Article

Atomic-scale deformation mechanisms at high-pressure in inderborite, CaMg $[B_3O_3(OH)_5]_2(H_2O)_4·2H_2O$

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Abstract

The high-pressure behaviour of inderborite [ideally CaMg[B₃O₃(OH)₅]₂(H₂O)₄⋅2H₂O, space group C2/c with a ≈ 12.14 , $b \approx 7.43$, $c \approx 19.23$ Å and β $\approx 90.3^\circ$ at room conditions] has been studied by two *in situ* single-crystal synchrotron X-ray diffraction experiments up to ∼10 GPa, using He as pressure-transmitting fluid. Between 8.11(5) and 8.80(5) GPa, inderborite undergoes a first-order phase transition to its high-pressure polymorph, inderborite-II (with $a \approx 11.37$, $b \approx 6.96$, $c \approx 17.67$ Å, β $\approx 96.8^{\circ}$ and $\Delta V \approx 7.0\%$, space group unknown). The isothermal bulk modulus ($K_{V0} = \beta^{-1} p_{0,T0}$, where β $p_{0,T0}$ is the volume compressibility coefficient) of inderborite was found to be $K_{V0} = 41(1)$ GPa. The destructive nature of the phase transition prevented any structure resolution of inderborite-II or even the continuation of the experiments at pressures higher than 10.10(5) GPa. In the pressure range 0–8.11(5) GPa, the compressional anisotropy of inderborite, indicated by the ratio between the principal components of the Eulerian finite unit-strain ellipsoid, is $\varepsilon_1:\varepsilon_2:\varepsilon_3 = 1.4:1.05:1$. The deformation mechanisms at the atomic scale in inderborite are here described. Our findings support the hypothesis of a quasi-linear correlation between the total H₂O content and P-stability range in hydrated borates, as the pressure at which inderborite undergoes the phase transition falls in line with most of the hydrate borates studied at high-pressure so far.

Keywords: inderborite; high-pressure; single crystal X-ray diffraction; elastic compressibility; phase transition

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Introduction

Boron is a strategic element used in a variety of products, including ant poisons, detergents (for bleaching), borosilicate glasses (such as Pyrex®), and ceramics (Abe, [1952](#page-7-0); Woods, [1994;](#page-8-0) Klotz and Moss, [1996](#page-8-0); Yu et al., [2018;](#page-8-0) Chen et al., [2020](#page-7-0); U.S.G.S, [2022\)](#page-8-0). The strategic importance of boron, and the moderate supply risk due to its uneven distribution, has been recognised by the European Union, which has classified borates as critical raw material since 2014 (European Commission, [2014\)](#page-7-0). Economically viable boron mineral deposits are distributed irregularly worldwide and are mostly represented by five main hydrated borate minerals: ulexite, colemanite, borax, tincalconite and kernite (Kistler and Helvacı, [1994;](#page-8-0) Helvaci and Alonso, [2000;](#page-8-0) Zheng et al., [2005;](#page-8-0) García-Veigas and Helvacı, [2013\)](#page-7-0). Other borate minerals, such as inderborite, meyerhofferite, inyoite and tertschite, are often found in smaller weight fractions alongside these main minerals. Due to their low production cost, hydrated borates are believed to be good candidates as aggregates in neutron shielding concretes (Okuno, [2005](#page-8-0); Okuno et al., [2009;](#page-8-0) Glinicki et al., 2018), because of the 10 B isotope (which accounts

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for ∼20% of natural boron) high cross-section for thermal neutrons (∼3840 barns) (Carter et al., [1953](#page-7-0); Palmer and Swihart, [1996](#page-8-0)), leading to the reaction:

¹⁰B + n $\rightarrow \alpha +^7$ Li + γ .

Inderborite, ideally CaMg[B₃O₃(OH)₅]₂(H₂O)₄⋅2H₂O, space group C2/c with $a \approx 12.14$, $b \approx 7.43$, $c \approx 19.23$ Å and $\beta \approx 90.3^{\circ}$, was originally discovered at the Inder Lake borate deposit, western Kazakhstan, and later also at the Eskişehir district, Turkey (Kurkutova et al., [1965;](#page-8-0) Palmer and Helvaci, [1997](#page-8-0)). The lower occurrence of inderborite, with respect to other most common borates, is attributed to its extremely narrow stability field in the CaO–MgO–B₂O₃–H₂O system, as demonstrated by Birsoy and Özbaş ([2012](#page-7-0)). However, minor fractions of inderborite are commonly found associated with colemanite and ulexite in valuable ore deposits of hydrate borates (e.g. Kirka and Sarikaya deposits) (Palmer and Helvaci, [1997](#page-8-0); Helvacı and Palmer, [2017](#page-8-0)). For example, inderborite has been found in the ore debris near the Kuşkaya gallery of the Turkish Borax Mining Company, in the Sarikaya borate deposits, alongside other borate minerals such as colemanite, borax, ulexite, kurnakovite and inderite (Baysal, [1973\)](#page-7-0).

