



An interface between the POWHEG BOX and MADGRAPH5_AMC@NLO

Paolo Nason^{1,2,a}, Carlo Oleari^{1,2,b}, Marco Rocco^{1,2,c}, Marco Zaro^{3,d}

¹ Università di Milano-Bicocca, Piazza della Scienza 3, 20126 Milan, Italy

² INFN, Sezione di Milano-Bicocca, Piazza della Scienza 3, 20126 Milan, Italy

³ INFN, Sezione di Milano and TIFLab, Via Celoria 16, 20133 Milan, Italy

Received: 28 August 2020 / Accepted: 15 October 2020 / Published online: 24 October 2020
© The Author(s) 2020

Abstract In this paper we present a framework for developing POWHEG BOX generators using MADGRAPH5_AMC@NLO for the computation of the matrix elements. Within this framework, all the flexibility of MADGRAPH5_AMC@NLO for the generation of matrix elements for Standard Model processes and for several of its extensions can be exploited, as well as all features of the POWHEG BOX framework, including the possibility of multijet merging without a merging scale (using the so called MiNLO approach). As a proof of concept, we develop a generator for the production of a spin-0 Higgs-like boson in association with up to two jets, with CP-violating couplings.

Contents

1 Introduction	1
2 Interface to MG5_AMC	2
2.1 Technical details	3
2.2 Distribution of the code	4
3 A case study: X_0jj production with CP-violating couplings	4
3.1 Theoretical setup	4
3.2 Generation of the code	4
3.3 Simulation parameters	5
3.4 Phenomenology	5
3.5 Reweighting	8
3.6 MiNLO	10
4 Conclusions	10
References	11

^a e-mail: paolo.nason@mib.infn.it

^b e-mail: carlo.oleari@mib.infn.it (corresponding author)

^c e-mail: m.rocco10@campus.unimib.it

^d e-mail: marco.zaro@mi.infn.it

1 Introduction

Next-to-leading-order (NLO) calculations for Standard Model (SM) and, sometimes, beyond-the-SM (BSM) processes, interfaced to parton shower (PS) generators, generally dubbed NLO+PS generators, are by now the methods of choice for the generation of event samples for signal and background processes at the LHC. This state of the art has been made possible, on the one side, by the formulations of general methods for computing NLO corrections [1, 2], and, on the other, by the theoretical development of algorithms for interfacing fixed order calculations with parton shower generators [3–8]. These algorithms were implemented in software packages for the automatic computation of NLO corrections [9–13], and for the automatic implementation of NLO+PS generators [9, 14–17] that considerably ease the construction of generators for new processes.

MADGRAPH5_AMC@NLO, often abbreviated to MG5_AMC in the following, is a framework where automation has been pushed to the highest level. In fact, a user without any knowledge of NLO calculations or NLO+PS implementations can easily generate samples of parton-level events with NLO+PS accuracy, within the MC@NLO procedure. These events can be then directly fed into a PS generator, such as PYTHIA or HERWIG. The MG5_AMC framework is not restricted to the case of SM processes. In fact, it is possible to employ any user-defined model if this is provided in the so-called UFO format [18], for example as generated by FEYNRULES [19, 20]. In particular, in order to undertake an NLO computation, the model should include the relevant UV and rational counterterms (both needed for the numerical evaluation of the one-loop matrix elements), which can be also automatically computed with FEYNRULES+NLOCT [21]. Furthermore, the FEYNRULES+MG5_AMC framework has been recently extended in order to fully support the supersymmetric case, including the implementation of different renormal-

isation conditions [22], and the use of the so-called diagram removal and diagram subtraction techniques when intermediate resonances are present. NLO capabilities for BSM processes have been proven successful for a number of processes, see Ref. [22] and references therein.

