | -0.871 | 0.018 | -0.103 |
| C13' | 0.001 | 0.004 | 0.000 | 0.000 | 0.000 | 0.223 | 0.017 | 0.065 |
| C12' | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | -0.194 | 0.014 | -0.062 |
| C11' | 0.001 | 0.004 | 0.000 | 0.000 | 0.000 | 0.254 | 0.016 | 0.068 |
| C10' | 0.001 | 0.005 | 0.000 | 0.001 | 0.000 | -0.919 | 0.018 | -0.105 |
| C15' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.031 | -0.001 | 0.034 |
| C17' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.008 | -0.016 |
| C16' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.002 | 0.009 | -0.012 |
| C16' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.001 | 0.009 | -0.012 |
| C1' | 0.001 | 0.004 | 0.000 | 0.000 | 0.000 | -0.747 | 0.016 | -0.098 |
| C2' | 0.001 | 0.004 | 0.000 | 0.000 | 0.000 | 0.205 | 0.017 | 0.063 |
| C3' | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | -0.167 | 0.014 | -0.059 |
| C4' | 0.001 | 0.004 | 0.000 | 0.000 | 0.000 | 0.200 | 0.017 | 0.063 |
| C5' | 0.001 | 0.005 | 0.000 | 0.001 | 0.000 | -0.814 | 0.018 | -0.101 |
| C6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.029 | 0.003 | 0.033 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.009 | -0.014 |
| C8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.007 | -0.012 |
| C7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.008 | -0.013 |
| H1 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | 0.005 |
| H2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.004 | -0.011 |
| H3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -0.008 | -0.012 |
| H4 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.001 | 0.010 | -0.009 |
| H5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.003 | -0.011 |
| H6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.010 |
| H7 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.001 | 0.011 | -0.009 |
| H8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -0.002 | -0.011 |
| H9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.008 | 0.011 |
| H10 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | 0.007 |
| H11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.005 | -0.012 |
| H12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -0.007 | -0.012 |
| H13 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.001 | 0.010 | -0.009 |
| H14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.005 | 0.011 |
| H15 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -0.005 | -0.011 |
| H16 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.001 | 0.011 | -0.010 |
| H17 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.006 | -0.012 |
| H18 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.008 | 0.010 |
| H19 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.126 | -0.008 | 0.054 |
| H20 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.004 | 0.011 | 0.018 |
| H21 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.009 | 0.011 | 0.022 |
| H22 | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | 0.121 | -0.009 | 0.053 |
| H23 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.095 | 0.008 | 0.049 |
| H24 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.004 | 0.012 | 0.018 |
| H25 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.010 | 0.011 | 0.023 |
| H26 | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.107 | -0.013 | 0.051 |
| H1' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.012 | 0.006 |
| H2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.005 | -0.012 |


| H3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.006 | -0.013 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H4 $^{\prime}$ | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.001 | 0.012 | -0.010 |
| H5 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.005 | -0.012 |
| H6 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.004 | 0.011 |
| H7 $^{\prime}$ | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.001 | 0.012 | -0.010 |
| H8 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -0.006 | -0.012 |
| H9 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | -0.007 | 0.012 |
| H10 $^{\prime}$ | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.012 | 0.007 |
| H11 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.004 | -0.014 |
| H12 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.004 | -0.013 |
| H13 $^{\prime}$ | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.001 | 0.012 | -0.010 |
| H14 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | -0.006 | 0.013 |
| H15 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.005 | -0.012 |
| H16 $^{\prime}$ | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.001 | 0.012 | -0.010 |
| H17 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | -0.006 | -0.014 |
| H18 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | -0.006 | 0.011 |
| H19 $^{\prime}$ | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.223 | 0.012 | 0.065 |
| H20 $^{\prime}$ | 0.001 | 0.003 | 0.000 | 0.000 | 0.000 | 0.006 | 0.015 | 0.020 |
| H21 $^{\prime}$ | 0.001 | 0.003 | 0.000 | 0.000 | 0.000 | 0.012 | 0.015 | 0.025 |
| H22' $^{\prime}$ | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.205 | 0.012 | 0.064 |
| H23 $^{\prime}$ | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | 0.181 | 0.013 | 0.061 |
| H24 $^{\prime}$ | 0.001 | 0.003 | 0.000 | 0.000 | 0.000 | 0.006 | 0.015 | 0.020 |
| H25 $^{\prime}$ | 0.001 | 0.003 | 0.000 | 0.000 | 0.000 | 0.014 | 0.015 | 0.026 |
| H26 $^{\prime}$ | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.166 | 0.012 | 0.059 |

Table A2.12: Contributions at $0.5 \AA$ to Cu 1 atomic basin along the $\mathrm{Cu}-\mathrm{Cu}$ internuclear axis for the EO molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r})$. $\mathrm{R}_{\mathrm{SF}}$ $\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\mathrm{FSs}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 0.004 | 13.236 | 0.003 | 0.001 | 0.002 | -849.522 | 0.255 | -1.020 |
| N 1 | -0.004 | -12.259 | -0.003 | -0.001 | -0.002 | 602.638 | -0.248 | 0.910 |
| N 2 | 0.005 | 18.984 | 0.002 | 0.003 | -0.001 | 446.862 | 0.287 | 0.824 |
| N 3 | 0.004 | 15.102 | 0.003 | 0.002 | 0.001 | -315.074 | 0.266 | -0.733 |
| N 5 | -0.001 | -3.401 | -0.001 | 0.000 | 0.000 | 12.023 | -0.162 | 0.247 |
| N 4 | -0.001 | -3.122 | 0.000 | 0.000 | 0.000 | 16.992 | -0.157 | 0.277 |
| C 14 | 0.000 | 1.017 | 0.000 | 0.000 | 0.000 | 60.319 | 0.108 | 0.422 |
| C 13 | 0.000 | 1.606 | 0.000 | 0.000 | 0.000 | -16.442 | 0.126 | -0.274 |
| C 12 | 0.000 | 1.022 | 0.000 | 0.000 | 0.000 | 14.992 | 0.109 | 0.266 |
| C 11 | 0.000 | 1.503 | 0.000 | 0.000 | 0.000 | -18.907 | 0.123 | -0.287 |
| C 10 | 0.000 | 1.063 | 0.000 | 0.000 | 0.000 | 64.390 | 0.110 | 0.432 |
| C 15 | 0.000 | -0.035 | 0.000 | 0.000 | 0.000 | -2.514 | -0.035 | -0.146 |
| C 17 | 0.000 | 0.203 | 0.000 | 0.000 | 0.000 | 0.255 | 0.063 | 0.068 |
| C 16 | 0.000 | 0.333 | 0.000 | 0.000 | 0.000 | 0.127 | 0.075 | 0.054 |
| C 16 | 0.000 | 0.345 | 0.000 | 0.000 | 0.000 | 0.108 | 0.076 | 0.051 |
| C 1 | 0.000 | 1.189 | 0.000 | 0.000 | 0.000 | 49.395 | 0.114 | 0.395 |
| C 2 | 0.000 | 1.611 | 0.000 | 0.000 | 0.000 | -14.596 | 0.126 | -0.263 |


| C3 | 0.000 | 0.973 | 0.000 | 0.000 | 0.000 | 12.815 | 0.107 | 0.252 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| C4 | 0.001 | 1.815 | 0.000 | 0.000 | 0.000 | -15.196 | 0.131 | -0.267 |
| C5 | 0.000 | 0.986 | 0.000 | 0.000 | 0.000 | 59.336 | 0.107 | 0.420 |
| C6 | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | -2.344 | 0.022 | -0.143 |
| C9 | 0.000 | 0.324 | 0.000 | 0.000 | 0.000 | 0.174 | 0.074 | 0.060 |
| C8 | 0.000 | 0.260 | 0.000 | 0.000 | 0.000 | 0.103 | 0.069 | 0.050 |
| C7 | 0.000 | 0.226 | 0.000 | 0.000 | 0.000 | 0.143 | 0.066 | 0.056 |
| Cu1' | 0.004 | 13.258 | 0.003 | 0.001 | 0.002 | -849.472 | 0.255 | -1.020 |
| N1' | -0.004 | -12.211 | -0.003 | -0.001 | -0.002 | 602.633 | -0.248 | 0.910 |
| N2' | 0.005 | 18.961 | 0.002 | 0.003 | -0.001 | 446.879 | 0.287 | 0.824 |
| N3' | 0.004 | 15.101 | 0.003 | 0.002 | 0.001 | -315.073 | 0.266 | -0.733 |
| N5' | -0.001 | -3.409 | -0.001 | 0.000 | 0.000 | 12.023 | -0.162 | 0.247 |
| N4' | -0.001 | -3.123 | 0.000 | 0.000 | 0.000 | 16.995 | -0.157 | 0.277 |
| C14' | 0.000 | 1.010 | 0.000 | 0.000 | 0.000 | 60.318 | 0.108 | 0.422 |
| C13' | 0.000 | 1.590 | 0.000 | 0.000 | 0.000 | -16.440 | 0.126 | -0.274 |
| C12' | 0.000 | 1.025 | 0.000 | 0.000 | 0.000 | 14.991 | 0.109 | 0.266 |
| C11' | 0.000 | 1.505 | 0.000 | 0.000 | 0.000 | -18.907 | 0.123 | -0.287 |
| C10' | 0.000 | 1.094 | 0.000 | 0.000 | 0.000 | 64.381 | 0.111 | 0.432 |
| C15' | 0.000 | -0.036 | 0.000 | 0.000 | 0.000 | -2.514 | -0.036 | -0.146 |
| C17' | 0.000 | 0.236 | 0.000 | 0.000 | 0.000 | 0.254 | 0.067 | 0.068 |
| C16' | 0.000 | 0.367 | 0.000 | 0.000 | 0.000 | 0.126 | 0.077 | 0.054 |
| C16' | 0.000 | 0.348 | 0.000 | 0.000 | 0.000 | 0.108 | 0.076 | 0.051 |
| C1' | 0.000 | 1.004 | 0.000 | 0.000 | 0.000 | 49.294 | 0.108 | 0.395 |
| C2' | 0.000 | 1.613 | 0.000 | 0.000 | 0.000 | -14.597 | 0.126 | -0.263 |
| C3' | 0.000 | 0.975 | 0.000 | 0.000 | 0.000 | 12.815 | 0.107 | 0.252 |
| C4' | 0.001 | 1.790 | 0.000 | 0.000 | 0.000 | -15.196 | 0.131 | -0.267 |
| C5' | 0.000 | 0.977 | 0.000 | 0.000 | 0.000 | 59.324 | 0.107 | 0.420 |
| C6' | 0.000 | -0.024 | 0.000 | 0.000 | 0.000 | -2.346 | -0.031 | -0.143 |
| C9' | 0.000 | 0.313 | 0.000 | 0.000 | 0.000 | 0.174 | 0.073 | 0.060 |
| C8' | 0.000 | 0.221 | 0.000 | 0.000 | 0.000 | 0.101 | 0.065 | 0.050 |
| C7' | 0.000 | 0.241 | 0.000 | 0.000 | 0.000 | 0.143 | 0.067 | 0.056 |
| H1 | 0.000 | 0.879 | 0.000 | 0.000 | 0.000 | -0.012 | 0.103 | -0.025 |
| H2 | 0.000 | 0.057 | 0.000 | 0.000 | 0.000 | 0.105 | 0.041 | 0.051 |
| H3 | 0.000 | -0.276 | 0.000 | 0.000 | 0.000 | 0.149 | -0.070 | 0.057 |
| H4 | 0.000 | 0.826 | 0.000 | 0.000 | 0.000 | 0.058 | 0.101 | 0.042 |
| H5 | 0.000 | -0.013 | 0.000 | 0.000 | 0.000 | 0.121 | -0.026 | 0.053 |
| H6 | 0.000 | 0.062 | 0.000 | 0.000 | 0.000 | -0.081 | 0.043 | -0.047 |
| H7 | 0.000 | 0.917 | 0.000 | 0.000 | 0.000 | 0.063 | 0.105 | 0.043 |
| H8 | 0.000 | -0.056 | 0.000 | 0.000 | 0.000 | 0.113 | -0.041 | 0.052 |
| H9 | 0.000 | -0.337 | 0.000 | 0.000 | 0.000 | -0.128 | -0.075 | -0.054 |
| H10 | 0.000 | 0.866 | 0.000 | 0.000 | 0.000 | -0.027 | 0.103 | -0.032 |
| H11 | 0.000 | 0.056 | 0.000 | 0.000 | 0.000 | 0.164 | 0.041 | 0.059 |
| H12 | 0.000 | -0.122 | 0.000 | 0.000 | 0.000 | 0.147 | -0.053 | 0.057 |
| H13 | 0.000 | 0.846 | 0.000 | 0.000 | 0.000 | 0.061 | 0.102 | 0.043 |
| H14 | 0.000 | 0.017 | 0.000 | 0.000 | 0.000 | -0.125 | 0.028 | -0.054 |
| H15 | 0.000 | -0.066 | 0.000 | 0.000 | 0.000 | 0.122 | -0.044 | 0.053 |
| H16 | 0.000 | 0.927 | 0.000 | 0.000 | 0.000 | 0.075 | 0.105 | 0.045 |
| H17 | 0.000 | -0.147 | 0.000 | 0.000 | 0.000 | 0.162 | -0.057 | 0.059 |
| H18 | 0.000 | -0.324 | 0.000 | 0.000 | 0.000 | -0.083 | -0.074 | -0.047 |