Kurkutova et al. [\(1965\)](#page-8-0) were the first to determine the crystal structure of inderborite [\(Fig. 1](#page-1-0)), although the complex hydrogen bond network was only described later by Burns and Hawthorne [\(1994](#page-7-0)). In a recent paper, based on a multimethodological approach, the crystal chemistry (with a focus on

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Figure 1. Inderborite structure, based on the model proposed by Gatta et al. ([2023\)](#page-8-0), viewed perpendicular to the (100) plane. Ca-polyhedrons in indigo, Mg-polyhedrons in orange, boron polyhedrons in green, hydrogen in small pale pink spheres. Drawn using VESTA software (Momma and Izumi, [2008\)](#page-8-0),

the B isotopic composition) and structure of inderborite (based on a single-crystal neutron diffraction experiment) were re-investigated by Gatta et al. [\(2023](#page-8-0)). They confirmed that the chemical composition of the inderborite from Inder, Kazakhstan is virtually identical to the ideal one. The fundamental building block (FBB) of inderborite is a $[B_3O_3(OH)_5]^{2-}$ ring, consisting of 2 $B\varphi_4$ tetrahedrons and one planar trigonal $B\varphi_3$ unit (φ represents an O^{2-} anion, an OH⁻ hydroxyl group or a H₂O molecule). The same < $\Delta 2$ | > unit (Δ stands for a B φ_3 unit, and \Box for a B φ_4 tetrahedron), in which all oxygen atoms that are not shared between two boron atoms are protonated (Burns and Hawthorne, [1994\)](#page-7-0), occurs also in kurnakovite, meyerhofferite, inyoite, inderite and solongoite, whereas in hydroboracite and colemanite it is polymerised into chains (Hawthorne, [2012\)](#page-8-0). In the crystal structure of inderborite, the $[B_3O_3(OH)_5]^{2-}$ rings are interconnected with the Ca-polyhedra and Mg-octahedra through the O1, O2, O3, O6 and O8 oxygen hinges. This results in the formation of continuous heteropolyhedral sheets parallel to (100) (Fig. 1), connected through a complex hydrogen bonding network involving O7 and O4 as acceptors, respectively from the O3 and O6 hydroxyl groups and from the O10 $H₂O$ molecule. A crucial role in providing

stability to the crystal structure is attributed to the interstitial ('zeolitic') H_2O molecule O11, which occupies a key position between the sheets (Fig. 1). O11 is connected, via hydrogen bonding, to O8 and O9: the former is an oxygen hinge that connects the Mg-octahedron with the B2-tetrahedron, whereas the latter is a $H₂O$ molecule belonging only to the Mg-octahedron. This further connects the crystal structure along the [010] crystallographic direction. O9 is also a *donor* to O10, the only H₂O molecule of the complex Ca polyhedrons, providing the only weak connection between Ca- and Mg-polyhedrons.

At the present time, inderborite remains an extremely poorly studied mineral. The only available Raman spectrum to date can be found on the <https://rruff.info/> website, and some important thermodynamic parameters (such as the thermal expansion coefficient and elastic compressibility) are still missing. As pointed out by Gatta et al. ([2023\)](#page-8-0), given the importance of the hydrogen bonding network in inderborite, a compressional, thermal, or chemical perturbation of the H-bonding scheme could easily lead to a phase transition. On this basis, in this study we aim to: (1) assess the stability range of inderborite with respect to pressure, including for potential industrial utilisation of this borate; and (2) describe the structural evolution of

inderborite, at the atomic scale, with increasing pressure. While inderborite is not likely to be used as primary component in radiation shielding concretes, its association with major hydrated borates (e.g. colemanite and borax) makes it imperative to investigate its stability under non-ambient conditions. Furthermore, its stability at high-pressure allows (3) comparisons to be drawn with other hydrated borate structures studied and to strengthen the hypothesis of a correlation between the total H_2O content and the stability range of hydrated borates under pressure.

Experimental procedures

The sample of inderborite used in this study comes from the type locality (Inder Deposit, Kazakhstan), and was provided by the late Dr. Renato Pagano. Crystals from the same sample were recently used for the experiments reported by Gatta et al. [\(2023\)](#page-8-0). Inderborite is a light (1.92 g/cm^3) and soft $(3.5 \text{ on the Mohs})$ scale) mineral with a prismatic habit. Two single crystals, each measuring ∼20×15×10 μm, were selected for high-pressure experiments at the ID15b beamline, ESRF, Grenoble, France. The diffraction experiment employed a convergent monochromatic beam ($E \approx 30$ keV, $\lambda \approx 0.41$ Å and ~ 200 mA). Helium was used as the pressure-transmitting fluid (Klotz et al., [2009\)](#page-8-0), and two ruby micro-spheres were added as pressure calibrants (pressure uncertainty \pm 0.05 GPa; Mao *et al.*, [1986](#page-8-0)). The crystals were loaded in two different membrane-driven DACs (diamond anvil cells), with 600 μm culet Boehler-Almax design anvils. For each DAC, a stainless-steel foil (with thickness of ∼250 μm) was pre-indented to ∼80 μm and then drilled by spark-erosion, leading to a P-chamber of ∼300 μm in diameter. The diffraction patterns were collected by an Eiger2X 9M detector, positioned ∼180 mm from the sample. The sample-to-detector distance was calibrated using a Si standard and a vanadinite (Pb₅(VO₄)₃Cl) single crystal. A pure ω-scan ($-32^{\circ} \le \omega \le +32^{\circ}$) was used to collect the diffraction patterns, with a 0.5° step width and a 0.5 s exposure time per step. Further details on the beamline setup can be found in Hanfland ([2016](#page-8-0)) and Poreba et al. ([2022](#page-8-0)).