The POWHEG method allows to generate events with positive weights and, because of this, it has become the method of choice when large samples of events are needed. In fact, in view of the large amount of computer resources needed for detector simulation, the experimental collaborations cannot afford to use the larger samples that are required when negative weights are present.¹ The method has been also extended with the introduction of some theoretical developments of general interest. One of them deals with the generation of multijet samples that maintain a certain level of accuracy, even when some of the jets become unresolved [24,25]. This approach has also led to the development of NNLO+PS generators, i.e. generators where next-to-next-to-leading-order (NNLO) calculations are interfaced to parton showers [26–28].² Another development has been the extension of the POWHEG method for the inclusion of processes with decaying coloured resonances, which is capable of handling the interference of the emitted radiation generated in production and decay [32].³

The POWHEG BOX framework automatizes the construction of NLO+PS generators, once the matrix elements are available. In the early POWHEG BOX processes, the matrix elements were obtained from the authors of specific calculations. A considerable leap in the construction of the matrix elements took place when an interface of the POWHEG BOX to MADGRAPH4 was set up [34], allowing for the implementation of all tree-level ingredients required by a given NLO process. After this development, the only missing ingredient for an NLO calculation in the POWHEG BOX was the virtual contribution. Later, interfaces to automatic generators of virtual processes were also developed in Refs. [35,36] for GOSAM, and in Ref. [37] for OPENLOOPS.

As of now, an interface to the matrix-element generator that is available within the MG5_AMC package has not been developed. The main obstacle is the fact that MG5_AMC is built as a single package that aims at the production of partonic events, at difference with MADGRAPH4, that was initially conceived for the generation of tree-level matrix elements. An interface between the matrix-element generator of MG5_AMC and the POWHEG BOX is also highly desirable since many BSM processes are available within MG5_AMC.

In order to exploit the full capabilities of the MG5_AMC package, such interface should also build, in addition to the virtual contribution, all the necessary tree-level matrix elements: the Born, the colour- and spin-correlated Born, and the real matrix elements.

The purpose of the present work is to present an interface between the MG5_AMC matrix-element generator and the POWHEG BOX. The structure of the interface is such that developments in MG5_AMC and POWHEG can remain independent to a large extent. For this reason, our aim is not to construct a framework that is automatized at the same level as the full MG5_AMC package itself, but rather to build an MG5_AMC extension that makes the NLO matrix elements readily available to POWHEG. Thus, progresses on the POWHEG BOX side and on the MG5_AMC side can take place independently, which is a considerable advantage in view of the way in which theoretical projects are developed. Furthermore, this kind of interface allows generalisations to other NLO+PS frameworks, that may also benefit from it for the implementation of the matrix elements.

The paper is organised as follows. In Sect. 2 we describe the interface and we give some technical details on how to use it and how to distribute the generated code. In Sect. 3 we consider, as a case study, the production of a spin-0 boson X_0 plus two jets. In particular, we present a few distributions able to characterise the X_0 boson CP properties and we discuss some features connected to the POWHEG BOX reweighting feature. We also show a few distributions obtained with the MiNLO approach. Finally, in Sect. 4 we draw our conclusions.

2 Interface to MG5_AMC

The new interface between POWHEG and MG5_AMC uses the capability of the latter to provide tree-level and one-loop matrix elements to be used by the former. The interface itself is a plugin for MG5_AMC: as such, it does not require any modification of the core code and it works with any recent version of MG5_AMC.⁴ It re-organises the output of MG5_AMC in a format which is suitable for the POWHEG BOX [14], closely following what is described in Ref. [34]. At variance with what is discussed there, no external providers for the one-loop matrix elements are needed. Rather, one-loop matrix elements are directly generated by MG5_AMC thanks to the MADLOOP module [9,39], which encapsulates several different strategies, such as integrand reduction [40], Laurent-series expansion [41] and tensor-

¹ A variant of the MC@NLO method for drastically reducing the negative weight fraction has appeared in Ref. [23].

² Alternative methods for multijet merging have been presented in Refs. [7,8,29]. Alternative methods for NNLO+PS accuracy have been proposed in Refs. [30,31].

³ See also Ref. [33].

⁴ Versions 2.6 and onward are fully supported, for what concerns QCD corrections. The extension of the interface to more recent releases able to deal with electro-weak corrections (from version 3) [38] is left for future work.

integral reduction [42–44], as implemented in different computer libraries [45–48] and improved by an in-house implementation of the OPENLOOPS method [10]. Thus, by fully exploiting the capabilities of MADLOOP, the evaluation of virtual matrix elements and the assessment of the numerical stability of the results are granted. Along with the matrix elements, the relevant helicity routines are also provided, in the ALOHA format [49].

2.1 Technical details

The interface plugin, dubbed MG5AMC-PWG, is publicly available.⁵ Its usage is very simple, as one only needs to copy (or link) the MG5AMC_PWG folder inside the PLUGIN directory of MG5_AMC. Please refer to the README file enclosed in the package for conditions of usage and instructions.