| H19 | 0.000 | -0.154 | 0.000 | 0.000 | 0.000 | -15.502 | -0.058 | -0.269 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H20 | 0.000 | 1.395 | 0.000 | 0.000 | 0.000 | -0.488 | 0.120 | -0.085 |
| H21 | 0.000 | 1.331 | 0.000 | 0.000 | 0.000 | -0.947 | 0.118 | -0.106 |
| H22 | 0.000 | -0.235 | 0.000 | 0.000 | 0.000 | -14.684 | -0.066 | -0.264 |
| H23 | 0.000 | 0.663 | 0.000 | 0.000 | 0.000 | -11.675 | 0.094 | -0.244 |
| H24 | 0.000 | 1.405 | 0.000 | 0.000 | 0.000 | -0.493 | 0.121 | -0.085 |
| H25 | 0.000 | 1.263 | 0.000 | 0.000 | 0.000 | -1.081 | 0.116 | -0.111 |
| H26 | 0.000 | -1.088 | 0.000 | 0.000 | 0.000 | -12.792 | -0.111 | -0.252 |
| H1' | 0.000 | 0.878 | 0.000 | 0.000 | 0.000 | -0.012 | 0.103 | -0.025 |
| H2' | 0.000 | 0.058 | 0.000 | 0.000 | 0.000 | 0.105 | 0.042 | 0.051 |
| H3' | 0.000 | -0.275 | 0.000 | 0.000 | 0.000 | 0.149 | -0.070 | 0.057 |
| H4' | 0.000 | 0.826 | 0.000 | 0.000 | 0.000 | 0.058 | 0.101 | 0.042 |
| H5' | 0.000 | -0.003 | 0.000 | 0.000 | 0.000 | 0.121 | -0.015 | 0.053 |
| H6' | 0.000 | 0.037 | 0.000 | 0.000 | 0.000 | -0.081 | 0.036 | -0.047 |
| H7' | 0.000 | 0.917 | 0.000 | 0.000 | 0.000 | 0.063 | 0.105 | 0.043 |
| H8' | 0.000 | -0.056 | 0.000 | 0.000 | 0.000 | 0.113 | -0.041 | 0.052 |
| H9' | 0.000 | -0.338 | 0.000 | 0.000 | 0.000 | -0.128 | -0.075 | -0.054 |
| H10' | 0.000 | 0.866 | 0.000 | 0.000 | 0.000 | -0.027 | 0.103 | -0.032 |
| H11' | 0.000 | 0.057 | 0.000 | 0.000 | 0.000 | 0.164 | 0.041 | 0.059 |
| H12' | 0.000 | -0.122 | 0.000 | 0.000 | 0.000 | 0.147 | -0.053 | 0.057 |
| H13' | 0.000 | 0.846 | 0.000 | 0.000 | 0.000 | 0.061 | 0.102 | 0.043 |
| H14' | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | -0.125 | 0.022 | -0.054 |
| H15' | 0.000 | -0.066 | 0.000 | 0.000 | 0.000 | 0.122 | -0.043 | 0.053 |
| H16' | 0.000 | 0.926 | 0.000 | 0.000 | 0.000 | 0.075 | 0.105 | 0.045 |
| H17' | 0.000 | -0.147 | 0.000 | 0.000 | 0.000 | 0.162 | -0.057 | 0.059 |
| H18' | 0.000 | -0.323 | 0.000 | 0.000 | 0.000 | -0.083 | -0.074 | -0.047 |
| H19' | 0.000 | -0.154 | 0.000 | 0.000 | 0.000 | -15.501 | -0.058 | -0.269 |
| H20' | 0.000 | 1.395 | 0.000 | 0.000 | 0.000 | -0.488 | 0.120 | -0.085 |
| H21' | 0.000 | 1.331 | 0.000 | 0.000 | 0.000 | -0.947 | 0.118 | -0.106 |
| H22' | 0.000 | -0.233 | 0.000 | 0.000 | 0.000 | -14.684 | -0.066 | -0.264 |
| H23' | 0.000 | 0.663 | 0.000 | 0.000 | 0.000 | -11.675 | 0.094 | -0.244 |
| H24' | 0.000 | 1.408 | 0.000 | 0.000 | 0.000 | -0.493 | 0.121 | -0.085 |
| H25' | 0.000 | 1.257 | 0.000 | 0.000 | 0.000 | -1.081 | 0.116 | -0.111 |
| H26' | 0.000 | -1.088 | 0.000 | 0.000 | 0.000 | -12.792 | -0.111 | -0.252 |

Table A2.13: Contributions at the middle point between the two copper atoms along the $\mathrm{Cu}-\mathrm{Cu}$ internuclear axis for the
EO molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FSs}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 1.895 | 98.268 | 1.093 | 0.803 | 0.290 | 101.355 | 0.497 | 0.502 |
| N 1 | 0.000 | -0.010 | 0.000 | 0.000 | 0.000 | -0.995 | -0.023 | -0.108 |
| N2 | -0.002 | -0.092 | -0.001 | -0.001 | 0.000 | -1.607 | -0.049 | -0.126 |
| $\mathrm{~N}^{\prime}$ | -0.002 | -0.086 | 0.000 | -0.001 | 0.001 | 3.551 | -0.047 | 0.164 |
| $\mathrm{~N}^{\prime}$ | 0.001 | 0.077 | 0.000 | 0.001 | -0.001 | -2.768 | 0.046 | -0.151 |
| N3 | 0.005 | 0.279 | 0.002 | 0.003 | -0.001 | -4.927 | 0.070 | -0.183 |
| O1 | 0.002 | 0.128 | 0.001 | 0.002 | -0.001 | -4.147 | 0.054 | -0.173 |


| F1 | 0.000 | 0.022 | 0.000 | 0.000 | 0.000 | -0.078 | 0.030 | -0.046 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| F2 | 0.001 | 0.051 | 0.000 | 0.001 | 0.000 | -0.118 | 0.040 | -0.053 |
| F3 | 0.000 | 0.018 | 0.000 | 0.000 | 0.000 | -0.075 | 0.028 | -0.045 |
| C1 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.448 | 0.012 | 0.082 |
| C2 | 0.001 | 0.063 | 0.000 | 0.001 | 0.000 | -0.832 | 0.043 | -0.101 |
| C3 | 0.001 | 0.041 | 0.000 | 0.000 | 0.000 | 0.252 | 0.037 | 0.068 |
| C4 | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | 0.303 | 0.026 | 0.072 |
| C5 | 0.001 | 0.058 | 0.000 | 0.001 | 0.000 | -0.915 | 0.042 | -0.105 |
| C6 | 0.001 | 0.029 | 0.000 | 0.000 | 0.000 | -0.338 | 0.033 | -0.075 |
| C7 | 0.000 | 0.022 | 0.000 | 0.000 | 0.000 | -0.594 | 0.030 | -0.091 |
| C8 | 0.000 | 0.017 | 0.000 | 0.000 | 0.000 | -0.705 | 0.028 | -0.096 |
| C9 | 0.000 | 0.011 | 0.000 | 0.000 | 0.000 | -0.856 | 0.024 | -0.102 |
| H1 | 0.001 | 0.029 | 0.000 | 0.000 | 0.000 | 0.072 | 0.033 | 0.045 |
| H2 | 0.001 | 0.074 | 0.001 | 0.001 | 0.000 | 0.147 | 0.045 | 0.057 |
| H3 | 0.001 | 0.036 | 0.000 | 0.000 | 0.000 | 0.006 | 0.036 | 0.019 |
| H4 | 0.000 | 0.024 | 0.000 | 0.000 | 0.000 | 0.086 | 0.031 | 0.048 |
| H5 | 0.001 | 0.073 | 0.001 | 0.001 | 0.000 | 0.092 | 0.045 | 0.049 |
| H6 | 0.001 | 0.034 | 0.000 | 0.000 | 0.000 | 0.078 | 0.035 | 0.046 |
| H7 | 0.000 | 0.019 | 0.000 | 0.000 | 0.000 | -0.034 | 0.029 | -0.035 |
| H8 | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | -0.034 | 0.027 | -0.035 |
| H9 | 0.001 | 0.028 | 0.000 | 0.000 | 0.000 | -0.007 | 0.033 | -0.021 |
| H10 | 0.001 | 0.065 | 0.001 | 0.001 | 0.000 | 0.064 | 0.043 | 0.043 |
| H11 | 0.001 | 0.037 | 0.000 | 0.000 | 0.000 | 0.035 | 0.036 | 0.035 |
| H12 | 0.001 | 0.045 | 0.000 | 0.000 | 0.000 | 0.007 | 0.038 | 0.020 |
| H13 | 0.001 | 0.055 | 0.001 | 0.001 | 0.000 | 0.037 | 0.041 | 0.036 |
| H14 | 0.001 | 0.051 | 0.000 | 0.000 | 0.000 | -0.014 | 0.040 | -0.026 |
| Cu1' | 0.000 | -0.005 | 0.000 | 0.000 | 0.001 | 2.350 | -0.019 | 0.143 |
| N1' | 0.000 | -0.018 | 0.000 | 0.000 | 0.000 | -0.050 | -0.028 | -0.040 |
| N2' | 0.000 | -0.018 | 0.000 | 0.000 | 0.000 | 0.065 | -0.028 | 0.043 |
| N5 | 0.004 | 0.215 | 0.002 | 0.002 | 0.001 | 2.751 | 0.065 | 0.151 |
| N4 | 0.003 | 0.170 | 0.001 | 0.002 | -0.001 | -2.711 | 0.060 | -0.150 |
| N3' | 0.002 | 0.116 | 0.001 | 0.001 | 0.000 | -0.284 | 0.053 | -0.071 |
| O1' | -0.001 | -0.040 | 0.000 | 0.000 | 0.000 | -0.769 | -0.037 | -0.099 |
| F1' | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | -0.052 | 0.025 | -0.040 |
| F2' | 0.000 | 0.026 | 0.000 | 0.000 | 0.000 | -0.081 | 0.032 | -0.047 |
| F3' | 0.000 | -0.024 | 0.000 | 0.000 | 0.000 | -0.056 | -0.031 | -0.041 |
| C1' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.289 | 0.011 | 0.071 |
| C2' | 0.000 | 0.006 | 0.000 | 0.000 | 0.000 | -0.451 | 0.019 | -0.083 |
| C3' | 0.000 | 0.009 | 0.000 | 0.000 | 0.000 | 0.127 | 0.022 | 0.054 |
| C4' | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | 0.161 | 0.016 | 0.059 |
| C5' | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | -0.430 | 0.022 | -0.081 |
| C6' | 0.000 | 0.007 | 0.000 | 0.000 | 0.000 | -0.149 | 0.021 | -0.057 |
| C7' | 0.000 | 0.005 | 0.000 | 0.000 | 0.000 | -0.270 | 0.018 | -0.070 |
| C8' | 0.000 | 0.007 | 0.000 | 0.000 | 0.000 | -0.295 | 0.021 | -0.072 |
| C9' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | -0.442 | -0.011 | -0.082 |
| H1' | 0.000 | -0.007 | 0.000 | 0.000 | 0.000 | 0.040 | -0.021 | 0.037 |
| H2' | 0.001 | 0.026 | 0.000 | 0.000 | 0.000 | 0.095 | 0.032 | 0.049 |
| H3' | -0.001 | -0.028 | 0.000 | 0.000 | 0.000 | 0.001 | -0.033 | 0.010 |
| H4' | 0.000 | -0.003 | 0.000 | 0.000 | 0.000 | 0.036 | -0.016 | 0.036 |


| $\mathrm{H}^{\prime}$ | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | 0.045 | 0.026 | 0.038 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H} 6^{\prime}$ | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | 0.029 | 0.024 | 0.033 |
| $\mathrm{H} 7^{\prime}$ | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | -0.020 | 0.014 | -0.029 |
| $\mathrm{H} 8^{\prime}$ | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | -0.019 | 0.022 | -0.029 |
| $\mathrm{H}^{\prime}$ | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | -0.004 | 0.021 | -0.018 |
| $\mathrm{H}^{\prime} 0^{\prime}$ | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | 0.034 | 0.027 | 0.035 |
| $\mathrm{H} 11^{\prime}$ | 0.000 | -0.011 | 0.000 | 0.000 | 0.000 | 0.017 | -0.024 | 0.028 |
| $\mathrm{H} 12^{\prime}$ | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | 0.003 | 0.026 | 0.015 |
| $\mathrm{H} 13^{\prime}$ | 0.000 | 0.009 | 0.000 | 0.000 | 0.000 | 0.019 | 0.022 | 0.029 |
| $\mathrm{H} 14^{\prime}$ | 0.000 | 0.015 | 0.000 | 0.000 | 0.000 | -0.008 | 0.026 | -0.022 |

Table A2.14: Contributions at the CD along the $\mathrm{Cu}-\mathrm{N} 5$ bond for the EE molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}$,
$\mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FS}}\right)$ are evaluated as in tab A 2.1 .

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FSs}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 1.893 | 98.467 | 0.951 | 0.942 | 0.009 | 164.093 | 0.497 | 0.590 |
| N 1 | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | -8.227 | 0.022 | -0.217 |
| N 2 | -0.002 | -0.092 | -0.001 | -0.001 | 0.000 | -8.396 | -0.049 | -0.219 |
| $\mathrm{~N}^{\prime}$ | -0.002 | -0.086 | 0.000 | -0.001 | 0.001 | 23.366 | -0.048 | 0.308 |
| $\mathrm{~N}^{\prime}$ | 0.003 | 0.153 | 0.001 | 0.002 | -0.001 | -17.452 | 0.058 | -0.279 |
| N3 | 0.002 | 0.080 | 0.000 | 0.001 | -0.001 | -13.663 | 0.046 | -0.258 |
| O1 | 0.002 | 0.129 | 0.001 | 0.002 | -0.001 | -22.979 | 0.054 | -0.306 |
| F1 | 0.001 | 0.031 | 0.000 | 0.000 | 0.000 | -0.423 | 0.034 | -0.081 |
| F2 | 0.001 | 0.050 | 0.000 | 0.001 | 0.000 | -0.666 | 0.040 | -0.094 |
| F3 | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | -0.423 | 0.027 | -0.081 |
| C1 | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | 2.535 | 0.014 | 0.147 |
| C2 | 0.001 | 0.058 | 0.000 | 0.001 | 0.000 | -4.739 | 0.042 | -0.181 |
| C3 | 0.001 | 0.043 | 0.000 | 0.000 | 0.000 | 1.491 | 0.038 | 0.123 |
| C4 | 0.000 | 0.018 | 0.000 | 0.000 | 0.000 | 1.794 | 0.028 | 0.131 |
| C5 | 0.001 | 0.075 | 0.001 | 0.001 | 0.000 | -5.524 | 0.045 | -0.190 |
| C6 | 0.001 | 0.038 | 0.000 | 0.000 | 0.000 | -2.066 | 0.036 | -0.137 |
| C7 | 0.000 | 0.007 | 0.000 | 0.000 | 0.000 | -3.481 | 0.020 | -0.163 |
| C8 | 0.001 | 0.028 | 0.000 | 0.000 | 0.000 | -3.583 | 0.033 | -0.165 |
| C9 | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | -4.622 | 0.025 | -0.179 |
| H1 | 0.001 | 0.041 | 0.000 | 0.000 | 0.000 | 0.362 | 0.037 | 0.077 |
| H2 | 0.001 | 0.072 | 0.001 | 0.001 | 0.000 | 0.799 | 0.045 | 0.100 |
| H3 | 0.000 | 0.021 | 0.000 | 0.000 | 0.000 | 0.023 | 0.030 | 0.031 |
| H4 | 0.001 | 0.032 | 0.000 | 0.000 | 0.000 | 0.402 | 0.034 | 0.079 |
| H5 | 0.001 | 0.063 | 0.001 | 0.001 | 0.000 | 0.472 | 0.043 | 0.084 |
| H6 | 0.001 | 0.027 | 0.000 | 0.000 | 0.000 | 0.391 | 0.032 | 0.079 |
| H7 | 0.000 | 0.019 | 0.000 | 0.000 | 0.000 | -0.200 | 0.029 | -0.063 |
| H8 | 0.000 | 0.022 | 0.000 | 0.000 | 0.000 | -0.194 | 0.030 | -0.062 |
| H9 | 0.001 | 0.031 | 0.000 | 0.000 | 0.000 | -0.042 | 0.034 | -0.038 |
| H10 | 0.001 | 0.075 | 0.001 | 0.001 | 0.000 | 0.378 | 0.045 | 0.078 |
| H11 | 0.001 | 0.032 | 0.000 | 0.000 | 0.000 | 0.219 | 0.034 | 0.065 |
| H12 | 0.001 | 0.059 | 0.001 | 0.001 | 0.000 | 0.037 | 0.042 | 0.036 |
| H13 | 0.001 | 0.061 | 0.001 | 0.001 | 0.000 | 0.225 | 0.042 | 0.066 |