Data analysis

The CrysAlisPro package (Rigaku Oxford Diffraction, [2019](#page-8-0)) was used to index the diffraction peaks and integrate their intensities; corrections for Lorentz-polarisation effects were also applied. The semi-empirical ABSPACK routine, implemented in CrysAlisPro, was used to account for X-ray absorption effects caused by the DAC components. Table 1 lists the unit-cell parameters at high pressure, and their evolution with P is shown in [Fig. 2.](#page-3-0) Selected diffraction patterns are also presented in [Fig. 3.](#page-4-0) The JANA2006 package (Petrícek et al., [2014](#page-8-0)) was used for all structure refinements, with the initial fractional coordinates taken from Burns and Hawthorne [\(1994\)](#page-7-0) and Gatta et al. ([2023](#page-8-0)). The CIFs (crystallographic information files) are deposited as supplementary materials (see below).

High-pressure data were collected up to 9.84(5) GPa, as the number and intensity of the observed reflections [*i.e.* with F_0^2 > $3\sigma(F_0^2)$] decreased significantly after the phase transition at 8.80(5) GPa (as [Fig. 3](#page-4-0) shows), effectively ending the experiment. In both the experiments, crystals did not recover after the phase transition. This was the most destructive phase transition observed in hydrated borates to date (compare Comboni et al., [2020b,](#page-7-0) [2022a](#page-7-0)), as the number of observed reflections was barely

Table 1. Evolution of the unit-cell parameters of inderborite with pressure obtained from the two independent experiments (*high-pressure polymorph).

P (GPa)	$a(\AA)$	$b(\AA)$	c (Å)	β (°)	$V(\AA^3)$
First dataset					
0.0001	12.1300(5)	7.4253(2)	19.1940(4)	90.324(6)	1728.80(7)
0.43(5)	12.0977(4)	7.4114(6)	19.1495(3)	90.332(3)	1716.9(2)
0.61(5)	12.0820(4)	7.4028(6)	19.1256(3)	90.351(3)	1710.6(2)
1.19(5)	12.0212(4)	7.3744(6)	19.0295(3)	90.382(3)	1686.9(4)
1.80(5)	11.9696(5)	7.3425(7)	18.9417(4)	90.418(4)	1664.7(2)
2.35(5)	11.9198(4)	7.3170(6)	18.8554(3)	90.444(3)	1644.5(4)
2.82(5)	11.8804(4)	7.2925(6)	18.7842(3)	90.457(3)	1627.4(4)
3.33(5)	11.8361(4)	7.2664(6)	18.6986(3)	90.483(3)	1608.1(4)
3.84(5)	11.8093(4)	7.2487(6)	18.6366(4)	90.534(3)	1595.3(2)
4.54(5)	11.7653(4)	7.2194(7)	18.5425(4)	90.566(3)	1574.9(2)
6.23(5)	11.6781(5)	7.1664(7)	18.3259(4)	90.629(4)	1533.6(2)
7.08(5)	11.6443(5)	7.1444(7)	18.2319(4)	90.638(3)	1516.7(2)
7.80(5)	11.6192(5)	7.1256(8)	18.1556(4)	90.629(3)	1503.1(2)
8.11(5)	11.5986(5)	7.1162(8)	18.1089(4)	90.623(3)	1494.6(2)
$8.80(5)$ *	11.37(1)	6.964(5)	17.672(12)	96.8(2)	1390(6)
$10.10(5)^*$	11.49(1)	6.99(2)	17.33(4)	95.7(2)	1385(6)
Second dataset					
0.0001	12.139(6)	7.4286(3)	19.1975(5)	90.352(6)	1731.2(8)
0.35(5)	12.110(5)	7.4128(2)	19.1484(5)	90.371(6)	1718.9(8)
0.86(5)	12.065(6)	7.3902(2)	19.0812(5)	90.402(6)	1701.3(8)
1.56(5)	12.008(5)	7.3589(2)	18.9832(5)	90.402(7)	1677.4(8)
2.32(5)	11.931(7)	7.3231(3)	18.8708(6)	90.425(8)	1648.7(10)
3.05(5)	11.875(6)	7.2868(3)	18.7546(6)	90.515(7)	1622.8(8)
3.81(5)	11.830(6)	7.2477(3)	18.6346(5)	90.516(7)	1597.7(8)
4.67(5)	11.802(6)	7.2110(3)	18.5194(6)	90.592(7)	1575.9(8)
5.30(5)	11.764(7)	7.1928(3)	18.4533(7)	90.636(9)	1561.4(9)
6.20(5)	11.719(6)	7.1655(3)	18.3571(6)	90.555(8)	1541.4(8)
6.90(5)	11.674(7)	7.1460(3)	18.2757(7)	90.603(9)	1524.5(10)
7.45(5)	11.654(7)	7.1305(3)	18.2115(6)	90.638(9)	1513.3(9)
$8.96(5)$ *	11.435(2)	6.932(8)	17.453(12)	96.05(8)	1375(2)