The plugin can be loaded by launching, within the MG5_AMC installation directory,

```
./bin/mg5_aMC --mode=MG5aMC_PWG
```

in a command shell. In order to generate the code for a specific process at NLO QCD accuracy, the usual syntax of MG5_AMC should be employed. For example, in the case of top-pair production, the syntax is the following:

```
generate p p > t t~ [QCD]
output pp_ttx
```

where `pp_ttx` is the name (chosen by the user) of the directory where the code will be created. During the execution of the `generate` command, the MG5AMC-PWG plugin checks whether an installation of the POWHEG BOX V2 is available on the system and asks for its installation path (this is needed only once).

When this stage is concluded, the user can `quit` MG5_AMC and finds the MG5_AMC code for the Born, real and virtual contributions in the `pp_ttx` directory, in addition to a few basic POWHEG BOX V2 files. In particular, the `Born.f`, `real.f` and `virtual.f` files are ready to be used. Also the `init_processes.f` file can be used as it is, but can be also modified if particular features of the POWHEG BOX V2 need to be activated and initialised.

A few comments about the other files are in order:

- The `Born_phsp.f` file is just a place holder. It needs to be replaced by the actual phase-space generator for the process at hand. Examples of `Born_phsp.f` implementations can be found in the processes already imple-

mented in the POWHEG BOX V2. In the current setup, a subroutine `born_suppression` should be also implemented in the `Born_phsp.f` file. This function is used at the integration stage to suppress divergences when present at the Born level, i.e. when there are jets and photons.

- The call of the `setpara("param_card.dat")` routine in the `init_couplings.f` file initialises the parameters listed in the `Cards/param_card.dat` file to the corresponding values, according to the UFO model [18] used in MG5_AMC.⁶ It is also possible to assign a value to a MG5_AMC parameter at execution time. An example of this can be found in the `init_couplings.f` file for the process X_0jj , that we discuss in Sect. 3. In this file we reassign the value of $\cos\alpha$, the CP-mixing parameter that appears in the Lagrangian of Eq. (3.3). This parameter is indicated with `cosa` in the `Cards/param_card.dat` file, and is initialised to the value specified in this file, if no further action is taken. In order to reassign its value at execution time, we change the values of the internal MG5_AMC variables, `mdl_cosa` and `mp_mdl_cosa` (for double and quadruple precision), that encode this parameter.

After any reassignment of the MG5_AMC parameters, the user has to call the `coup` routine in order to recompute all the dependent variables.

- In order to have full consistency between the MG5_AMC amplitudes and what is computed by the POWHEG BOX V2, all the physical parameters used by the POWHEG BOX V2 should be set starting from those assigned or computed by MG5_AMC. An example of this is the list of the external-particle masses, `kn_masses`, used by POWHEG BOX V2 when generating the kinematics of the event. Using $t\bar{t}$ production as example, `kn_masses` should be set to

```
\( 0, 0, mdl_mt, mdl_mt, 0 \)
```

in `init_couplings.f` or `Born_phsp.f`, where `mdl_mt` is the mass of the top quark used inside MG5_AMC, the first two entries are the masses of the incoming particles, and the last massless particle is the radiated one, when computing the real contribution.

- The interface also builds a script file, `prepare_run_dir`, that is useful to create a directory where the produced code can be executed. For example, by typing the command

⁵ Details can be found at <https://code.launchpad.net/~mg5amc-pwg-team/mg5amc-pwg/v0>, while the code can be downloaded with the command: `bzr branch lp: mg5amc-pwg-team/mg5amc-pwg/v0`. The installation of the revision control system `bazaar` is required.

⁶ It should be noted that the `Cards/param_card.dat` file is not read at execution time. Rather, it is parsed at compilation time into a FORTRAN include file, which is then compiled together with the code. Hence, after any parameter modification within this file, the main executable has to be recompiled.

```
./prepare_run_dir test
```

a directory `test` is created. This directory contains all the relevant links to the `MG5_AMC` code and a template of the `powheg.input` file, required by the `POWHEG BOX V2`. This last file should then be changed and modified according to the process at hand.