| H14 | 0.001 | 0.057 | 0.001 | 0.001 | 0.000 | -0.084 | 0.042 | -0.047 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1' | 0.000 | -0.004 | 0.000 | 0.000 | 0.001 | 13.047 | -0.017 | 0.254 |
| N1' | 0.000 | -0.017 | 0.000 | 0.000 | 0.000 | -0.291 | -0.028 | -0.071 |
| N2' | 0.000 | -0.019 | 0.000 | 0.000 | 0.000 | 0.356 | -0.029 | 0.076 |
| N5 | 0.003 | 0.164 | 0.002 | 0.001 | 0.001 | 13.974 | 0.059 | 0.259 |
| N4 | 0.001 | 0.042 | 0.000 | 0.001 | -0.001 | -13.674 | 0.038 | -0.258 |
| N3' | 0.003 | 0.144 | 0.001 | 0.001 | 0.000 | -1.419 | 0.056 | -0.121 |
| O1' | -0.001 | -0.043 | -0.001 | 0.000 | 0.000 | -4.255 | -0.038 | -0.175 |
| F1' | 0.000 | 0.009 | 0.000 | 0.000 | 0.000 | -0.287 | 0.023 | -0.071 |
| F2' | 0.001 | 0.027 | 0.000 | 0.000 | 0.000 | -0.440 | 0.032 | -0.082 |
| F3' | 0.000 | -0.022 | 0.000 | 0.000 | 0.000 | -0.307 | -0.030 | -0.073 |
| C1' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 1.572 | 0.011 | 0.125 |
| C2' | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | -2.463 | 0.021 | -0.145 |
| C3' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | 0.687 | 0.023 | 0.095 |
| C4' | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | 0.868 | 0.016 | 0.103 |
| C5' | 0.000 | 0.009 | 0.000 | 0.000 | 0.000 | -2.324 | 0.022 | -0.143 |
| C6' | 0.000 | 0.007 | 0.000 | 0.000 | 0.000 | -0.804 | 0.021 | -0.100 |
| C7' | 0.000 | 0.005 | 0.000 | 0.000 | 0.000 | -1.467 | 0.018 | -0.122 |
| C8' | 0.000 | 0.007 | 0.000 | 0.000 | 0.000 | -1.651 | 0.020 | -0.127 |
| C9' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | -2.448 | -0.013 | -0.145 |
| H1' | 0.000 | -0.013 | 0.000 | 0.000 | 0.000 | 0.225 | -0.026 | 0.066 |
| H2' | 0.001 | 0.027 | 0.000 | 0.000 | 0.000 | 0.527 | 0.032 | 0.087 |
| H3' | 0.000 | -0.023 | 0.000 | 0.000 | 0.000 | 0.006 | -0.031 | 0.020 |
| H4' | 0.000 | -0.006 | 0.000 | 0.000 | 0.000 | 0.204 | -0.019 | 0.063 |
| H5' | 0.000 | 0.015 | 0.000 | 0.000 | 0.000 | 0.250 | 0.026 | 0.068 |
| H6' | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | 0.160 | 0.025 | 0.059 |
| H7' | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | -0.107 | 0.015 | -0.051 |
| H8' | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | -0.101 | 0.021 | -0.050 |
| H9' | 0.000 | 0.007 | 0.000 | 0.000 | 0.000 | -0.023 | 0.021 | -0.031 |
| H10' | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | 0.181 | 0.027 | 0.061 |
| H11' | 0.000 | -0.008 | 0.000 | 0.000 | 0.000 | 0.093 | -0.021 | 0.049 |
| H12' | 0.000 | 0.013 | 0.000 | 0.000 | 0.000 | 0.016 | 0.025 | 0.027 |
| H13' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | 0.105 | 0.023 | 0.051 |
| H14' | 0.000 | 0.015 | 0.000 | 0.000 | 0.000 | -0.046 | 0.026 | -0.039 |

Table A2.15: Contributions at the CD along the $\mathrm{Cu}-\mathrm{N} 3$ bond for the EE molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}$,
$\mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\mathrm{FSs}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 9.135 | 99.711 | 5.114 | 4.021 | 1.093 | 100.271 | 0.500 | 0.500 |
| N 1 | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | -0.035 | 0.016 | -0.035 |
| N 2 | -0.001 | -0.016 | -0.001 | 0.000 | -0.001 | -0.048 | -0.027 | -0.039 |
| $\mathrm{~N}^{\prime}$ | -0.002 | -0.019 | 0.000 | -0.001 | 0.001 | 0.091 | -0.029 | 0.048 |
| $\mathrm{~N}^{\prime}$ | 0.002 | 0.018 | 0.000 | 0.001 | -0.001 | -0.071 | 0.028 | -0.045 |
| N3 | 0.003 | 0.033 | 0.001 | 0.002 | -0.001 | -0.093 | 0.034 | -0.049 |
| O1 | 0.003 | 0.033 | 0.001 | 0.002 | -0.001 | -0.115 | 0.034 | -0.052 |
| F1 | 0.000 | 0.005 | 0.000 | 0.000 | 0.000 | -0.002 | 0.019 | -0.014 |


| F2 | 0.001 | 0.011 | 0.000 | 0.001 | 0.000 | -0.003 | 0.024 | -0.016 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| F3 | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | -0.002 | 0.018 | -0.014 |
| C1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.012 | 0.008 | 0.025 |
| C2 | 0.001 | 0.013 | 0.000 | 0.001 | 0.000 | -0.022 | 0.026 | -0.030 |
| C3 | 0.001 | 0.009 | 0.000 | 0.000 | 0.000 | 0.007 | 0.023 | 0.021 |
| C4 | 0.001 | 0.015 | 0.001 | 0.001 | 0.000 | -0.026 | 0.026 | -0.032 |
| C5 | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | 0.008 | 0.016 | 0.022 |
| C6 | 0.001 | 0.007 | 0.000 | 0.000 | 0.000 | -0.010 | 0.021 | -0.023 |
| C7 | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | -0.016 | 0.018 | -0.027 |
| C8 | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | -0.019 | 0.017 | -0.029 |
| C9 | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | -0.022 | 0.017 | -0.030 |
| H1 | 0.001 | 0.007 | 0.000 | 0.000 | 0.000 | 0.002 | 0.021 | 0.013 |
| H2 | 0.001 | 0.015 | 0.001 | 0.001 | 0.000 | 0.004 | 0.027 | 0.017 |
| H3 | 0.001 | 0.007 | 0.000 | 0.000 | 0.000 | 0.000 | 0.021 | 0.006 |
| H4 | 0.001 | 0.007 | 0.000 | 0.000 | 0.000 | 0.002 | 0.020 | 0.014 |
| H5 | 0.001 | 0.016 | 0.001 | 0.001 | 0.000 | 0.002 | 0.027 | 0.015 |
| H6 | 0.001 | 0.006 | 0.000 | 0.000 | 0.000 | 0.002 | 0.020 | 0.014 |
| H7 | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | -0.001 | 0.018 | -0.011 |
| H8 | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | -0.001 | 0.017 | -0.011 |
| H9 | 0.001 | 0.006 | 0.000 | 0.000 | 0.000 | 0.000 | 0.020 | -0.006 |
| H10 | 0.001 | 0.015 | 0.001 | 0.001 | 0.000 | 0.002 | 0.026 | 0.013 |
| H11 | 0.001 | 0.009 | 0.000 | 0.000 | 0.000 | 0.001 | 0.022 | 0.011 |
| H12 | 0.001 | 0.011 | 0.000 | 0.000 | 0.000 | 0.000 | 0.024 | 0.006 |
| H13 | 0.001 | 0.013 | 0.001 | 0.001 | 0.000 | 0.001 | 0.025 | 0.011 |
| H14 | 0.001 | 0.012 | 0.001 | 0.001 | 0.000 | 0.000 | 0.024 | -0.008 |
| Cu1' | 0.000 | -0.001 | 0.000 | 0.000 | 0.001 | 0.060 | -0.011 | 0.042 |
| N1' | 0.000 | -0.004 | 0.000 | 0.000 | 0.000 | -0.001 | -0.016 | -0.011 |
| N2' | 0.000 | -0.004 | 0.000 | 0.000 | 0.000 | 0.002 | -0.017 | 0.013 |
| N5 | 0.004 | 0.039 | 0.002 | 0.001 | 0.001 | 0.067 | 0.036 | 0.044 |
| N4 | 0.002 | 0.025 | 0.001 | 0.002 | -0.001 | -0.066 | 0.032 | -0.044 |
| N3' | 0.002 | 0.024 | 0.001 | 0.001 | 0.000 | -0.007 | 0.031 | -0.021 |
| O1' | -0.001 | -0.008 | 0.000 | 0.000 | 0.000 | -0.019 | -0.022 | -0.029 |
| F1' | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | -0.001 | 0.014 | -0.012 |
| F2' | 0.000 | 0.005 | 0.000 | 0.000 | 0.000 | -0.002 | 0.019 | -0.014 |
| F3' | 0.000 | -0.005 | 0.000 | 0.000 | 0.000 | -0.001 | -0.018 | -0.012 |
| C1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.007 | 0.007 | 0.021 |
| C2' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.011 | 0.011 | -0.024 |
| C3' | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | 0.003 | 0.013 | 0.016 |
| C4' | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | -0.011 | 0.013 | -0.024 |
| C5' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.004 | 0.009 | 0.017 |
| C6' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.004 | 0.012 | -0.017 |
| C7' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.007 | 0.011 | -0.020 |
| C8' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.008 | 0.012 | -0.021 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.011 | -0.006 | -0.024 |
| H1' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.001 | -0.013 | 0.011 |
| H2' | 0.000 | 0.005 | 0.000 | 0.000 | 0.000 | 0.002 | 0.019 | 0.015 |
| H3' | -0.001 | -0.005 | 0.000 | 0.000 | 0.000 | 0.000 | -0.019 | 0.003 |
| H4' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | 0.001 | -0.010 | 0.010 |
| H5' | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | 0.001 | 0.015 | 0.011 |


| H6 | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | 0.001 | 0.014 | 0.010 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H7 $^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | 0.008 | -0.009 |
| H8 $^{\prime}$ | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | 0.000 | 0.013 | -0.008 |
| H9 $^{\prime}$ | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | 0.000 | 0.012 | -0.005 |
| H10 $^{\prime}$ | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | 0.001 | 0.016 | 0.010 |
| H11 $^{\prime}$ | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 0.000 | -0.014 | 0.008 |
| H12 $^{\prime}$ | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | 0.000 | 0.015 | 0.004 |
| H13 $^{\prime}$ | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | 0.000 | 0.013 | 0.009 |
| H14' $^{\prime}$ | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | 0.000 | 0.015 | -0.006 |

Table A2.16: Contributions at the Cu 1 atomic basin along the $\mathrm{Cu}-\mathrm{N} 5$ bond for the EE molecular system; $\mathrm{LS}, \mathrm{SF} \%$,
$\mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r})$. $\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1.

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\text {FSs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1 | 0.044 | 46.746 | 0.026 | 0.017 | 0.009 | 284.129 | 0.388 | 0.708 |
| N1 | -0.001 | -0.598 | 0.000 | 0.000 | 0.000 | -5.577 | -0.091 | -0.191 |
| N2 | -0.002 | -2.512 | -0.001 | -0.001 | 0.000 | -10.157 | -0.146 | -0.233 |
| N5 | -0.001 | -1.537 | 0.000 | -0.001 | 0.001 | 30.306 | -0.124 | 0.336 |
| N4 $^{\prime}$ | 0.001 | 0.870 | 0.000 | 0.001 | -0.001 | -24.220 | 0.103 | -0.312 |
| N3 | 0.021 | 22.961 | 0.009 | 0.013 | -0.004 | -117.241 | 0.306 | -0.527 |
| O1 | 0.001 | 0.938 | 0.000 | 0.001 | -0.001 | -30.361 | 0.105 | -0.336 |
| F1 | 0.000 | 0.309 | 0.000 | 0.000 | 0.000 | -0.705 | 0.073 | -0.096 |
| F2 | 0.001 | 1.017 | 0.000 | 0.000 | 0.000 | -1.035 | 0.108 | -0.109 |
| F3 | 0.000 | 0.301 | 0.000 | 0.000 | 0.000 | -0.672 | 0.072 | -0.094 |
| C1 | 0.000 | 0.002 | 0.000 | 0.000 | 0.000 | 3.909 | 0.012 | 0.170 |
| C2 | 0.001 | 1.158 | 0.000 | 0.001 | 0.000 | -7.127 | 0.113 | -0.207 |
| C3 | 0.001 | 0.734 | 0.000 | 0.000 | 0.000 | 2.089 | 0.097 | 0.138 |
| C4 | 0.001 | 0.877 | 0.000 | 0.001 | 0.000 | -7.455 | 0.103 | -0.210 |
| C5 | 0.000 | 0.231 | 0.000 | 0.000 | 0.000 | 2.526 | 0.066 | 0.147 |
| C6 | 0.000 | 0.450 | 0.000 | 0.000 | 0.000 | -2.740 | 0.083 | -0.151 |
| C7 | 0.000 | 0.499 | 0.000 | 0.000 | 0.000 | -5.002 | 0.085 | -0.184 |
| C8 | 0.000 | 0.208 | 0.000 | 0.000 | 0.000 | -6.427 | 0.064 | -0.200 |
| C9 | 0.000 | 0.066 | 0.000 | 0.000 | 0.000 | -7.863 | 0.044 | -0.214 |
| H1 | 0.000 | 0.250 | 0.000 | 0.000 | 0.000 | 0.712 | 0.068 | 0.096 |
| H2 | 0.001 | 1.548 | 0.001 | 0.001 | 0.000 | 1.365 | 0.125 | 0.119 |
| H3 | 0.001 | 0.847 | 0.000 | 0.000 | 0.000 | 0.053 | 0.102 | 0.040 |
| H4 | 0.000 | 0.110 | 0.000 | 0.000 | 0.000 | 0.853 | 0.052 | 0.102 |
| H5 | 0.001 | 1.510 | 0.001 | 0.001 | 0.000 | 0.851 | 0.124 | 0.102 |
| H6 | 0.001 | 0.823 | 0.000 | 0.000 | 0.000 | 0.686 | 0.101 | 0.095 |
| H7 | 0.000 | 0.350 | 0.000 | 0.000 | 0.000 | -0.284 | 0.076 | -0.071 |
| H8 | 0.000 | 0.258 | 0.000 | 0.000 | 0.000 | -0.286 | 0.069 | -0.071 |
| H9 | 0.000 | 0.482 | 0.000 | 0.000 | 0.000 | -0.062 | 0.084 | -0.043 |
| H10 | 0.001 | 1.134 | 0.001 | 0.001 | 0.000 | 0.542 | 0.112 | 0.088 |
| H11 | 0.001 | 0.648 | 0.000 | 0.000 | 0.000 | 0.285 | 0.093 | 0.071 |
| H12 | 0.001 | 0.703 | 0.000 | 0.000 | 0.000 | 0.055 | 0.096 | 0.041 |
| H13 | 0.001 | 0.948 | 0.000 | 0.000 | 0.000 | 0.311 | 0.106 | 0.073 |