enough to properly index the diffraction pattern of the highpressure polymorph, inderborite-II, which was found to be metrically monoclinic. The space group has not been unambiguously determined.

Relevant interatomic distances, average bond lengths, angles, polyhedral volumes, distortion index [defined as $D = \frac{1}{n} \sum_{n=1}^{n}$ $i=1$ $\frac{|l_i-l_{av}|}{l_{av}},$ where l_i is the distance from the central atom to the i^{th} coordinating atom, and l_{av} is the average bond length; Baur, [1974](#page-7-0)], quadratic elongation [defined as $\langle \lambda \rangle = \frac{1}{n} \sum_{n=1}^{n}$ $\frac{i-1}{i}$ $\frac{l_i}{l_0}$ $\left(\frac{l_i}{l_0}\right)^2$, where l_0 is the center-to-vertex distance of a regular polyhedron of the same volume and l_i is the actual centre-to-vertex length; Robinson et al., [1971](#page-8-0)] and bond angle variance [defined as σ^2 = $\frac{1}{m-1}\sum_{i=1}^m$ $\sum_{i=1} (\phi_i - \phi_0)^2$ where *m* is the number of faces in the polyhedron×3/2, *i.e.* number of bond angles, ϕ_i is the *i*th bond angle, and ϕ_0 is the ideal bond angle for a regular polyhedron e.g. 90 \degree for an octahedron; Robinson et al., [1971](#page-8-0)] have been calculated using the tools implemented in the VESTA software (Momma and Izumi, [2008](#page-8-0)), and are listed in Supplementary Table S1. Relevant interatomic angles and distances are reported in [Table 2.](#page-5-0)

To describe the isothermal behaviour of inderborite, a second-order Birch–Murnaghan Equation of State (BM–EoS) was fitted to the P–V data (Birch, [1947\)](#page-7-0). This EoS allows refinement of the bulk modulus [K_{V0} or $K_{P0,T0}$, defined as $-V_0(\partial P/\partial T)$ $\partial V_{T0} = \beta^{-1} p_{0,T0}$, where $\beta_{P0,T0}$ is the volume compressibility coefficient at room conditions] and its P-derivatives $[K'=\partial K_{P0,T0}/\partial P]$

Figure 2. Evolution with pressure of the unit-cell parameters of inderborite: first dataset in black squares, second dataset in red diamonds, inderborite-II in green circles. Estimated standard deviations are smaller than symbols.

Figure 3. Reconstruction, based on the experimental data, of the 0kl*, hk0* and h0l* reciprocal lattice planes of inderborite- (left side) and inderborite-II (right side). Above the phase transition, the number of observed reflections dropped dramatically.

and $K^{"}=\partial^{2}K_{P0,T0}/\partial P^{2}$. When truncated to the second order in energy, *i.e.* with $K' = \partial K_{P0, T0}/\partial P = 4$, the EoS transforms to:

$$
P(fe) = 3K_{P0,T0}fe(1+2fe)^{5/2},
$$

where fe [defined as $fe = \left[\left(\frac{V_0}{V}\right)^{\frac{2}{3}} - 1\right]/2$] is the Eulerian finite strain. The truncation to the second order in energy is reasonable when the experimental data plot following a horizontal trend in the diagram with Eulerian strain vs. 'normalised pressure' [F, defined as $F = P/[3fe(1 + 2fe)^{5/2}]$]. The BM-EoS parameters (listed in [Table 3](#page-5-0)) were refined by minimising the differences between the EoS curves and the experimental data, which were weighted by their uncertainties in P and V. The fitting was carried out using the EOS-FIT7-GUI software (Angel et al., [2014](#page-7-0); Gonzalez-Platas et al., [2016](#page-8-0)). An estimated uncertainty of ± 0.05 GPa was considered for pressure (Mao et al., [1986](#page-8-0)) during the data fitting. The fe vs F plot is shown in Supplementary Fig. S1.

Results

Elastic behaviour

The linear elastic parameters, listed in [Table 3](#page-5-0), suggest that inderborite is a rather isotropic mineral, which deforms almost equally

Table 2. Evolution, with pressure, of some relevant interatomic angles (in °) and distances (d in Å) in inderborite structure [Δ defined as the difference between the value at 0.0001 GPa and that at 8.11 GPa].