The `POWHEG` process generated along these lines can be completed with all sorts of features that are commonly used in the `POWHEG BOX V2`. For example, one can activate the `MinLO` option for processes with associated jets, or use the `damping` option to separate the real contributions into two parts, along the lines of what was suggested in the original `POWHEG` paper [4], and applied for the first time in Ref. [50].

2.2 Distribution of the code

A process generated with this interface to `MG5_AMC` cannot be distributed as a usual `POWHEG BOX` process, since the searching path of the linked libraries are written in several files at generation time.

An author can distribute the instructions for `MG5_AMC`, needed in order to generate the process, and the actual files, that overwrite the place holders created by the interface plugin. In this way, all relevant paths point to the right directories in the user computer.

Alternatively, the author of the process may provide a script file that automatically executes all these tasks, helping the installation phase.

3 A case study: $X_0 jj$ production with CP-violating couplings

For our case study, we considered the production of a spin-0 boson X_0 (a Higgs-like boson) that couples to a massive top quark, produced via gluon fusion, and accompanied by two jets, in the heavy-top-mass limit. We discuss a few distributions able to characterise the X_0 boson CP properties, and discuss a few results obtained using the `POWHEG BOX V2` reweighting feature. We also present a few distributions obtained with the `MinLO` method.

3.1 Theoretical setup

The theoretical framework of this study is fully inherited from what was done in Ref. [51], where the process was studied at NLO in QCD. In particular, in the heavy-top-mass limit, the CP structure of the X_0 -top interaction characterises the effective ggX_0 vertex. The starting point is the effective Lagrangian

$$\mathcal{L}_0^t = -\bar{\psi}_t (k_{Htt} g_{Htt} \cos \alpha + i k_{Att} g_{Att} \sin \alpha \gamma_5) \psi_t X_0, \quad (3.1)$$

where X_0 is the spin-0 boson, ψ_t the top-quark spinor, α the CP-mixing angle parameter ($0 \leq \alpha \leq \pi$), k_{Htt} and k_{Att} the real coupling parameters and

$$g_{Htt} = g_{Att} = \frac{m_t}{v} = \frac{y_t}{\sqrt{2}} \quad (3.2)$$

the Yukawa couplings, with v the vacuum expectation value.

The CP-even case, that will be labeled 0^+ , corresponds to the assignment $\cos \alpha = 1$, namely to the SM scenario, while the CP-odd case, labeled 0^- , to $\cos \alpha = 0$. A CP-mixed case, 0^\pm , where the spin-0 boson receives contributions from both a scalar and a pseudoscalar state, is also taken into account by setting $\cos \alpha = 1/\sqrt{2}$.

For our purposes, it will suffice to notice that the Higgs interaction with the gluons originates as an effective coupling induced by a top-quark loop. The relevant effective Lagrangian, in the *Higgs Characterisation* framework [52], reads

$$\mathcal{L}_{0,g}^{\text{loop}} = -\frac{1}{4} (k_{Hgg} g_{Hgg} \cos \alpha G_{\mu\nu}^a G^{a,\mu\nu} + k_{Agg} g_{Agg} \sin \alpha \epsilon^{\mu\nu\rho\sigma} G_{\mu\nu}^a G_{\rho\sigma}^a) X_0, \quad (3.3)$$

where $G_{\mu\nu}^a$ is the gluon field strength and

$$k_{Hgg} = -\frac{\alpha_S}{3\pi v}, \quad k_{Agg} = \frac{\alpha_S}{2\pi v}. \quad (3.4)$$

The theoretical setup is made available online in the `FEYN-RULES` [20] repository as a UFO model named `HC_NLO_X0` [51,53–55], which is in fact the one used for our case study.

3.2 Generation of the code

In order to generate the code, we have first to install the UFO model `HC_NLO_X0_UFO.zip` under the `models` directory of the `MG5_AMC` version being used. We have then followed the procedure described in Sect. 2.1 for the generation of the code, and given the following commands to `MG5_AMC`:

```
import model HC_NLO_X0_UFO-heft
generate p p > x0 j j / t [QCD]
install ninja
install collier
output X0jj
```

where we have also inserted the command lines to install `NINJA` [46] and `COLLIER` [48], that are optional and need to be installed just once.

We have then overwritten the `Born_phsp.f` file generated by the interface with the `Born_phsp.f` from the `Hjj`

POWHEG BOX V2 process, taking care of assigning to the POWHEG variables `hmass` and `hwidth` (the mass and width of the Higgs-like boson) the MG5_AMC values, `mdl_mx0` and `mdl_wx0` respectively.