| H14 | 0.001 | 0.906 | 0.000 | 0.000 | 0.000 | -0.123 | 0.104 | -0.054 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1' | 0.000 | -0.145 | 0.000 | 0.000 | 0.001 | 22.218 | -0.057 | 0.303 |
| N1' | 0.000 | -0.412 | 0.000 | 0.000 | 0.000 | -0.489 | -0.080 | -0.085 |
| N2' | 0.000 | -0.409 | 0.000 | 0.000 | 0.000 | 0.550 | -0.080 | 0.088 |
| N5 | 0.006 | 5.947 | 0.003 | 0.002 | 0.001 | 28.234 | 0.195 | 0.328 |
| N4 | 0.008 | 8.191 | 0.003 | 0.004 | -0.001 | -27.972 | 0.217 | -0.327 |
| N3' | 0.002 | 2.214 | 0.001 | 0.001 | 0.000 | -2.838 | 0.140 | -0.153 |
| O1' | -0.001 | -0.859 | -0.001 | 0.000 | 0.000 | -7.328 | -0.102 | -0.209 |
| F1' | 0.000 | 0.319 | 0.000 | 0.000 | 0.000 | -0.486 | 0.074 | -0.085 |
| F2' | 0.001 | 0.548 | 0.000 | 0.000 | 0.000 | -0.770 | 0.088 | -0.099 |
| F3' | 0.000 | -0.535 | 0.000 | 0.000 | 0.000 | -0.535 | -0.087 | -0.087 |
| C1' | 0.000 | 0.017 | 0.000 | 0.000 | 0.000 | 2.747 | 0.028 | 0.151 |
| C2' | 0.000 | 0.096 | 0.000 | 0.000 | 0.000 | -4.299 | 0.049 | -0.175 |
| C3' | 0.000 | 0.183 | 0.000 | 0.000 | 0.000 | 1.215 | 0.061 | 0.115 |
| C4' | 0.000 | 0.172 | 0.000 | 0.000 | 0.000 | -4.116 | 0.060 | -0.173 |
| C5' | 0.000 | 0.071 | 0.000 | 0.000 | 0.000 | 1.537 | 0.045 | 0.124 |
| C6' | 0.000 | 0.153 | 0.000 | 0.000 | 0.000 | -1.420 | 0.058 | -0.121 |
| C7' | 0.000 | 0.095 | 0.000 | 0.000 | 0.000 | -2.555 | 0.049 | -0.147 |
| C8' | 0.000 | 0.156 | 0.000 | 0.000 | 0.000 | -2.747 | 0.058 | -0.151 |
| C9' | 0.000 | -0.007 | 0.000 | 0.000 | 0.000 | -4.128 | -0.021 | -0.173 |
| H1' | 0.000 | -0.069 | 0.000 | 0.000 | 0.000 | 0.364 | -0.044 | 0.077 |
| H2' | 0.001 | 0.553 | 0.000 | 0.000 | 0.000 | 0.884 | 0.088 | 0.103 |
| H3' | -0.001 | -0.667 | 0.000 | 0.000 | 0.000 | 0.003 | -0.094 | 0.016 |
| H4' | 0.000 | -0.032 | 0.000 | 0.000 | 0.000 | 0.328 | -0.034 | 0.074 |
| H5' | 0.000 | 0.299 | 0.000 | 0.000 | 0.000 | 0.413 | 0.072 | 0.080 |
| H6' | 0.000 | 0.239 | 0.000 | 0.000 | 0.000 | 0.268 | 0.067 | 0.069 |
| H7' | 0.000 | 0.040 | 0.000 | 0.000 | 0.000 | -0.191 | 0.037 | -0.062 |
| H8' | 0.000 | 0.193 | 0.000 | 0.000 | 0.000 | -0.177 | 0.062 | -0.061 |
| H9' | 0.000 | 0.167 | 0.000 | 0.000 | 0.000 | -0.041 | 0.059 | -0.037 |
| H10' | 0.000 | 0.368 | 0.000 | 0.000 | 0.000 | 0.320 | 0.077 | 0.074 |
| H11' | 0.000 | -0.271 | 0.000 | 0.000 | 0.000 | 0.168 | -0.070 | 0.059 |
| H12' | 0.000 | 0.310 | 0.000 | 0.000 | 0.000 | 0.027 | 0.073 | 0.032 |
| H13' | 0.000 | 0.186 | 0.000 | 0.000 | 0.000 | 0.186 | 0.061 | 0.061 |
| H14' | 0.000 | 0.321 | 0.000 | 0.000 | 0.000 | -0.081 | 0.074 | -0.047 |

Table A2.17: Contributions at the bcp along the $\mathrm{Cu}-\mathrm{N} 5$ bond for the EE molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}$,
$\mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $\mathrm{s}(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r})$. $\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {FSs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 0.005 | 0.725 | 0.003 | 0.001 | 0.002 | 8.424 | 0.097 | 0.219 |
| N 1 | -0.001 | -0.094 | 0.000 | 0.000 | 0.000 | -0.340 | -0.049 | -0.075 |
| N 2 | -0.002 | -0.335 | -0.001 | -0.001 | 0.000 | -0.426 | -0.075 | -0.081 |
| $\mathrm{~N}^{\prime}$ | -0.001 | -0.133 | 0.000 | -0.001 | 0.001 | 3.190 | -0.055 | 0.159 |
| N4' | 0.000 | -0.007 | 0.000 | 0.000 | -0.001 | -2.674 | -0.020 | -0.150 |
| N3 | 0.597 | 92.021 | 0.311 | 0.286 | 0.025 | 96.902 | 0.486 | 0.495 |
| O1 | -0.001 | -0.123 | -0.001 | 0.000 | -0.001 | -2.395 | -0.054 | -0.144 |
| F1 | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | -0.081 | 0.027 | -0.047 |


| F2 | 0.001 | 0.133 | 0.000 | 0.000 | 0.000 | -0.115 | 0.055 | -0.052 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| F3 | 0.000 | 0.025 | 0.000 | 0.000 | 0.000 | -0.076 | 0.031 | -0.046 |
| C1 | 0.000 | -0.003 | 0.000 | 0.000 | 0.000 | 0.429 | -0.015 | 0.081 |
| C2 | 0.001 | 0.121 | 0.000 | 0.000 | 0.000 | -0.754 | 0.053 | -0.098 |
| C3 | 0.001 | 0.080 | 0.000 | 0.000 | 0.000 | 0.214 | 0.046 | 0.064 |
| C4 | 0.001 | 0.079 | 0.000 | 0.000 | 0.000 | -0.750 | 0.046 | -0.098 |
| C5 | 0.000 | 0.023 | 0.000 | 0.000 | 0.000 | 0.262 | 0.031 | 0.069 |
| C6 | 0.000 | 0.045 | 0.000 | 0.000 | 0.000 | -0.272 | 0.038 | -0.070 |
| C7 | 0.000 | 0.060 | 0.000 | 0.000 | 0.000 | -0.514 | 0.042 | -0.086 |
| C8 | 0.000 | 0.026 | 0.000 | 0.000 | 0.000 | -0.706 | 0.032 | -0.096 |
| C9 | 0.000 | -0.006 | 0.000 | 0.000 | 0.000 | -0.889 | -0.019 | -0.104 |
| H1 | -0.001 | -0.087 | 0.000 | 0.000 | 0.000 | 0.091 | -0.048 | 0.049 |
| H2 | 0.001 | 0.207 | 0.001 | 0.001 | 0.000 | 0.162 | 0.064 | 0.059 |
| H3 | 0.001 | 0.117 | 0.000 | 0.000 | 0.000 | 0.006 | 0.053 | 0.020 |
| H4 | -0.001 | -0.096 | 0.000 | 0.000 | 0.000 | 0.105 | -0.049 | 0.051 |
| H5 | 0.001 | 0.188 | 0.001 | 0.001 | 0.000 | 0.098 | 0.062 | 0.050 |
| H6 | 0.001 | 0.120 | 0.000 | 0.000 | 0.000 | 0.072 | 0.053 | 0.045 |
| H7 | 0.000 | 0.040 | 0.000 | 0.000 | 0.000 | -0.030 | 0.037 | -0.034 |
| H8 | 0.000 | 0.025 | 0.000 | 0.000 | 0.000 | -0.030 | 0.032 | -0.034 |
| H9 | 0.000 | 0.053 | 0.000 | 0.000 | 0.000 | -0.007 | 0.040 | -0.020 |
| H10 | 0.001 | 0.118 | 0.000 | 0.000 | 0.000 | 0.057 | 0.053 | 0.041 |
| H11 | 0.000 | 0.066 | 0.000 | 0.000 | 0.000 | 0.029 | 0.043 | 0.033 |
| H12 | 0.000 | 0.065 | 0.000 | 0.000 | 0.000 | 0.006 | 0.043 | 0.019 |
| H13 | 0.001 | 0.101 | 0.000 | 0.000 | 0.000 | 0.032 | 0.050 | 0.034 |
| H14 | 0.001 | 0.100 | 0.000 | 0.000 | 0.000 | -0.013 | 0.050 | -0.025 |
| Cu1' | 0.000 | -0.029 | 0.000 | 0.000 | 0.001 | 2.835 | -0.033 | 0.152 |
| N1' | 0.000 | -0.072 | 0.000 | 0.000 | 0.000 | -0.065 | -0.045 | -0.043 |
| N2' | 0.000 | -0.066 | 0.000 | 0.000 | 0.000 | 0.056 | -0.044 | 0.041 |
| N5 | 0.009 | 1.406 | 0.005 | 0.004 | 0.001 | 4.215 | 0.121 | 0.174 |
| N4 | 0.030 | 4.682 | 0.015 | 0.016 | -0.001 | -4.233 | 0.180 | -0.174 |
| N3' | 0.002 | 0.265 | 0.001 | 0.001 | 0.000 | -0.394 | 0.069 | -0.079 |
| O1' | -0.001 | -0.127 | -0.001 | 0.000 | 0.000 | -0.948 | -0.054 | -0.106 |
| F1' | 0.000 | 0.062 | 0.000 | 0.000 | 0.000 | -0.061 | 0.043 | -0.042 |
| F2' | 0.001 | 0.082 | 0.000 | 0.000 | 0.000 | -0.099 | 0.047 | -0.050 |
| F3' | -0.001 | -0.084 | 0.000 | 0.000 | 0.000 | -0.068 | -0.047 | -0.044 |
| C1' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.354 | 0.010 | 0.076 |
| C2' | 0.000 | 0.005 | 0.000 | 0.000 | 0.000 | -0.556 | 0.019 | -0.089 |
| C3' | 0.000 | 0.024 | 0.000 | 0.000 | 0.000 | 0.159 | 0.031 | 0.058 |
| C4' | 0.000 | 0.025 | 0.000 | 0.000 | 0.000 | -0.538 | 0.031 | -0.088 |
| C5' | 0.000 | 0.012 | 0.000 | 0.000 | 0.000 | 0.200 | 0.024 | 0.063 |
| C6' | 0.000 | 0.023 | 0.000 | 0.000 | 0.000 | -0.185 | 0.031 | -0.061 |
| C7' | 0.000 | 0.013 | 0.000 | 0.000 | 0.000 | -0.328 | 0.026 | -0.074 |
| C8' | 0.000 | 0.025 | 0.000 | 0.000 | 0.000 | -0.341 | 0.031 | -0.075 |
| C9' | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | -0.514 | 0.017 | -0.086 |
| H1' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | 0.044 | 0.024 | 0.038 |
| H2' | 0.001 | 0.083 | 0.000 | 0.000 | 0.000 | 0.109 | 0.047 | 0.051 |
| H3' | -0.001 | -0.112 | 0.000 | 0.000 | 0.000 | 0.000 | -0.052 | -0.005 |
| H4' | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | 0.040 | 0.017 | 0.037 |
| H5' | 0.000 | 0.045 | 0.000 | 0.000 | 0.000 | 0.051 | 0.038 | 0.040 |


| H6 | 0.000 | 0.033 | 0.000 | 0.000 | 0.000 | 0.033 | 0.035 | 0.035 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H7 $^{\prime}$ | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | -0.025 | 0.017 | -0.031 |
| H8 $^{\prime}$ | 0.000 | 0.033 | 0.000 | 0.000 | 0.000 | -0.023 | 0.035 | -0.031 |
| H9 $^{\prime}$ | 0.000 | 0.027 | 0.000 | 0.000 | 0.000 | -0.005 | 0.032 | -0.019 |
| H10 $^{\prime}$ | 0.000 | 0.061 | 0.000 | 0.000 | 0.000 | 0.041 | 0.042 | 0.037 |
| H11 $^{\prime}$ | 0.000 | -0.054 | 0.000 | 0.000 | 0.000 | 0.022 | -0.041 | 0.030 |
| H12 $^{\prime}$ | 0.000 | 0.053 | 0.000 | 0.000 | 0.000 | 0.003 | 0.040 | 0.016 |
| H13 $^{\prime}$ | 0.000 | 0.026 | 0.000 | 0.000 | 0.000 | 0.024 | 0.032 | 0.031 |
| H14' $^{\prime}$ | 0.000 | 0.052 | 0.000 | 0.000 | 0.000 | -0.011 | 0.040 | -0.024 |