P (GPa) Interatomic angles	$O2 - O3 - O6$	$O1 - O6 - O4$	$O6 - O1 - O8$	0801109	060703	0501004
0.0001	89.8(1)	165.7(1)	125.6(1)	132.2(2)	67.3(3)	121.2(4)
0.43(5)	89.3(1)	166.6(2)	125.0(1)	132.6(2)	67.3(1)	121.1(2)
0.61(5)	88.8(1)	166.8(2)	124.8(1)	132.2(3)	67.4(1)	121.1(2)
1.19(5)	88.3(1)	167.0(2)	124.7(1)	132.1(2)	67.5(1)	121.2(2)
1.80(5)	87.7(1)	167.4(2)	124.4(1)	131.6(3)	67.4(1)	121.2(2)
2.35(5)	86.9(1)	167.9(2)	124.2(1)	131.1(3)	67.9(1)	120.9(2)
2.82(5)	86.7(1)	168.2(2)	123.8(1)	131.1(3)	67.8(1)	121.2(2)
3.33(5)	86.0(1)	168.6(2)	123.5(1)	130.4(3)	68.1(1)	121.1(2)
3.84(5)	85.5(1)	169.0(2)	122.9(1)	130.3(3)	68.2(1)	121.1(2)
4.54(5)	85.0(1)	169.5(2)	122.4(1)	129.6(3)	68.2(1)	121.0(2)
6.23(5)	83.5(2)	170.7(2)	120.6(2)	128.0(3)	68.5(2)	121.0(3)
7.08(5)	82.7(2)	171.4(3)	120.2(2)	127.3(3)	68.6(2)	120.9(3)
7.80(5)	82.2(2)	172.0(3)	119.1(2)	126.8(3)	69.0(2)	120.9(3)
8.11(5)	82.0(2)	172.3(3)	118.6(2)	126.7(3)	69.2(2)	121.2(3)
Δ total	$-7.8(3)$	$-6.6(4)$	7.0(3)	5.5(5)	$-1.9(5)$	0.0(7)
P (GPa)						
Distances	0607	0307	05010	01004	08011	01109
0.0001	2.62(2)	2.867(9)	2.733(8)	2.79(2)	2.92(2)	3.10(2)
0.43(5)	2.639(4)	2.861(5)	2.723(6)	2.787(4)	2.898(5)	3.076(6)
0.61(5)	2.633(4)	2.859(5)	2.723(6)	2.779(4)	2.888(5)	3.083(6)
1.19(5)	2.611(4)	2.840(5)	2.713(6)	2.756(4)	2.862(5)	3.052(6)
1.80(5)	2.592(4)	2.820(5)	2.699(6)	2.732(4)	2.842(5)	3.034(6)
2.35(5)	2.576(4)	2.806(5)	2.692(6)	2.713(4)	2.824(5)	3.010(6)
2.82(5)	2.564(4)	2.789(5)	2.685(6)	2.697(4)	2.806(5)	2.982(6)
3.33(5)	2.550(4)	2.771(6)	2.669(6)	2.682(4)	2.797(5)	2.947(6)
3.84(5)	2.543(4)	2.773(6)	2.666(7)	2.671(4)	2.781(5)	2.926(7)
4.54(5)	2.529(4)	2.757(6)	2.658(6)	2.653(4)	2.770(5)	2.898(6)
6.23(5)	2.506(6)	2.719(7)	2.649(7)	2.613(6)	2.722(6)	2.873(7)
7.08(5)	2.501(6)	2.699(7)	2.646(8)	2.594(6)	2.712(6)	2.866(7)
7.80(5)	2.493(6)	2.677(7)	2.649(8)	2.579(6)	2.694(6)	2.866(7)
8.11(5)	2.487(6)	2.674(7)	2.638(8)	2.574(6)	2.684(6)	2.856(7)
Δ total	0.13(3)	0.19(2)	0.10(2)	0.22(3)	0.24(3)	0.24(3)

along the principal crystallographic directions. However, as expected in monoclinic crystals, the unit-cell angle β is free to vary with pressure, meaning that the linear bulk moduli along the principal crystallographic directions (listed in Table 3) do not actually describe the compressional anisotropy. To overcome this problem, the Eulerian finite strain analysis was performed with the Win_Strain software (Angel, [2011\)](#page-7-0). The geometrical relationships between the unit-strain ellipsoid and the crystallographic axes of inderborite can be described by the following matrix (with $\varepsilon_1 > \varepsilon_2 > \varepsilon_3$):

$$
\begin{pmatrix}\n\varepsilon_1 \\
\varepsilon_2 \\
\varepsilon_3\n\end{pmatrix}\n\angle \begin{pmatrix}\n79.8^\circ & 90^\circ & 10.8^\circ \\
169.8^\circ & 90^\circ & 79.2^\circ \\
90.0^\circ & 180^\circ & 90.0^\circ\n\end{pmatrix}\n\cdot\n\begin{pmatrix}\na \\
b \\
c\n\end{pmatrix}
$$

Table 3. Refined elastic parameters of the inderborite unit-cell and of the coordination polyhedrons, based on the isothermal II-BM Equation of State fit (*fixed parameter).