In order to ease the installation procedure, we provide a `tarball` file that needs to be inflated in the installation directory. This file contains all the modified files that replace the place holders.

3.3 Simulation parameters

We have performed a simulation for the LHC, running at a centre-of-mass energy of $\sqrt{s} = 13$ TeV. The mass of the spin-0 boson X_0 has been set equal to 125 GeV. We have chosen the NNPDF2.3 (NLO) set [56] for the parton distribution functions, within the LHAPDF interface [57,58].

The differential cross section for X_0jj production is already divergent at the Born level, unless a minimum set of generation cuts is imposed on the transverse momentum of the final-state jets and on their invariant mass. Alternatively, the divergences can be avoided if the code is executed with the MiNLO option activated. We have generated the kinematics of the underlying Born configurations imposing the following minimum set of cuts

$$p_T^{jk} > 10 \text{ GeV}, \quad k = 1, 2, \quad m_{j_1j_2} > 10 \text{ GeV}. \quad (3.5)$$

In the phenomenological study we perform in Sect. 3.4, we apply more stringent cuts, and we have checked that the results we present are insensitive to the generation cuts.

In order to integrate the divergent underlying Born cross section, the POWHEG BOX V2 can further apply a suppression factor at the integrand level. We stress that the final kinematic distributions are independent of this factor.⁷

3.4 Phenomenology

In this section we present results produced by the POWHEG BOX V2 at the Les Houches Event (LHE) level, i.e. after the emission of the first radiation, accurate at NLO for large transverse momentum, and with leading-logarithmic accuracy at small p_T , due to the presence of the POWHEG Sudakov form factor. The results are computed on samples of 3.2 M events.

The renormalisation and factorisation scales are set to

$$\mu_R = \mu_F = \frac{H_T}{2}, \quad (3.6)$$

where H_T is the sum of the transverse masses of the particles in the final state.

⁷ We have set `bornsuppfact` to 30 GeV in our simulation.

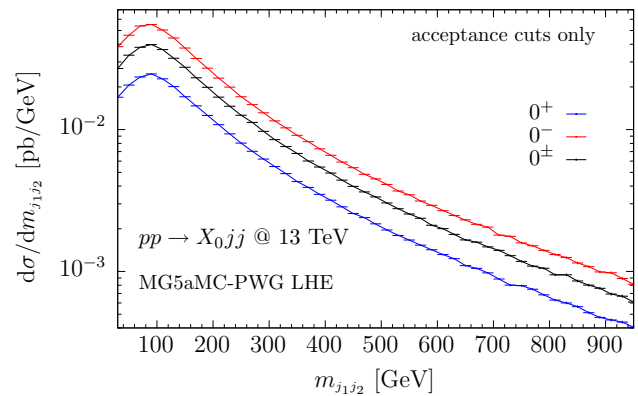


Fig. 1 Differential cross section as a function of the invariant-mass distribution of the two leading jets in $pp \rightarrow X_0jj$ for the three CP scenarios. The blue curve corresponds to the CP-even scenario with $\cos \alpha = 1$, the red curve to the CP-odd scenario with $\cos \alpha = 0$ and the black curve to the mixture of the 0^+ and 0^- scenarios with $\cos \alpha = 1/\sqrt{2}$

Jets are reconstructed employing the anti- k_T algorithm [59] via the FASTJET implementation [60], with distance parameter $R = 0.4$, and the two leading jets are required to have transverse momentum and pseudorapidity such that

$$p_T^{jk} > 30 \text{ GeV}, \quad |\eta_{jk}| < 4.5, \quad k = 1, 2. \quad (3.7)$$

Events that do not pass this minimum set of acceptance cuts are discarded.

In Fig. 1 we plot the differential cross section for X_0jj production as a function of the invariant mass of the two leading jets, $m_{j_1j_2}$, for three different CP scenarios: CP even (0^+), CP odd (0^-) and a mixture of the two (0^\pm). The shapes of the three spectra are very similar among each other. Since a cut on the invariant mass of the dijet system enhances the discriminating power among different CP scenarios [61], the fact that the three spectra have similar shapes implies that the cut acts in a similar way on each of them. Typically a cut on $m_{j_1j_2}$ enhances the contributions coming from the exchange of a gluon in the t channel, and these contributions are more sensitive to the CP properties of the X_0 boson.