Table A2.18: Contributions at $0.05 \AA$ to the N 5 atomic basin along the $\mathrm{Cu}-\mathrm{N} 5$ bond for the EE molecular system; LS,
$\mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r})$. $\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FSs}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 0.003 | 0.001 | 0.002 | 0.000 | 0.002 | 2.792 | 0.012 | 0.152 |
| N 1 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.111 | -0.007 | -0.052 |
| N 2 | -0.002 | -0.001 | -0.001 | -0.001 | 0.000 | -0.104 | -0.011 | -0.051 |
| N 5 | -0.001 | 0.000 | 0.000 | -0.001 | 0.001 | 1.219 | -0.007 | 0.115 |
| $\mathrm{~N}^{\prime}$ | 0.000 | 0.000 | 0.000 | 0.000 | -0.001 | -1.039 | -0.005 | -0.109 |
| N3 | 98.616 | 49.635 | 99.340 | 99.277 | 0.063 | 99.148 | 0.396 | 0.499 |
| O1 | -0.001 | -0.001 | -0.001 | 0.000 | -0.001 | -0.842 | -0.009 | -0.102 |
| F1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.032 | 0.003 | -0.034 |
| F2 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.045 | 0.008 | -0.038 |
| F3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.030 | 0.004 | -0.033 |
| C1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.168 | -0.002 | 0.059 |
| C2 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.291 | 0.008 | -0.071 |
| C3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.082 | 0.007 | 0.047 |
| C4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.287 | 0.007 | -0.071 |
| C5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.101 | 0.004 | 0.050 |
| C6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.104 | 0.005 | -0.051 |
| C7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.197 | 0.006 | -0.063 |
| C8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.273 | 0.005 | -0.070 |
| C9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.347 | 0.002 | -0.076 |
| H1 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.037 | -0.008 | 0.036 |
| H2 | 0.001 | 0.001 | 0.001 | 0.001 | 0.000 | 0.064 | 0.009 | 0.043 |
| H3 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.003 | 0.008 | 0.015 |
| H4 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.042 | -0.008 | 0.037 |
| H5 | 0.001 | 0.001 | 0.001 | 0.001 | 0.000 | 0.039 | 0.009 | 0.036 |
| H6 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.027 | 0.008 | 0.032 |
| H7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.012 | 0.005 | -0.024 |
| H8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.012 | 0.004 | -0.025 |
| H9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.003 | 0.006 | -0.015 |
| H10 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.022 | 0.008 | 0.030 |
| H11 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.011 | 0.006 | 0.024 |
| H12 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.002 | 0.006 | 0.014 |


| H13 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.012 | 0.007 | 0.025 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H14 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.005 | 0.007 | -0.019 |
| Cu1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 1.168 | -0.005 | 0.113 |
| N1' | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.026 | -0.007 | -0.032 |
| N2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.022 | -0.007 | 0.030 |
| N5 | 0.011 | 0.005 | 0.006 | 0.005 | 0.001 | 1.842 | 0.019 | 0.132 |
| N4 | 0.045 | 0.023 | 0.022 | 0.023 | -0.001 | -1.796 | 0.031 | -0.131 |
| N3' | 0.002 | 0.001 | 0.001 | 0.001 | 0.000 | -0.167 | 0.010 | -0.059 |
| O1' | -0.001 | 0.000 | -0.001 | 0.000 | 0.000 | -0.392 | -0.008 | -0.079 |
| F1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.025 | 0.007 | -0.031 |
| F2' | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.041 | 0.007 | -0.037 |
| F3' | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.028 | -0.007 | -0.033 |
| C1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.147 | 0.001 | 0.057 |
| C2' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.231 | 0.001 | -0.066 |
| C3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.066 | 0.004 | 0.044 |
| C4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.225 | 0.005 | -0.066 |
| C5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.084 | 0.004 | 0.047 |
| C6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.077 | 0.005 | -0.046 |
| C7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.136 | 0.004 | -0.055 |
| C8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.139 | 0.005 | -0.056 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.210 | 0.003 | -0.064 |
| H1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.018 | 0.004 | 0.028 |
| H2' | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.044 | 0.007 | 0.038 |
| H3' | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.008 | -0.004 |
| H4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.016 | 0.003 | 0.027 |
| H5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.021 | 0.006 | 0.030 |
| H6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.014 | 0.005 | 0.026 |
| H7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.010 | 0.002 | -0.024 |
| H8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.010 | 0.005 | -0.023 |
| H9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.002 | 0.005 | -0.014 |
| H10' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.017 | 0.006 | 0.028 |
| H11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.009 | -0.006 | 0.023 |
| H12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 0.006 | 0.012 |
| H13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.010 | 0.005 | 0.023 |
| H14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.004 | 0.006 | -0.018 |

Table A2.19: Contributions at the N5 atomic basin along the N5-N4 bond for the EE molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}$
, $\mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FS}}\right)$ are evaluated as in tab A2.1

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FSS}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 0.001 | 0.305 | 0.001 | 0.000 | 0.002 | 1145.081 | 0.044 | 0.676 |
| N1 | -0.001 | -0.115 | 0.000 | 0.000 | 0.000 | -44.475 | -0.031 | -0.229 |
| N2 | -0.001 | -0.307 | -0.001 | -0.001 | 0.000 | -31.036 | -0.044 | -0.203 |
| N5 | 0.000 | -0.065 | 0.000 | -0.001 | 0.001 | 606.369 | -0.026 | 0.547 |
| N4' | -0.001 | -0.155 | -0.001 | 0.000 | -0.001 | -527.187 | -0.035 | -0.522 |
| N3 | 0.235 | 51.110 | 0.118 | 0.117 | 0.000 | 374.562 | 0.240 | 0.466 |


| O1 | -0.001 | -0.290 | -0.001 | 0.000 | 0.000 | -367.983 | -0.043 | -0.463 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| F1 | 0.000 | 0.011 | 0.000 | 0.000 | 0.000 | -15.313 | 0.014 | -0.161 |
| F2 | 0.001 | 0.182 | 0.000 | 0.000 | 0.000 | -21.551 | 0.037 | -0.180 |
| F3 | 0.000 | 0.003 | 0.000 | 0.000 | 0.000 | -14.702 | 0.009 | -0.158 |
| C1 | 0.000 | -0.005 | 0.000 | 0.000 | 0.000 | 79.827 | -0.011 | 0.278 |
| C2 | 0.001 | 0.144 | 0.000 | 0.000 | 0.000 | -137.233 | 0.034 | -0.333 |
| C3 | 0.000 | 0.100 | 0.000 | 0.000 | 0.000 | 37.772 | 0.030 | 0.217 |
| C4 | 0.000 | 0.026 | 0.000 | 0.000 | 0.000 | 46.130 | 0.019 | 0.232 |
| C5 | 0.000 | 0.085 | 0.000 | 0.000 | 0.000 | -129.573 | 0.028 | -0.327 |
| C6 | 0.000 | 0.054 | 0.000 | 0.000 | 0.000 | -46.032 | 0.024 | -0.232 |
| C7 | 0.000 | 0.061 | 0.000 | 0.000 | 0.000 | -86.509 | 0.025 | -0.286 |
| C8 | 0.000 | 0.046 | 0.000 | 0.000 | 0.000 | -114.501 | 0.023 | -0.314 |
| C9 | 0.000 | -0.014 | 0.000 | 0.000 | 0.000 | -152.820 | -0.016 | -0.346 |
| H1 | -0.001 | -0.190 | 0.000 | 0.000 | 0.000 | 16.180 | -0.037 | 0.163 |
| H2 | 0.001 | 0.248 | 0.001 | 0.001 | 0.000 | 29.175 | 0.041 | 0.199 |
| H3 | 0.000 | 0.100 | 0.000 | 0.000 | 0.000 | 0.912 | 0.030 | 0.063 |
| H4 | -0.001 | -0.138 | 0.000 | 0.000 | 0.000 | 16.734 | -0.033 | 0.165 |
| H5 | 0.001 | 0.195 | 0.000 | 0.000 | 0.000 | 16.505 | 0.037 | 0.165 |
| H6 | 0.001 | 0.128 | 0.000 | 0.000 | 0.000 | 11.405 | 0.033 | 0.145 |
| H7 | 0.000 | 0.045 | 0.000 | 0.000 | 0.000 | -5.367 | 0.023 | -0.113 |
| H8 | 0.000 | 0.033 | 0.000 | 0.000 | 0.000 | -5.369 | 0.021 | -0.113 |
| H9 | 0.000 | 0.060 | 0.000 | 0.000 | 0.000 | -1.190 | 0.025 | -0.068 |
| H10 | 0.001 | 0.131 | 0.000 | 0.000 | 0.000 | 9.807 | 0.033 | 0.138 |
| H11 | 0.000 | 0.054 | 0.000 | 0.000 | 0.000 | 5.030 | 0.024 | 0.111 |
| H12 | 0.000 | 0.074 | 0.000 | 0.000 | 0.000 | 0.942 | 0.027 | 0.063 |
| H13 | 0.001 | 0.110 | 0.000 | 0.000 | 0.000 | 5.576 | 0.031 | 0.115 |
| H14 | 0.001 | 0.119 | 0.000 | 0.000 | 0.000 | -2.355 | 0.032 | -0.086 |
| Cu1' | 0.000 | -0.062 | 0.000 | -0.001 | 0.001 | 621.262 | -0.026 | 0.552 |
| N1' | -0.001 | -0.135 | 0.000 | 0.000 | 0.000 | -17.267 | -0.033 | -0.167 |
| N2' | -0.001 | -0.120 | 0.000 | 0.000 | 0.000 | 7.296 | -0.032 | 0.125 |
| N5 | 0.019 | 4.107 | 0.010 | 0.009 | 0.002 | 1167.256 | 0.104 | 0.681 |
| N4 | 0.199 | 43.216 | 0.098 | 0.100 | -0.002 | -1694.383 | 0.227 | -0.771 |
| N3' | 0.002 | 0.359 | 0.001 | 0.001 | 0.000 | -92.719 | 0.046 | -0.293 |
| O1' | -0.001 | -0.201 | -0.001 | 0.000 | 0.000 | -213.065 | -0.038 | -0.386 |
| F1' | 0.000 | 0.106 | 0.000 | 0.000 | 0.000 | -12.460 | 0.031 | -0.150 |
| F2' | 0.001 | 0.126 | 0.000 | 0.000 | 0.000 | -20.496 | 0.032 | -0.177 |
| F3' | -0.001 | -0.113 | 0.000 | 0.000 | 0.000 | -14.089 | -0.031 | -0.156 |
| C1' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 73.747 | -0.008 | 0.271 |
| C2' | 0.000 | 0.004 | 0.000 | 0.000 | 0.000 | -117.966 | 0.010 | -0.317 |
| C3' | 0.000 | 0.034 | 0.000 | 0.000 | 0.000 | 34.191 | 0.021 | 0.210 |
| C4' | 0.000 | 0.020 | 0.000 | 0.000 | 0.000 | 43.006 | 0.017 | 0.226 |
| C5' | 0.000 | 0.041 | 0.000 | 0.000 | 0.000 | -116.782 | 0.022 | -0.316 |
| C6' | 0.000 | 0.038 | 0.000 | 0.000 | 0.000 | -40.463 | 0.022 | -0.222 |
| C7' | 0.000 | 0.020 | 0.000 | 0.000 | 0.000 | -71.486 | 0.018 | -0.268 |
| C8' | 0.000 | 0.042 | 0.000 | 0.000 | 0.000 | -72.193 | 0.023 | -0.269 |
| C9' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | -110.344 | 0.014 | -0.310 |
| H1' | 0.000 | 0.041 | 0.000 | 0.000 | 0.000 | 9.224 | 0.022 | 0.136 |
| H2' | 0.001 | 0.139 | 0.000 | 0.000 | 0.000 | 22.996 | 0.034 | 0.184 |
| H3' | -0.001 | -0.194 | 0.000 | 0.000 | 0.000 | -0.250 | -0.037 | -0.041 |


| H4' | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | 8.317 | 0.016 | 0.131 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}^{\prime}$ | 0.000 | 0.073 | 0.000 | 0.000 | 0.000 | 10.618 | 0.027 | 0.142 |
| $\mathrm{H}^{\prime}$ | 0.000 | 0.052 | 0.000 | 0.000 | 0.000 | 7.107 | 0.024 | 0.124 |
| H7 $^{\prime}$ | 0.000 | 0.005 | 0.000 | 0.000 | 0.000 | -5.338 | 0.011 | -0.113 |
| H8 $^{\prime}$ | 0.000 | 0.056 | 0.000 | 0.000 | 0.000 | -4.846 | 0.025 | -0.109 |
| H9 $^{\prime}$ | 0.000 | 0.047 | 0.000 | 0.000 | 0.000 | -1.136 | 0.023 | -0.067 |
| H10' $^{\prime}$ | 0.000 | 0.107 | 0.000 | 0.000 | 0.000 | 8.975 | 0.031 | 0.134 |
| H11 $^{\prime}$ | 0.000 | -0.100 | 0.000 | 0.000 | 0.000 | 4.970 | -0.030 | 0.110 |
| H12' $^{\prime}$ | 0.000 | 0.092 | 0.000 | 0.000 | 0.000 | 0.747 | 0.029 | 0.059 |
| H13' $^{\prime}$ | 0.000 | 0.044 | 0.000 | 0.000 | 0.000 | 5.277 | 0.023 | 0.113 |
| H14' $^{\prime}$ | 0.000 | 0.089 | 0.000 | 0.000 | 0.000 | -2.238 | 0.029 | -0.085 |