	V_0, x_0 (Å ³ , Å)	$K_{V0, x0}$ (GPa)	K'	$βV0, x0$ (GPa ⁻¹)
V	1731(1)	41(1)	4*	0.0244(6)
a	12.129(2)	44.6(6)	4*	0.0075(3)
b	7.4255(6)	47.5(4)	4*	0.0070(2)
C	19.195(2)	34.6(4)	4*	0.0096(3)
$Ca-\phi_8$	26.1(7)	53(4)	4*	0.019(1)
$Mg-\varphi_6$	12.27(5)	81(8)	4^*	0.012(1)
$B1-\varphi_4$	1.628(3)	260(30)	4*	0.0038(5)
$B2-\varphi_4$	1.643(3)	170(12)	4^*	0.0059(4)

for inderborite, between 0.0001 and 8.11(5) GPa, $\varepsilon_1:\varepsilon_2:\varepsilon_3 =$ 1.4:1.05:1 $[\epsilon_1 = 0.00723(5) \text{ GPa}^{-1}; \epsilon_2 = 0.00546(3) \text{ GPa}^{-1};$ and $\varepsilon_3 = 0.00524(4)$ GPa⁻¹]. The inderborite response to compression is only moderately anisotropic, with the major direction (ϵ_1) of compression describing an angle of only 10° with the c axis. This finding is surprising if compared to other hydrous borates, such as meyerhofferite $(\epsilon_1:\epsilon_2:\epsilon_3 =$ 5.8:4.7:1) or invoite $(\epsilon_1:\epsilon_2:\epsilon_3=3.5:2.1:1)$ (Comboni et al., [2020a,](#page-7-0) [2022a\)](#page-7-0). Regarding the high-pressure polymorph, the poor quality of the diffraction data did not allow any robust calculation, as discussed above. However, the previous matrix, showing the unit-strain ellipsoid calculated between 0.0001 and 8.11(5) GPa, does not describe the P-induced evolution of the strain ellipsoid itself, which undergoes a significant change as pressure increases. Initially, between 0.0001 and 2.35(5) GPa, the unit-strain ellipsoid is described by the following matrix:

$$
\begin{pmatrix}\n\varepsilon_1 \\
\varepsilon_2 \\
\varepsilon_3\n\end{pmatrix}\n\angle \begin{pmatrix}\n49.6^\circ & 90^\circ & 40.9^\circ \\
40.4^\circ & 90^\circ & 130.9^\circ \\
90.0^\circ & 0^\circ & 90.0^\circ\n\end{pmatrix}\n\cdot\n\begin{pmatrix}\na \\
b \\
c\n\end{pmatrix}
$$

with $\varepsilon_1 \cdot \varepsilon_2 \cdot \varepsilon_3 = 1.3$:1.1:1 [$\varepsilon_1 = 0.0079(2) \text{ GPa}^{-1}$; $\varepsilon_2 = 0.0070(2) \text{ GPa}^{-1}$; and $\varepsilon_3 = 0.0062(1) \text{ GPa}^{-1}$]. Therefore, in the initial stage of compression, ε_1 and ε_2 lie on the *ac* plane, whereas ε_3 is parallel to *b*. However, as pressure increases, ε_1 , ε_2 and ε_3 deviate from the original orientation and, between 6.23(5) and 8.11(5) GPa, the unit-strain ellipsoid matrix changes to:

$$
\begin{pmatrix}\n\varepsilon_1 \\
\varepsilon_2 \\
\varepsilon_3\n\end{pmatrix}\n\angle \begin{pmatrix}\n90.9^\circ & 90^\circ & 0.3^\circ \\
90.0^\circ & 180^\circ & 90.0^\circ \\
0.9^\circ & 90^\circ & 89.7^\circ\n\end{pmatrix}\n\cdot\n\begin{pmatrix}\na \\
b \\
c\n\end{pmatrix}
$$

with $\varepsilon_1:\varepsilon_2:\varepsilon_3 = 1.7:1:1$ $[\varepsilon_1 = 0.0063(2) \text{ GPa}^{-1}; \varepsilon_2 = 0.0037(6) \text{ GPa}^{-1};$ $\varepsilon_3 = 0.0036(5) \text{ GPa}^{-1}$. Close to the phase transition, magnitude and orientation of the unit-strain ellipsoid differ from the earlier stages of compression, with ε_1 being almost parallel to c, ε_3 almost parallel to a, and ε_2 parallel to b.