In the following plots we impose an additional cut on the dijet mass. In particular, we consider the two cases where

$$m_{j_1j_2} > 250 \text{ GeV} \quad \text{and} \quad m_{j_1j_2} > 500 \text{ GeV}. \quad (3.8)$$

In addition, since we are interested in shape comparisons among different CP scenarios, we normalise each curve to one.

In Figs. 2 and 3 we plot the transverse momentum and pseudorapidity of the X_0 boson, and in Figs. 4 and 5 we show the transverse momentum and pseudorapidity of the leading jet. The increase of the cut on the dijet mass hardens the p_T spectrum of the X_0 boson and the leading jet j_1 . Moreover,

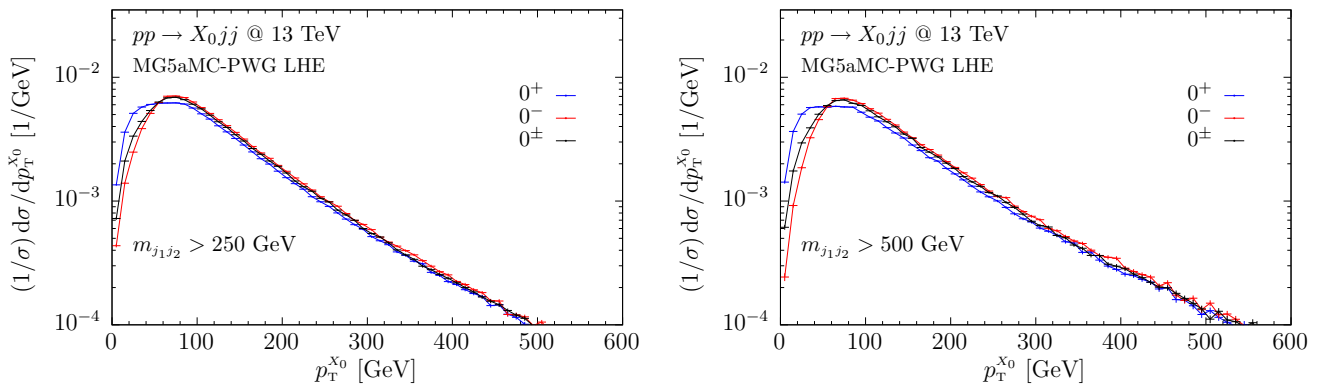


Fig. 2 Normalised differential cross section as a function of the transverse momentum of the spin-0 boson X_0 , for the three CP scenarios. On the left panel, a cut of 250 GeV is imposed on the dijet mass, while on the right panel a cut of 500 GeV is applied. The colour code is the same as in Fig. 1

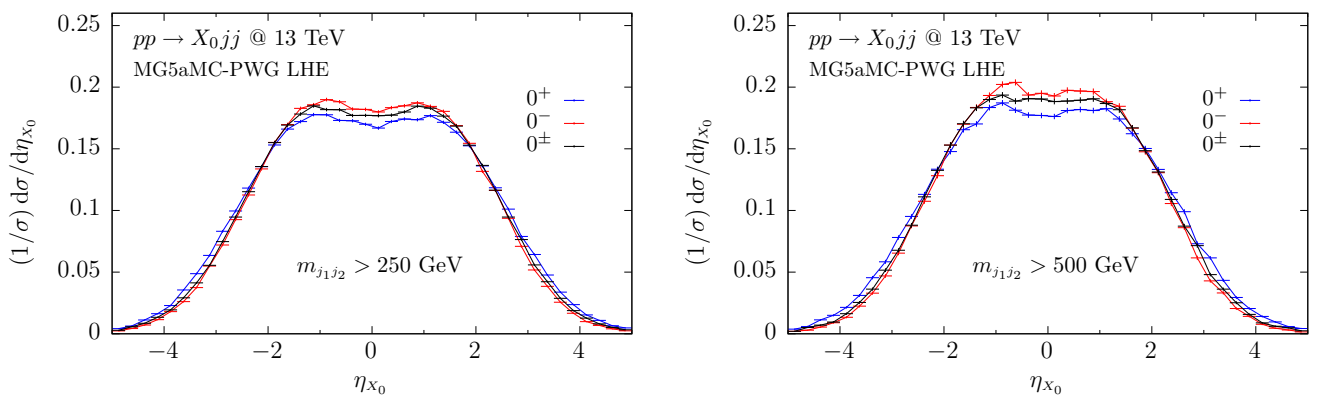


Fig. 3 Normalised differential cross section as a function of the pseudorapidity of the spin-0 boson X_0 , for the three CP scenarios. On the left panel, a cut of 250 GeV is imposed on the dijet mass, while on the right panel a cut of 500 GeV is applied. The colour code is the same as in Fig. 1