Table A2.20: Contributions at the bcp along the N5-N4 bond for the EE molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}$,
$\mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FS}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | 0.000 | 0.000 | 0.000 | -0.001 | 0.001 | 21.001 | -0.007 | 0.297 |
| N 1 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.764 | -0.008 | -0.098 |
| N 2 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.012 | -0.008 | 0.024 |
| $\mathrm{~N}^{\prime}$ | 0.052 | 0.026 | 0.027 | 0.025 | 0.003 | 56.442 | 0.032 | 0.413 |
| N4 | 98.337 | 49.555 | 99.165 | 99.172 | -0.008 | -167.819 | 0.396 | -0.594 |
| N3 | 0.002 | 0.001 | 0.001 | 0.001 | 0.000 | -3.404 | 0.010 | -0.162 |
| O1 | -0.001 | -0.001 | -0.001 | 0.000 | 0.000 | -7.430 | -0.009 | -0.210 |
| F1 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.381 | 0.007 | -0.078 |
| F2 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.629 | 0.007 | -0.092 |
| F3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.428 | -0.006 | -0.081 |
| C1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2.283 | -0.002 | 0.142 |
| C2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -3.738 | 0.003 | -0.167 |
| C3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1.102 | 0.005 | 0.111 |
| C4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -3.817 | 0.005 | -0.168 |
| C5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1.385 | 0.004 | 0.120 |
| C6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.348 | 0.005 | -0.119 |
| C7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -2.397 | 0.004 | -0.144 |
| C8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -2.358 | 0.005 | -0.143 |
| C9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -3.672 | 0.003 | -0.166 |
| H1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.302 | 0.006 | 0.072 |
| H2 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.748 | 0.008 | 0.098 |
| H3 | -0.001 | -0.001 | -0.001 | -0.001 | 0.000 | -0.019 | -0.009 | -0.029 |
| H4 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.268 | 0.004 | 0.069 |
| H5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.341 | 0.006 | 0.075 |
| H6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.232 | 0.006 | 0.066 |
| H7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.171 | 0.003 | -0.060 |
| H8 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.155 | 0.006 | -0.058 |
| H9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.036 | 0.006 | -0.036 |
| H10 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.297 | 0.007 | 0.072 |
| H11 | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.172 | -0.007 | 0.060 |
| H12 | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.025 | 0.007 | 0.031 |


| H13 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.174 | 0.006 | 0.060 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H14 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.071 | 0.007 | -0.045 |
| Cu1' | 0.000 | 0.000 | 0.001 | 0.000 | 0.001 | 27.133 | 0.007 | 0.324 |
| N1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.990 | -0.007 | -0.107 |
| N2' | -0.001 | -0.001 | -0.001 | 0.000 | 0.000 | -0.378 | -0.009 | -0.078 |
| N5 | 0.000 | 0.000 | 0.001 | 0.000 | 0.001 | 17.831 | 0.006 | 0.281 |
| N4 | -0.001 | -0.001 | -0.001 | 0.000 | -0.001 | -16.057 | -0.010 | -0.272 |
| N3' | 0.046 | 0.023 | 0.023 | 0.023 | 0.000 | 7.464 | 0.031 | 0.211 |
| O1' | -0.002 | -0.001 | -0.001 | -0.001 | 0.000 | -9.100 | -0.010 | -0.225 |
| F1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.441 | 0.003 | -0.082 |
| F2' | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -0.620 | 0.008 | -0.092 |
| F3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.435 | -0.004 | -0.082 |
| C1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2.282 | -0.002 | 0.142 |
| C2' | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | -3.853 | 0.007 | -0.169 |
| C3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1.038 | 0.006 | 0.109 |
| C4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -3.505 | 0.006 | -0.164 |
| C5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1.262 | 0.004 | 0.116 |
| C6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.223 | 0.005 | -0.115 |
| C7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -2.271 | 0.005 | -0.142 |
| C8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -2.876 | 0.005 | -0.153 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -3.974 | -0.004 | -0.171 |
| H1' | -0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.411 | -0.008 | 0.080 |
| H2' | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.785 | 0.008 | 0.099 |
| H3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.018 | 0.005 | 0.028 |
| H4' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.402 | -0.007 | 0.080 |
| H5' | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.423 | 0.008 | 0.081 |
| H6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.285 | 0.007 | 0.071 |
| H7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.148 | 0.005 | -0.057 |
| H8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.147 | 0.005 | -0.057 |
| H9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.033 | 0.005 | -0.035 |
| H10' | 0.001 | 0.000 | 0.000 | 0.000 | 0.000 | 0.263 | 0.007 | 0.069 |
| H11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.136 | 0.004 | 0.055 |
| H12' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.024 | 0.006 | 0.031 |
| H13' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.150 | 0.006 | 0.057 |
| H14' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.066 | 0.007 | -0.043 |

Table A2.21: Contributions at the N4 atomic basin along the N5-N4 bond for the EE molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}$
, $\mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r})$. $\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {FSs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu1 | -0.001 | -0.125 | 0.000 | -0.001 | 0.001 | 241.723 | -0.032 | 0.403 |
| N1 | -0.001 | -0.224 | -0.001 | -0.001 | 0.000 | -11.404 | -0.039 | -0.145 |
| N2 | -0.001 | -0.214 | -0.001 | -0.001 | 0.000 | -3.144 | -0.039 | -0.095 |
| N5' | 0.247 | 49.369 | 0.126 | 0.121 | 0.005 | 1044.505 | 0.237 | 0.656 |
| N4' | 0.231 | 46.077 | 0.113 | 0.118 | -0.004 | -965.036 | 0.232 | -0.639 |
| N3 | 0.001 | 0.258 | 0.001 | 0.001 | 0.000 | -43.260 | 0.041 | -0.227 |


| O1 | -0.001 | -0.190 | -0.001 | 0.000 | 0.000 | -88.018 | -0.037 | -0.288 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| F1 | 0.001 | 0.115 | 0.000 | 0.000 | 0.000 | -3.937 | 0.031 | -0.102 |
| F2 | 0.001 | 0.132 | 0.000 | 0.000 | 0.000 | -6.533 | 0.033 | -0.121 |
| F3 | 0.000 | -0.060 | 0.000 | 0.000 | 0.000 | -4.359 | -0.025 | -0.106 |
| C1 | 0.000 | -0.005 | 0.000 | 0.000 | 0.000 | 23.886 | -0.011 | 0.186 |
| C2 | 0.000 | 0.018 | 0.000 | 0.000 | 0.000 | -39.945 | 0.017 | -0.221 |
| C3 | 0.000 | 0.042 | 0.000 | 0.000 | 0.000 | 12.125 | 0.022 | 0.148 |
| C4 | 0.000 | 0.067 | 0.000 | 0.000 | 0.000 | -42.890 | 0.026 | -0.226 |
| C5 | 0.000 | 0.028 | 0.000 | 0.000 | 0.000 | 15.314 | 0.020 | 0.161 |
| C6 | 0.000 | 0.052 | 0.000 | 0.000 | 0.000 | -15.575 | 0.024 | -0.161 |
| C7 | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | -27.859 | 0.016 | -0.196 |
| C8 | 0.000 | 0.063 | 0.000 | 0.000 | 0.000 | -26.436 | 0.026 | -0.193 |
| C9 | 0.000 | 0.016 | 0.000 | 0.000 | 0.000 | -41.814 | 0.016 | -0.224 |
| H1 | 0.001 | 0.110 | 0.000 | 0.000 | 0.000 | 3.331 | 0.031 | 0.097 |
| H2 | 0.001 | 0.196 | 0.001 | 0.000 | 0.000 | 8.276 | 0.038 | 0.131 |
| H3 | -0.001 | -0.247 | -0.001 | -0.001 | 0.000 | -0.300 | -0.041 | -0.043 |
| H4 | 0.000 | 0.043 | 0.000 | 0.000 | 0.000 | 2.947 | 0.023 | 0.093 |
| H5 | 0.000 | 0.099 | 0.000 | 0.000 | 0.000 | 3.756 | 0.030 | 0.100 |
| H6 | 0.000 | 0.067 | 0.000 | 0.000 | 0.000 | 2.597 | 0.026 | 0.089 |
| H7 | 0.000 | 0.008 | 0.000 | 0.000 | 0.000 | -1.876 | 0.013 | -0.080 |
| H8 | 0.000 | 0.067 | 0.000 | 0.000 | 0.000 | -1.693 | 0.026 | -0.077 |
| H9 | 0.000 | 0.068 | 0.000 | 0.000 | 0.000 | -0.387 | 0.026 | -0.047 |
| H10 | 0.001 | 0.163 | 0.000 | 0.000 | 0.000 | 3.401 | 0.035 | 0.097 |
| H11 | -0.001 | -0.149 | 0.000 | 0.000 | 0.000 | 2.096 | -0.034 | 0.083 |
| H12 | 0.001 | 0.132 | 0.000 | 0.000 | 0.000 | 0.286 | 0.033 | 0.043 |
| H13 | 0.000 | 0.074 | 0.000 | 0.000 | 0.000 | 1.994 | 0.027 | 0.081 |
| H14 | 0.001 | 0.118 | 0.000 | 0.000 | 0.000 | -0.763 | 0.032 | -0.059 |
| Cu1' | 0.000 | 0.032 | 0.001 | 0.000 | 0.001 | 226.618 | 0.021 | 0.394 |
| N1' | 0.000 | -0.083 | 0.000 | 0.000 | 0.000 | -7.423 | -0.028 | -0.126 |
| N2' | -0.001 | -0.145 | 0.000 | 0.000 | 0.000 | -0.506 | -0.034 | -0.052 |
| N5 | 0.001 | 0.216 | 0.001 | 0.000 | 0.001 | 170.606 | 0.039 | 0.358 |
| N4 | -0.002 | -0.327 | -0.001 | 0.000 | -0.001 | -158.360 | -0.045 | -0.350 |
| N3' | 0.017 | 3.471 | 0.009 | 0.009 | 0.000 | 15.150 | 0.098 | 0.160 |
| O1' | -0.002 | -0.303 | -0.001 | -0.001 | 0.000 | -76.249 | -0.043 | -0.274 |
| F1' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | -4.270 | 0.014 | -0.105 |
| F2' | 0.001 | 0.157 | 0.000 | 0.000 | 0.000 | -6.036 | 0.035 | -0.118 |
| F3' | 0.000 | -0.053 | 0.000 | 0.000 | 0.000 | -4.302 | -0.024 | -0.105 |
| C1' | 0.000 | -0.002 | 0.000 | 0.000 | 0.000 | 22.058 | -0.008 | 0.181 |
| C2' | 0.000 | 0.092 | 0.000 | 0.000 | 0.000 | -36.456 | 0.029 | -0.214 |
| C3' | 0.000 | 0.074 | 0.000 | 0.000 | 0.000 | 9.728 | 0.027 | 0.138 |
| C4' | 0.000 | 0.054 | 0.000 | 0.000 | 0.000 | -32.533 | 0.024 | -0.206 |
| C5' | 0.000 | 0.018 | 0.000 | 0.000 | 0.000 | 11.840 | 0.017 | 0.147 |
| C6' | 0.000 | 0.038 | 0.000 | 0.000 | 0.000 | -11.198 | 0.022 | -0.145 |
| C7' | 0.000 | 0.033 | 0.000 | 0.000 | 0.000 | -20.579 | 0.021 | -0.177 |
| C8' | 0.000 | 0.033 | 0.000 | 0.000 | 0.000 | -25.360 | 0.021 | -0.190 |
| C9' | 0.000 | -0.012 | 0.000 | 0.000 | 0.000 | -35.484 | -0.015 | -0.212 |
| H1' | -0.001 | -0.134 | 0.000 | 0.000 | 0.000 | 3.575 | -0.033 | 0.099 |
| H2' | 0.001 | 0.158 | 0.000 | 0.000 | 0.000 | 7.207 | 0.035 | 0.125 |
| H3' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | 0.143 | -0.007 | 0.034 |


| H4' | 0.000 | -0.072 | 0.000 | 0.000 | 0.000 | 3.444 | -0.027 | 0.098 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H5' | 0.001 | 0.106 | 0.000 | 0.000 | 0.000 | 3.785 | 0.031 | 0.101 |
| H6' | 0.000 | 0.071 | 0.000 | 0.000 | 0.000 | 2.514 | 0.027 | 0.088 |
| H7' | 0.000 | 0.029 | 0.000 | 0.000 | 0.000 | -1.405 | 0.020 | -0.072 |
| H8' | 0.000 | 0.030 | 0.000 | 0.000 | 0.000 | -1.377 | 0.020 | -0.072 |
| H9' | 0.000 | 0.040 | 0.000 | 0.000 | 0.000 | -0.314 | 0.022 | -0.044 |
| H10' | 0.000 | 0.086 | 0.000 | 0.000 | 0.000 | 2.430 | 0.028 | 0.087 |
| H11' | 0.000 | 0.010 | 0.000 | 0.000 | 0.000 | 1.245 | 0.014 | 0.070 |
| H12' | 0.000 | 0.054 | 0.000 | 0.000 | 0.000 | 0.221 | 0.024 | 0.039 |
| H13' | 0.000 | 0.067 | 0.000 | 0.000 | 0.000 | 1.397 | 0.026 | 0.072 |
| H14' | 0.000 | 0.084 | 0.000 | 0.000 | 0.000 | -0.625 | 0.028 | -0.055 |

Table A2.22: Contributions at the bcp along the $\mathrm{N} 4-\mathrm{N} 3$ bond for the EE molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}$,
$\mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta,
the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r}) . \mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FS}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cu 1 | -0.001 | -0.002 | 0.000 | -0.001 | 0.001 | 117.395 | -0.013 | 0.527 |
| N 1 | -0.001 | -0.003 | -0.001 | -0.001 | 0.000 | -6.773 | -0.016 | -0.204 |
| N 2 | -0.001 | -0.003 | -0.001 | -0.001 | 0.000 | -3.009 | -0.016 | -0.156 |
| $\mathrm{~N}^{\prime}$ | 45.422 | 99.828 | 22.713 | 22.709 | 0.004 | 370.279 | 0.500 | 0.774 |
| $\mathrm{~N}^{\prime}$ | 0.060 | 0.131 | 0.028 | 0.031 | -0.003 | -262.580 | 0.055 | -0.690 |
| N 3 | 0.001 | 0.002 | 0.000 | 0.001 | 0.000 | -22.428 | 0.014 | -0.304 |
| O1 | -0.001 | -0.002 | -0.001 | 0.000 | 0.000 | -43.371 | -0.013 | -0.378 |
| F 1 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | -1.758 | 0.012 | -0.130 |
| F 2 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | -2.931 | 0.012 | -0.154 |
| F3 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.919 | -0.008 | -0.134 |
| C1 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 10.761 | -0.004 | 0.238 |
| C2 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -18.245 | 0.007 | -0.284 |
| C3 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 5.702 | 0.009 | 0.192 |
| C4 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -20.633 | 0.011 | -0.295 |
| C5 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 7.270 | 0.008 | 0.209 |
| C6 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -7.716 | 0.009 | -0.213 |
| C7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -13.858 | 0.005 | -0.259 |
| C8 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -12.692 | 0.010 | -0.251 |
| C9 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -20.222 | 0.006 | -0.293 |
| H1 | 0.001 | 0.002 | 0.000 | 0.000 | 0.000 | 1.561 | 0.013 | 0.125 |
| H2 | 0.001 | 0.002 | 0.001 | 0.001 | 0.000 | 3.903 | 0.015 | 0.170 |
| H3 | -0.001 | -0.003 | -0.001 | -0.001 | 0.000 | -0.146 | -0.015 | -0.057 |
| H4 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 1.388 | 0.009 | 0.120 |
| H5 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | 1.777 | 0.012 | 0.130 |
| H6 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 1.247 | 0.010 | 0.116 |
| H7 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.887 | 0.005 | -0.103 |
| H8 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.799 | 0.010 | -0.100 |
| H9 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.180 | 0.010 | -0.061 |
| H10 | 0.001 | 0.002 | 0.001 | 0.000 | 0.000 | 1.669 | 0.014 | 0.128 |
| H11 | -0.001 | -0.002 | 0.000 | 0.000 | 0.000 | 1.088 | -0.014 | 0.111 |
| H12 | 0.001 | 0.002 | 0.000 | 0.000 | 0.000 | 0.141 | 0.013 | 0.056 |