Structure evolution

Referring to the first dataset [\(Table 1\)](#page-2-0), between ambient pressure and 8.11(5) GPa, the length of the unit-cell edges of inderborite decreases steadily by ∼4.3% for the a and b unit-cell edges and by ∼3.3% along the c edge. The unit-cell volume decreases monotonically by ∼13.5% and the β angle steadily increases by ∼3.3% (see [Table 1\)](#page-2-0). Similar values (i.e. within 3σ) were observed for the second dataset. Up to 8.11(5) GPa, the crystal structure of inderborite deforms steadily with no significant changes. Between 8.11(5) and 8.80(5) GPa, inderborite undergoes a phase transition to its high-pressure polymorph, inderborite-II. This phase transition is rather disruptive, and data were collected only up to 10.10(5) GPa, as the number and intensity of the observed reflections [*i.e.* with $F_0^2 > 3\sigma(F_0^2)$] decreased significantly after the phase transition (down to ∼60). The phase transition is marked by a sharp volume decrease, typical of first-order phase transformations. Upon decompression, the crystal structure of inderborite does not revert to its ambient pressure polymorph, indicating that the transition is irreversible (at least for the time scale of our experiment).

Discussion

The high-quality structural refinements of inderborite with pressure allowed a full description of the main deformation mechanisms able to accommodate the effect of compression. The bulk modulus (K_{V0}) of the B φ_4 tetrahedra, based on the isothermal Birch–Murnaghan Equation of State fit ([Table 3\)](#page-5-0), is more than five times higher than that of the inderborite unit cell. This suggests that the boron tetrahedrons act as uncompressible units, as expected at low–mid pressures [\(Table 3](#page-5-0) and Supplementary Table S1). The same behaviour has been observed in all the hydrated borates studied so far at high pressure (e.g. ulexite, jadarite and kernite; Comboni et al., [2020b](#page-7-0), [2021a](#page-7-0), [2022b\)](#page-7-0) and in other minerals as well (e.g. reedmergnerite, londonite and barium metaborates, Gatta et al., [2011](#page-8-0); Bekker et al., [2022;](#page-7-0) Gorelova et al., [2022\)](#page-8-0). On the other hand, the Mg φ_6 octahedra and Ca φ_8 polyhedrons are significantly softer but with an important difference. The Ca-polyhedron compresses as expected, similar to observations in other hydrous borate crystal structures, such as meyerhofferite and inyoite, as evidenced by its bulk modulus (53(4) GPa) that is within 1σ of the values observed in meyerhofferite and inyoite (Comboni et al., [2020a](#page-7-0), [2022a](#page-7-0)). In contrast, the Mg-polyhedron is significantly stiffer with respect to Mg-polyhedra in other structures: the calculated bulk modulus in this study (81(8) GPa) is 11% higher than that of the same polyhedron in kurnakovite and ∼20% higher than that in inderite (67(4) GPa) (Pagliaro *et al.*, [2021;](#page-8-0)