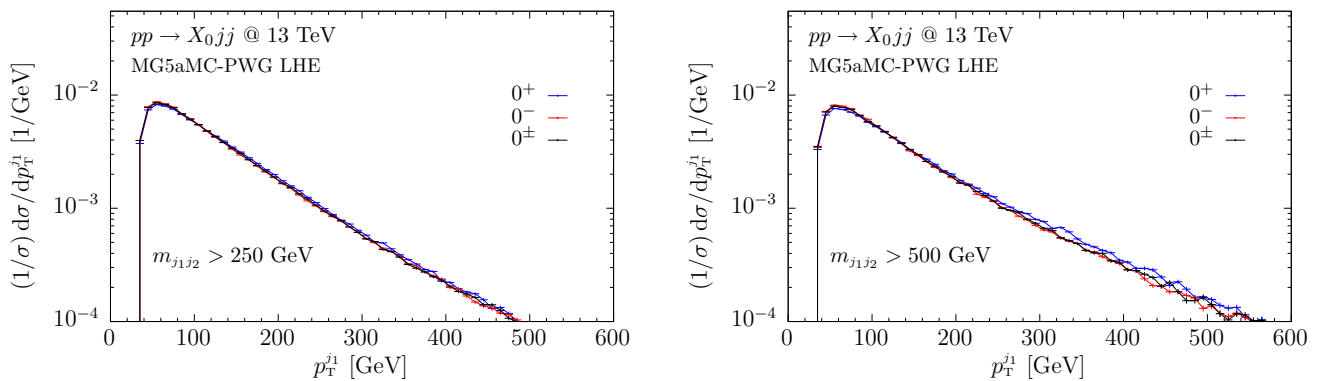


Fig. 4 Normalised differential cross section as a function of the transverse momentum of the leading jet, for the three CP scenarios. On the left panel, a cut of 250 GeV is imposed on the dijet mass, while on the right panel a cut of 500 GeV is applied. The colour code is the same as in Fig. 1

there are only mild differences among the three CP scenarios in the X_0 distributions at low transverse momentum and in the central pseudorapidity region, with a modest enhancement when the dijet-mass cut increases. No substantial differences

are present in p_T^{j1} and η_{j1} , also in agreement with what is found in Ref. [51].⁸

⁸ A possible concern is to what extent the effective-field-theory (EFT) Lagrangian of Eq. (3.3) produces sound results in the high-energy regimes, since it describes the full theory in the heavy-top-quark limit. From the exact calculation of Ref. [62], it is known that the EFT closely reproduces the $m_{j_1 j_2}$ spectrum even in the very high invariant-mass