| H13 | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.978 | 0.011 | 0.107 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| H14 | 0.001 | 0.001 | 0.000 | 0.000 | 0.000 | -0.353 | 0.012 | -0.076 |
| Cu1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.001 | 88.766 | 0.006 | 0.481 |
| N1' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | -2.635 | -0.010 | -0.149 |
| N2' | -0.001 | -0.001 | 0.000 | 0.000 | 0.000 | 0.458 | -0.012 | 0.083 |
| N5 | 0.001 | 0.003 | 0.001 | 0.000 | 0.001 | 71.225 | 0.016 | 0.447 |
| N4 | -0.001 | -0.003 | -0.001 | 0.000 | -0.001 | -67.100 | -0.016 | -0.438 |
| N3' | 0.010 | 0.023 | 0.005 | 0.005 | 0.000 | -0.288 | 0.030 | -0.071 |
| O1' | -0.001 | -0.003 | -0.001 | -0.001 | 0.000 | -29.627 | -0.016 | -0.333 |
| F1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -1.820 | 0.005 | -0.132 |
| F2' | 0.001 | 0.002 | 0.000 | 0.000 | 0.000 | -2.589 | 0.013 | -0.148 |
| F3' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | -1.856 | -0.010 | -0.132 |
| C1' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 9.407 | -0.001 | 0.227 |
| C2' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -15.299 | 0.010 | -0.267 |
| C3' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 4.074 | 0.010 | 0.172 |
| C4' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -13.567 | 0.009 | -0.257 |
| C5' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 4.975 | 0.006 | 0.184 |
| C6' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -4.635 | 0.008 | -0.180 |
| C7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -8.457 | 0.007 | -0.219 |
| C8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -10.271 | 0.007 | -0.234 |
| C9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -14.414 | -0.005 | -0.262 |
| H1' | -0.001 | -0.001 | 0.000 | 0.000 | 0.000 | 1.425 | -0.012 | 0.121 |
| H2' | 0.001 | 0.002 | 0.000 | 0.000 | 0.000 | 2.975 | 0.012 | 0.155 |
| H3' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.059 | -0.006 | 0.042 |
| H4' | 0.000 | -0.001 | 0.000 | 0.000 | 0.000 | 1.372 | -0.009 | 0.120 |
| H5' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 1.547 | 0.011 | 0.125 |
| H6' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 1.018 | 0.009 | 0.108 |
| H7' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.594 | 0.007 | -0.091 |
| H8' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.580 | 0.007 | -0.090 |
| H9' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | -0.133 | 0.008 | -0.055 |
| H10' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 1.011 | 0.010 | 0.108 |
| H11' | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.515 | 0.003 | 0.086 |
| H12' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.091 | 0.009 | 0.048 |
| H13' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | 0.583 | 0.009 | 0.090 |
| H14' | 0.000 | 0.001 | 0.000 | 0.000 | 0.000 | -0.265 | 0.010 | -0.069 |

Table A2.23: Contributions at the N 3 atomic basin along the $\mathrm{N} 4-\mathrm{N} 3$ bond for the EE molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}$,
$\mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{s}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source
alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r})$. $\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\mathrm{SF}}$ | $\mathrm{R}_{\mathrm{FS}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ni 1 | 1.540 | 96.918 | 0.766 | 0.774 | -0.009 | 73.646 | 0.495 | 0.452 |
| S 2 | 0.017 | 1.076 | 0.008 | 0.009 | -0.001 | 6.915 | 0.110 | 0.205 |
| S 3 | 0.007 | 0.457 | 0.003 | 0.004 | -0.001 | 5.660 | 0.083 | 0.192 |
| C 4 | 0.002 | 0.095 | 0.001 | 0.001 | 0.000 | 0.054 | 0.049 | 0.041 |
| H 5 | 0.002 | 0.138 | 0.001 | 0.001 | 0.000 | 0.205 | 0.056 | 0.064 |
| C 6 | 0.001 | 0.059 | 0.000 | 0.001 | 0.000 | 2.024 | 0.042 | 0.136 |
| C 7 | 0.000 | -0.007 | 0.000 | 0.000 | 0.000 | -0.521 | -0.021 | -0.087 |
| C 8 | 0.000 | 0.030 | 0.000 | 0.001 | -0.001 | 5.024 | 0.034 | 0.184 |
| H 9 | 0.002 | 0.155 | 0.001 | 0.001 | 0.000 | 0.733 | 0.058 | 0.097 |
| C 10 | 0.000 | 0.014 | 0.000 | 0.000 | 0.000 | -2.840 | 0.026 | -0.153 |
| H 11 | 0.003 | 0.157 | 0.001 | 0.001 | 0.000 | 0.905 | 0.058 | 0.104 |
| C 12 | 0.001 | 0.053 | 0.000 | 0.001 | -0.001 | 6.268 | 0.040 | 0.199 |
| H 13 | 0.002 | 0.147 | 0.001 | 0.001 | 0.000 | 0.669 | 0.057 | 0.094 |
| C 14 | 0.001 | 0.080 | 0.001 | 0.001 | 0.000 | -0.988 | 0.046 | -0.107 |
| H 15 | 0.002 | 0.135 | 0.001 | 0.001 | 0.000 | 0.758 | 0.055 | 0.098 |
| C 16 | 0.001 | 0.076 | 0.000 | 0.001 | 0.000 | 2.857 | 0.046 | 0.153 |
| H 17 | 0.002 | 0.141 | 0.001 | 0.001 | 0.000 | 0.745 | 0.056 | 0.098 |
| N 18 | 0.002 | 0.138 | 0.001 | 0.001 | 0.000 | 0.223 | 0.056 | 0.065 |

Table A2.24: Contributions at the CD along the $\mathrm{Ni} 1-\mathrm{S} 2$ bond for the adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{s}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r})$. R $\mathrm{R}_{\mathrm{SF}}$

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SF}_{S}-\mathrm{SF}_{\text {Smag }} \%$ | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {SFS }}-$ SFSmag |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ni 1 | 1.525 | 95.923 | 0.750 | 0.774 | -0.024 | 209.952 | 0.493 | 0.640 |
| S2 | 0.019 | 1.174 | 0.010 | 0.009 | 0.001 | -6.526 | 0.114 | -0.201 |
| S3 | 0.008 | 0.529 | 0.004 | 0.004 | 0.000 | -4.189 | 0.087 | -0.174 |
| C4 | 0.002 | 0.098 | 0.001 | 0.001 | 0.000 | -0.376 | 0.050 | -0.078 |
| H5 | 0.002 | 0.138 | 0.001 | 0.001 | 0.000 | 0.187 | 0.056 | 0.062 |
| C6 | 0.001 | 0.062 | 0.000 | 0.001 | 0.000 | 1.632 | 0.043 | 0.127 |
| C7 | 0.000 | -0.007 | 0.000 | 0.000 | 0.000 | -0.547 | -0.021 | -0.088 |
| C8 | 0.001 | 0.063 | 0.000 | 0.001 | 0.000 | 0.564 | 0.043 | 0.089 |
| H9 | 0.003 | 0.159 | 0.001 | 0.001 | 0.000 | 0.183 | 0.058 | 0.061 |
| C10 | 0.001 | 0.034 | 0.001 | 0.000 | 0.001 | -5.589 | 0.035 | -0.191 |
| H11 | 0.003 | 0.158 | 0.001 | 0.001 | 0.000 | 0.822 | 0.058 | 0.101 |
| C12 | 0.001 | 0.083 | 0.001 | 0.001 | 0.000 | 2.159 | 0.047 | 0.139 |
| H13 | 0.002 | 0.151 | 0.001 | 0.001 | 0.000 | 0.009 | 0.057 | 0.022 |
| C14 | 0.002 | 0.100 | 0.001 | 0.001 | 0.000 | -3.736 | 0.050 | -0.167 |
| H15 | 0.002 | 0.136 | 0.001 | 0.001 | 0.000 | 0.614 | 0.055 | 0.092 |
| C16 | 0.002 | 0.105 | 0.001 | 0.001 | 0.000 | -1.027 | 0.051 | -0.109 |
| H17 | 0.002 | 0.144 | 0.001 | 0.001 | 0.000 | 0.344 | 0.056 | 0.076 |
| N18 | 0.002 | 0.139 | 0.001 | 0.001 | 0.000 | 0.220 | 0.056 | 0.065 |

Table A2.25: Contributions at the CD along the $\mathrm{Ni} 1-\mathrm{S} 2$ bond for the adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex molecular system given by the relaxation $\mathrm{MO} ; \mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}}-\mathrm{SF}_{\mathrm{Smag}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $\mathrm{s}(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r})$ obtained by the relaxation (reaction) orbitals. $\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{SFs}-\mathrm{SFsmag}}\right)$ are the ray of the sphere that are proportional to the atomic contribution to $\rho(\mathbf{r})(\mathrm{s}(\mathbf{r}))$ evaluated as

$$
\begin{gathered}
\mathrm{R}_{\mathrm{SF}}=0.5 *(\mathrm{SF} \% / 100)^{1 / 3} \\
\mathrm{R}_{\mathrm{SFs}-\mathrm{SFsmag}}=0.5 *\left(\mathrm{SF}_{\mathrm{S}}-\mathrm{SF}_{\mathrm{Smag}} \% / 100\right)^{1 / 3}
\end{gathered}
$$

All the reported quantity are reported in a.u.

| $\Omega$ | LSs | SF $_{\text {Smag }} \%$ |
| :---: | :---: | :---: |
| Ni1 | 0.016 | -136.307 |
| S2 | -0.002 | 13.440 |
| S3 | -0.001 | 9.849 |
| C4 | 0.000 | 0.430 |
| H5 | 0.000 | 0.018 |
| C6 | 0.000 | 0.392 |
| C7 | 0.000 | 0.025 |
| C8 | -0.001 | 4.460 |
| H9 | 0.000 | 0.550 |
| C10 | 0.000 | 2.749 |
| H11 | 0.000 | 0.083 |
| C12 | 0.000 | 4.109 |
| H13 | 0.000 | 0.660 |
| C14 | 0.000 | 2.749 |
| H15 | 0.000 | 0.144 |
| C16 | 0.000 | 3.884 |
| H17 | 0.000 | 0.400 |
| N18 | 0.000 | 0.003 |

Table A2.26: Contributions at the CD along the $\mathrm{Ni} 1-\mathrm{S} 2$ bond for the adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex molecular system given by the $\mathrm{SOMO} ; \mathrm{LS}_{\mathrm{S}}$ and $\mathrm{SF}_{\text {Smag }} \%$ are respectively the Local source and the Source Function atomic percentage for $s(\mathbf{r}) R_{\text {Fssmag }}$ are the ray of the sphere that are proportional to the atomic contribution to $s(\mathbf{r})$ evaluated as

$$
\mathrm{R}_{\text {SFs }- \text { SFsmag }}=0.5 *\left(\mathrm{SF}_{\mathrm{S}}-\mathrm{SF}_{\text {Smag }} \% / 100\right)^{1 / 3}
$$

All the reported quantity are reported in a.u.

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SFs} \%$ | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {FSs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ni1 | 0,014 | 8,758 | 0,009 | 0,006 | 0,003 | 163,547 | 0,222 | 0,589 |
| S2 | 0,125 | 76,334 | 0,063 | 0,062 | 0,001 | 36,953 | 0,457 | 0,359 |
| S3 | 0,004 | 2,535 | 0,002 | 0,002 | $-0,001$ | $-27,874$ | 0,147 | $-0,327$ |
| C4 | 0,006 | 3,625 | 0,003 | 0,003 | 0,000 | $-2,079$ | 0,165 | $-0,137$ |
| H5 | 0,003 | 1,968 | 0,002 | 0,002 | 0,000 | $-1,639$ | 0,135 | $-0,127$ |
| C6 | 0,001 | 0,875 | 0,001 | 0,001 | 0,000 | $-13,711$ | 0,103 | $-0,258$ |
| C7 | 0,000 | $-0,050$ | 0,000 | 0,000 | 0,000 | 3,535 | $-0,040$ | 0,164 |
| C8 | 0,000 | $-0,118$ | 0,000 | 0,000 | 0,000 | $-20,031$ | $-0,053$ | $-0,293$ |
| H9 | 0,001 | 0,819 | 0,001 | 0,001 | 0,000 | $-4,094$ | 0,101 | $-0,172$ |
| C10 | $-0,001$ | $-0,623$ | 0,000 | $-0,001$ | 0,000 | 15,227 | $-0,092$ | 0,267 |
| H11 | 0,001 | 0,715 | 0,001 | 0,001 | 0,000 | $-5,450$ | 0,096 | $-0,190$ |
| C12 | 0,000 | 0,133 | 0,000 | 0,000 | 0,000 | $-26,442$ | 0,055 | $-0,321$ |
| H13 | 0,001 | 0,833 | 0,001 | 0,001 | 0,000 | $-3,703$ | 0,101 | $-0,167$ |
| C14 | 0,001 | 0,524 | 0,000 | 0,000 | 0,000 | 5,287 | 0,087 | 0,188 |
| H15 | 0,001 | 0,779 | 0,001 | 0,001 | 0,000 | $-3,826$ | 0,099 | $-0,168$ |
| C16 | 0,001 | 0,521 | 0,000 | 0,001 | 0,000 | $-10,535$ | 0,087 | $-0,236$ |
| H17 | 0,001 | 0,798 | 0,001 | 0,001 | 0,000 | $-3,776$ | 0,100 | $-0,168$ |
| N18 | 0,002 | 1,488 | 0,001 | 0,001 | 0,000 | $-1,496$ | 0,123 | $-0,123$ |