Comboni et al., [2023\)](#page-7-0). Although considerably stiff, the Mg– φ_6 polyhedron compression is highly anisotropic. In the experimental pressure range of this study, while the Mg–O9 and the Mg–O2 distances decrease by ∼1.8 and 1.5%, Mg–O8 decreases by ∼4%. This anisotropic compression, mainly affecting the Mg–O8 bond, leads to a progressive distortion of the Mg– φ_6 octahedron, as indicated by the progressive increase of the distortion index (σ^2) values (Supplementary Table S1). Overall, when compared to the bulk modulus of inderborite, all the polyhedrons are stiffer than the overall structure (see [Table 3](#page-5-0)), meaning that the structural deformation in response to the applied pressure must be accommodated by other mechanisms. Indeed, tilting around the oxygen hinges between the B-, Ca- and Mg- polyhedrons can be deduced from the data in [Table 2,](#page-5-0) which reports O–O–O angles that change significantly with pressure. In detail, the $O2-\overline{O3}-O6$, $O1-\overline{O6}-O4$ and $O6-\widehat{O1}-O8$ angles, which describe the degree of tilting between the $[B_3O_3(OH)_5]^2$ ⁻⁻ polyion and the Ca- φ_8 octahedron, show a steady and progressive deformation as pressure increases $[O2-\widehat{O3}-O6]$ and progressive deformation as pressure increases $[O2-\widehat{O3}-O6,$ O1–O6 –O4 decrease by ∼7.8(2)° and 6.6(2)°, whereas O6–O1 –O8 increases by ∼7.0(2)°]. The compression of the hydrogen-bonding network also accommodates part of the pressure-induced deformation and the interstitial ('zeolitic') $H₂O$ molecule O11 might play a role in the destabilisation of the crystal structure. This molecule is connected, via hydrogen bonding, with the O8 hydroxyl group and the O9 $H₂O$ molecules ([Fig. 1](#page-1-0), Supplementary Fig. S2). At ambient pressure, the interatomic angle $O8\cdots O11\cdots O9$ is 132.2(2)°, and it only remains roughly constant in the very first GPa of compression, decreasing progressively with increasing pressure ([Table 2\)](#page-5-0). This is paired with a steady decreasing of the O11⋅⋅⋅O9 and O11⋅⋅⋅O8 distances [\(Table 2](#page-5-0)), which decrease by ∼8.4 and 7.9%. These are not the only atoms of oxygen connected via hydrogen bonding affected by the structure deformation. Indeed, the interatomic O6…O3…O7 angle, which is formed by the oxygen atom O7 (being part of the B2-tetrahedron), acceptor of two hydrogen bonds from the hydroxyl groups O3 and O6 (which belong to the Ca-polyhedron), deforms steadily as pressure increases ([Table 2](#page-5-0)). In addition O11⋅⋅⋅O9 and O11⋅⋅⋅O8, together with the interatomic distances O6⋅⋅⋅O7 and O7⋅⋅⋅O3, decrease drastically with pressure (of ∼5 and 6.7%, [Table 2\)](#page-5-0). The H2O molecule O10 is the donor of two hydrogen bonds, with O4 and O5 as acceptors (Supplementary Fig. S2), two atoms of oxygen that act as hinges in the $[B_3O_3(OH)_5]^{2-}$ polyion. The interatomic angle O5⋅⋅⋅O10 ⋅⋅⋅O4 remains unchanged (within 1σ) up to 8.11(5), GPa, however the distances between the acceptors (O4 and O5) and the donor (O10) progressively decrease of ∼7.9 and 3.7%, respectively. Therefore, the interaction between the oxygen pairs O10⋅⋅⋅O4 and O10⋅⋅⋅O5 increases steadily with pressure. The compression of the hydrogen bond network is significantly larger with respect to the average decrease of the Ca–O, Mg–O and B–O distances ($~4\%$, $~2\%$ and $~1.6\%$, respectively), further highlighting that the main mechanisms with which the structure deforms are (1) the tilting around inter-polyhedral oxygen hinges and (2) compression of the hydrogen bonding network. This phenomenon is analogous to what was observed in several other hydrated borate structures characterised by a pervasive hydrogen bonding network, which plays a paramount role in the stability of the crystalline edifice (e.g. meyerhofferite and inyoite; Comboni et al., [2021b,](#page-7-0) [2022a](#page-7-0)). It is likely that the combination of these two deformation mechanisms induces the changes of the orientation of the unit strain ellipsoid, ultimately affecting the elasticity and the (very moderate)

anisotropy of inderborite. Supplementary Fig. S4 shows the evolu-tion of the O…O distance (reported in [Table 2](#page-5-0)) with pressure. Note that the slopes of such trends change manifestly with pressure, so this can be correlated potentially to the changes in the unit-strain ellipsoid configuration, highlighting, once again, the role of the hydrogen-bonding network on the stability of the crystal structure.

Concluding remarks

In this study, we have investigated the high-pressure behaviour of inderborite through in situ single crystal X-ray diffraction, up to ∼10 GPa. Data collected at high-pressure revealed that:

- (1) The ambient-condition polymorph of inderborite remains stable up to \sim 8 GPa. Between 8.11(5) and 8.80(5) GPa, inderborite undergoes a first-order phase transition. The space group of inderborite-II, which is metrically monoclinic, remains unclear. The phase transition (which is not reversible) is marked by a volume decrease of ∼7.0%.
- (2) The elastic parameters of inderborite have been determined, and the elastic behaviour has been described in detail. These data will contribute to improving the thermodynamic database of hydrous borates.
- (3) With increasing pressure, the volume compression is accommodated primarily by the deformation (and compression) of the hydrogen bonding network, as well as by the tilting of the Ca-, Mg- and B- polyhedrons around the bridging oxygen sites.
- (4) The pressure at which the inderborite-to-inderborite-II phase transition occurs $(8.5 \pm 0.40 \text{ GPa})$ follows the trend observed in most hydrated borates studied so far (Comboni et al., 2020a, 2021a, 2022a; Pagliaro et al., [2021](#page-8-0)), excluding inderite (Comboni et al., 2023). This finding strengthens the presumed correlation between the pressure at which the phase transition occurs and the total H_2O content (in wt.%, Supplementary Fig. S3).
- (5) The bulk modulus of inderborite $(K_{V0} = 41(1)$ GPa) is similar to the bulk modulus of quartz (∼37 GPa) and lower than those of other aggregates used in radiation shielding concretes (e.g. colemanite $K_{V0} = 67(4)$; Okuno, 2005; Lotti et al., [2017\)](#page-8-0). Similarly to colemanite and inderite, inderborite is a Na-free borate, meaning that it cannot promote ASR reactions (i.e. 'alkali-silica reactions'; Thomas, [2011;](#page-8-0) Figueira et al., 2019; Mohammadi et al., [2020](#page-8-0)), which are known to undermine the durability of Portland cements. Considering the stability field of inderborite at high pressure and its elastic parameters, this borate can potentially be used as a B-rich aggregate in radiation-shielding materials.

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Competing interests. The authors declare none.

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