Table A2.27: Contributions at the CC along the $\mathrm{Ni} 1-\mathrm{S} 2$ bond for the adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex molecular system; $\mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}} \%$ are respectively the Local source, the Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $s(\mathbf{r})$. R $\mathrm{R}_{\mathrm{SF}}$ $\left(\mathrm{R}_{\mathrm{FSs}}\right)$ are evaluated as in tab A2.1

| $\Omega$ | LS | $\mathrm{SF} \%$ | $\mathrm{LS}_{\alpha}$ | $\mathrm{LS}_{\beta}$ | LSs | $\mathrm{SF}_{\text {S }}-\mathrm{SF}_{\text {Smag }} \%$ | $\mathrm{R}_{\text {SF }}$ | $\mathrm{R}_{\text {SFS }}-$ SFSmag |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ni1 | 0,010 | 5,975 | 0,004 | 0,006 | $-0,002$ | $-88,888$ | 0,195 | $-0,481$ |
| S2 | 0,127 | 77,590 | 0,065 | 0,062 | 0,003 | 150,799 | 0,459 | 0,573 |
| S3 | 0,005 | 3,062 | 0,003 | 0,002 | 0,000 | 19,867 | 0,156 | 0,292 |
| C4 | 0,006 | 3,669 | 0,003 | 0,003 | 0,000 | 1,875 | 0,166 | 0,133 |
| H5 | 0,003 | 1,970 | 0,002 | 0,002 | 0,000 | $-1,496$ | 0,135 | $-0,123$ |
| C6 | 0,001 | 0,902 | 0,001 | 0,001 | 0,000 | $-11,262$ | 0,104 | $-0,241$ |
| C7 | 0,000 | $-0,048$ | 0,000 | 0,000 | 0,000 | 3,708 | $-0,039$ | 0,167 |
| C8 | 0,000 | 0,077 | 0,000 | 0,000 | 0,000 | $-2,414$ | 0,046 | $-0,144$ |
| H9 | 0,001 | 0,854 | 0,001 | 0,001 | 0,000 | $-1,007$ | 0,102 | $-0,108$ |
| C10 | $-0,001$ | $-0,480$ | 0,000 | $-0,001$ | 0,001 | 28,154 | $-0,084$ | 0,328 |
| H11 | 0,001 | 0,721 | 0,001 | 0,001 | 0,000 | $-4,938$ | 0,097 | $-0,183$ |
| C12 | 0,001 | 0,312 | 0,000 | 0,000 | 0,000 | $-10,164$ | 0,073 | $-0,233$ |
| H13 | 0,001 | 0,874 | 0,001 | 0,001 | 0,000 | $-0,040$ | 0,103 | $-0,037$ |
| C14 | 0,001 | 0,653 | 0,001 | 0,000 | 0,000 | 17,005 | 0,093 | 0,277 |
| H15 | 0,001 | 0,787 | 0,001 | 0,001 | 0,000 | $-3,093$ | 0,099 | $-0,157$ |
| C16 | 0,001 | 0,690 | 0,001 | 0,001 | 0,000 | 4,782 | 0,095 | 0,181 |
| H17 | 0,001 | 0,821 | 0,001 | 0,001 | 0,000 | $-1,738$ | 0,101 | $-0,130$ |
| N18 | 0,002 | 1,488 | 0,001 | 0,001 | 0,000 | $-1,479$ | 0,123 | $-0,123$ |

Table A2.28: Contributions at the CC along the $\mathrm{Ni} 1-\mathrm{S} 2$ bond for the adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex molecular
system given by the relaxation $\mathrm{MO} ; \mathrm{LS}, \mathrm{SF} \%, \mathrm{LS}_{\alpha}, \mathrm{LS}_{\beta}, \mathrm{LS}_{\mathrm{S}}, \mathrm{SF}_{\mathrm{S}}-\mathrm{SF}_{\text {Smag }} \%$ are respectively the Local source, the
Source Function atomic percentage for $\rho(\mathbf{r})$, the Local source alfa and beta, the Local Source for $s(\mathbf{r})$ and the Source Function atomic percentage for $\mathrm{s}(\mathbf{r})$ obtained by the relaxation (reaction) orbitals. $\mathrm{R}_{\mathrm{SF}}\left(\mathrm{R}_{\mathrm{SFs}-\mathrm{SFsmag}}\right.$ ) are the ray of the sphere that are proportional to the atomic contribution to $\rho(\mathbf{r})(\mathrm{s}(\mathbf{r}))$ evaluated as in Tab A2.25.

| $\Omega$ | Ls | $\mathrm{SF}_{\text {Smag }} \%$ |
| :---: | :---: | :---: |
| Ni 1 | 0,005 | 252,435 |
| S2 | $-0,002$ | $-113,847$ |
| S3 | $-0,001$ | $-47,741$ |
| C4 | 0,000 | $-3,954$ |
| H5 | 0,000 | $-0,143$ |
| C6 | 0,000 | $-2,449$ |
| C7 | 0,000 | $-0,174$ |
| C8 | 0,000 | $-17,617$ |
| H9 | 0,000 | $-3,087$ |
| C 10 | 0,000 | $-12,927$ |
| H11 | 0,000 | $-0,512$ |
| C 12 | 0,000 | $-16,278$ |
| H13 | 0,000 | $-3,663$ |
| C 14 | 0,000 | $-11,718$ |
| H 15 | 0,000 | $-0,733$ |
| C 16 | 0,000 | $-15,317$ |
| H17 | 0,000 | $-2,038$ |
| N18 | 0,000 | $-0,017$ |

Table A2.29: Contributions at the CC along the $\mathrm{Ni} 1-\mathrm{S} 2$ bond for the adt CpNi (dithiolene) ${ }^{\bullet}$ radical complex molecular system given by the $\mathrm{SOMO} ; \mathrm{LS}_{\mathrm{S}}$ and $\mathrm{SF}_{\text {Smag }} \%$ are respectively the Local source and the Source Function atomic percentage for $s(\mathbf{r}) \mathrm{R}_{\mathrm{FSsmag}}$ are the ray of the sphere that are proportional to the atomic contribution to $\mathrm{s}(\mathbf{r})$ evaluated as in Tab. A2.26


[^0]:    ${ }^{1}$ to obtain a charge density-quality set of structure factors from an X-ray diffraction experiment an accurate and highresolution experiment is required, possibly performed at low T . The interested reader is addressed to [8].

[^1]:    ${ }^{2}$ the rank is the number of non zero ED curvatures (eigenvalues of the Hessian matrix) at CP .
    ${ }^{3}$ in very few cases the $\rho(\mathbf{r})$ maxima (and associated zero-flux basins) were found in points where no nuclei are present. In such cases the $(3,-3) \mathrm{CP}$ are called non-nuclear attractors.

[^2]:    ${ }^{4}$ First row: IAM results from shelx, ${ }^{[21]}$ with the thermal motion of H atoms treated as isotropic and $(\sin \vartheta / \lambda)_{\mathrm{MAX}}=0.65$ $\AA^{-1}$. Second row: multipole model $\left(\mathrm{XD} 2006{ }^{[31]}\right)$ on experimental $\left(F_{\text {exp }}\right)$ structure factor amplitudes up to $\sin \vartheta / \lambda=0.9 \AA^{-}$ 1.
    ${ }^{5}$ Values in bohr ${ }^{-1}$. Where not reported, least-squares estimated standard deviations are smaller than the last digit.

[^3]:    ${ }^{1}$ Methanimidamide.
    ${ }^{2}$ 1-(methylsulfonyl)-methanimidamide.
    ${ }^{3}$ 3-amino-1,1-dioxo-4H-1 $\lambda^{6}, 2$-thiazete.
    ${ }^{4}$ Title compound.
    ${ }^{5}$ For TAYCUR, the unweighted average between the two symmetry-independent molecules is here reported.
    ${ }^{6}$ Unconjugated thiazetidine cycle.

[^4]:    ${ }^{1}$ Polymorph A, this work. The reported parameters derive from the final multipole model against experimental structure factors.
    ${ }^{2}$ Polymorph A, see ref. 19a. IAM model (shelx).
    ${ }^{3}$ Polymorph B, see ref. 19b. IAM model (shelx).
    ${ }^{4}$ The asymmetric unit of TAYCUR contains 2 independent molecules (molecule A on the left, molecule B on the right). See ref. 20. IAM model (shelx).

[^5]:    ${ }^{\text {a }}$ Atoms usually polarize in a direction counter to the electric field created by charge transfer (see Ref. 45 and Ref 15a).

[^6]:    ${ }^{\mathrm{b}}$ such as direct exchange, ligand-mediated exchange, superexchange, and so on

[^7]:    ${ }^{c}$ The results for ${ }^{3} \mathrm{~B}_{1} \mathrm{H}_{2} \mathrm{O}$ molecular system here presented are obtained performing quantum mechanical simulations in vacuo by means of the Gaussian09 program package, in particular we have optimized the structure at UHF level of theory using $6-311++G(2 p, 2 d)$ as basis set, detailed description of further QM calculations will be described in the next subsections.

[^8]:    ${ }^{d}$ we remind to the reader that the geometric part of the Green function is the distance between the points $\mathbf{r}$ and $\mathbf{r}{ }^{\prime}\left|r-\mathbf{r}^{\prime}\right|$

[^9]:    ${ }^{e}$ as a reaction to the alpha spin density in the $p_{x}$ orbital
    ${ }^{\mathrm{f}}$ or changing its value from positive to negative with respect to the contribution due to the remaining atoms
    $\mathrm{g}^{\mathrm{g}}$ values as low as $10^{-3}$ or $10^{-4}$ a.u. are typical

[^10]:    ${ }^{\mathrm{h}}$ the application of the topological descriptor $\mathrm{SF}_{\mathrm{s}}$ to this class of complexes will be better described in next sub-sections of this chapter

[^11]:    ${ }^{i}$ in particular we paid particular attention on the problem of spin contamination and static and dynamic electron correlation
    ${ }^{\mathrm{j}}$ pop $=$ no option in G09 program package

[^12]:    ${ }^{k}$ pop=noab option G09 program package; For CASSCF method, G09 apparently doesn't calculate and save spin density information. To this aim the $\operatorname{IOP}(5 / 72=1)$ option is mandatory, furthermore at the bottom of input file before the name selected for the .wfn file a " 11 " string needs ro be introduced. Finally, SlaterDet option should be used in this case in the CASSCF calculation. In this way is possible to recover a correct $\alpha$-density through the pop=noa option (but not the correct spin density through pop=noab, nor the correct $\beta$-density through pop=nob). From the total density and the $\alpha$-density the electron spin density and electron spin density Laplacian is obtained by difference: $s(\mathbf{r})=2 \rho_{a}(\mathbf{r})-\rho(\mathbf{r})$; $\nabla^{2} s(\mathbf{r})=2 \nabla^{2} \rho_{\alpha}(\mathbf{r})-\nabla^{2} \rho(\mathbf{r})$.

[^13]:    ${ }^{1}$ In case of theUHF/6-311++G(2d,2p) level of theory we refer to the spin-contamination annihilated wavefunction

[^14]:    ${ }^{m}$ i.e. the reciprocal of the distance $\left(\left|\mathbf{r}-\mathbf{r}^{\prime}\right|\right)^{-1}$ in eq. 5

[^15]:    ${ }^{\mathrm{n}}$ In particular UHF contamination spin annihilated level of theory provides a contribution three times larger with respect to $\operatorname{CASSCF}(8,8)$ computational model while ROHF gives a contribution to $\mathrm{s}(\mathbf{r})$ about five times larger than for the $\operatorname{CASSCF}\left(8,8^{\prime}\right)$ level of theory.

[^16]:    ${ }^{\circ}$ Due to the increased distance from the bcp, in this case the influence of the magnetic orbitals is clearly lower with respect to the bonded hydrogen.
    ${ }^{\mathrm{p}}$ This reference point correspond to the oxygen atomic basin's lone pair.

[^17]:    ${ }^{\mathrm{q}}$ It is worth to stress that $\mathrm{SF}_{\mathrm{S} \text { mag }} \equiv \mathrm{SF}_{\mathrm{S}}$ for ROHF level of theory

[^18]:    ${ }^{r}$ In terms of both their local properties at the critical points of $\rho(\mathbf{r})$ or $\nabla^{2} \rho(\mathbf{r})$ and of their SF and $\mathrm{SF}_{\mathrm{S}}$ contributions

[^19]:    ${ }^{\mathrm{s}} \mathrm{SF}\left(\mathbf{r}_{\mathrm{b}} ; \mathrm{ext}\right) \equiv \sum$ of SF contributions to $\rho(\mathbf{r})_{\mathrm{b}}$ from groups external to the $\mathrm{CH}_{3}$ group

[^20]:    ${ }^{\mathrm{t}} \mathrm{s}(\mathbf{r})$ to the bcp is almost two order of magnitude lower with respect $(3,-1)$ saddle critical point of $-\nabla^{2} \rho(\mathbf{r})$

[^21]:    ${ }^{\text {u }}$ In particular the H13 SF contribution to electron density is almost 14 times greater than the one from H12; on the contrary the $\mathrm{SF}_{\mathrm{S}}$ contribution from H 13 to $\mathrm{s}(\mathbf{r})$ is only three times as large as that from H 12 atom.

[^22]:    ${ }^{\mathrm{v}}$ This (3,-1) critical point and the almost symmetric one lying below such plane, but of $(3,+1)$ signature, may be both associated to non-bonded charge concentrations (NBCCs) and are largely due to the unpaired electron, although they do not correspond to electron spin density maxima.

[^23]:    ${ }^{w}$ only for large bridging angles $\mathrm{Cu}-\mathrm{N}-\mathrm{Cu}>108$ degree it turns to antiferromagnetic coupling

[^24]:    ${ }^{x}$ except the phase, in practice orbital related densities.

[^25]:    ${ }^{\mathrm{y}}$ in super-exchange terms: the positive spin density is induced close to the N 1 atom, but not in the bonding region because the $\mathrm{Cu}-\mathrm{N} 1_{\text {bridge }}$ is a dative bond

[^26]:    ${ }^{z}$ the $\pi^{*}$ involvement of the central N atom is clear from its spin density, while the $\pi_{\text {gerade }}$ has no contribution on this atom.

[^27]:    ${ }^{\text {aa }}$ This observation refers to the percentage, not to the absolute values, as there is a difference of two order of magnitude between the spin density values to be reconstructed

[^28]:    ${ }^{\text {a }}$ Estimated from the least-squares fitting of the orientation matrix against 8501 intense reflections with $6.0 \mathrm{deg}<2 \vartheta<114.7 \mathrm{deg}$.
    ${ }^{\mathrm{b}}$ Estimated from the least-squares fitting of the orientation matrix against 5044 intense reflections with $4.4 \mathrm{deg}<2 \vartheta<74.9 \mathrm{deg}$.
    ${ }^{\text {c }}$ Unweighted average of the two \#1 and \#2 individual unit cells.
    ${ }^{\mathrm{d}}$ First row: IAM results from shelx, with the thermal motion of H atoms treated as isotropic and $(\sin \vartheta / \lambda)_{\text {MAX }}=0.65 \AA^{-1}$. Second row: multipole model (XD2006) on experimental $\left(F_{\text {exp }}\right)$ structure factor amplitudes up to $\sin \vartheta / \lambda=0.9 \AA^{-1}$.
    ${ }^{\mathrm{e}}$ Values in bohr ${ }^{-1}$. Where not reported, least-squares estimated standard deviations are smaller than the last digit.

[^29]:    ${ }^{a}$ See Figure S4 in the Supporting Information for the packing scheme corresponding to this Table.
    ${ }^{\mathrm{b}} \mathrm{C}-\mathrm{H}$ distances have been fixed during the refinement to match neutron estimates (see text).
    ${ }^{c}$ Symmetry operation, with fractional translations, to localize the Donor D together with its attached hydrogen atom.
    All the acceptors A belong to the DTC asymmetric unit.
    ${ }^{\mathrm{d}}$ This is a $\mathrm{C}-\mathrm{H} \cdots \pi$ interaction between the C 14 methyl and the localized $\pi$-system of the $\mathrm{C} 10 \equiv \mathrm{~N} 3$ cyano group. Actually, a bcp is found in the experimental charge density distribution between H14C and C10. See Table S1 above.