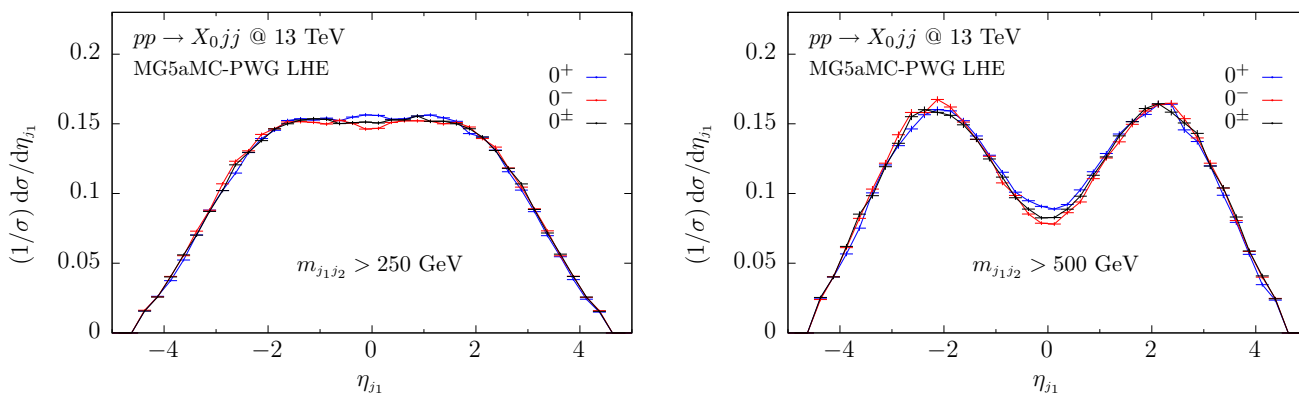


Fig. 5 Normalised differential cross section as a function of the pseudorapidity of the leading jet, for the three CP scenarios. On the left panel, a cut of 250 GeV is imposed on the dijet mass, while on the right panel a cut of 500 GeV is applied. The colour code is the same as in Fig. 1

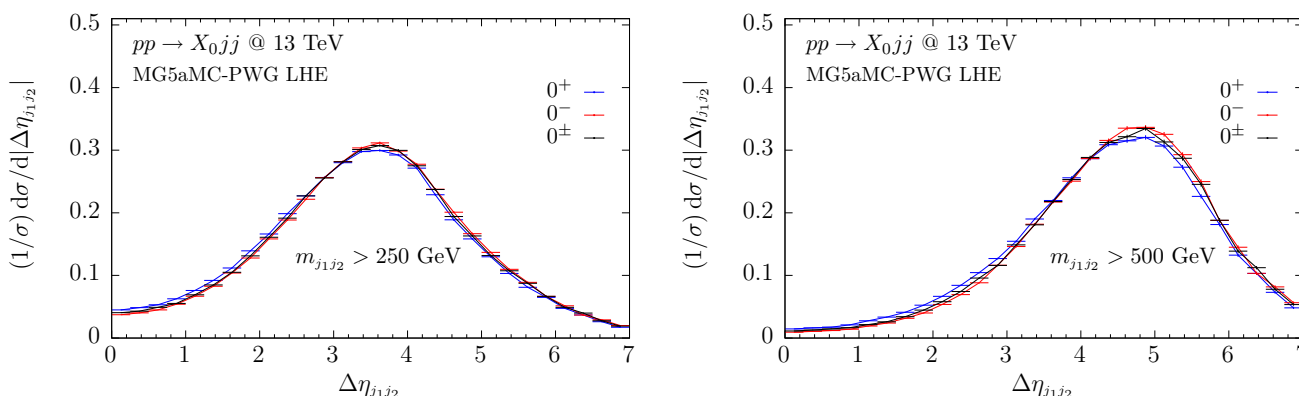


Fig. 6 Normalised differential cross section as a function of the pseudorapidity separation of the two leading jets (see Eq. (3.9)), for the three CP scenarios. On the left panel, a cut of 250 GeV is imposed on the dijet mass, while on the right panel a cut of 500 GeV is applied. The colour code is the same as in Fig. 1

The most sensitive observables to the CP coupling of the X_0 boson to the top quark in gluon fusion are dijet-correlation variables [61, 64–70]. As displayed in Fig. 6, no significant differences are seen in the differential cross sections as a function of the pseudorapidity separation of the two leading jets

$$\Delta\eta_{j_1j_2} = |\eta_{j_1} - \eta_{j_2}|. \tag{3.9}$$

Instead, when the differential cross sections are expressed as a function of the azimuthal-angle separation, the CP nature of the coupling is more evident [61]. In fact, the shape of the differential cross sections as a function of $\Delta\phi_{j_1j_2}$ are very different, as shown in Fig. 7, where we have defined (modulo 2π)

region. However, the EFT approximation breaks down when the transverse momenta of the jets are larger than the top mass [63], overestimating the exact prediction when p_T^i is larger than the top mass. Since the region of interest for discriminating the CP properties is at low transverse momentum, we can trust the results obtained within the EFT approach.

$$\Delta\phi_{j_1j_2} = |\phi_{j_1} - \phi_{j_2}|, \tag{3.10}$$

where the azimuth of a jet is computed as

$$\phi_{j_k} = \arg(\mathbf{p}^{j_k} \cdot \hat{y} + i \mathbf{p}^{j_k} \cdot \hat{x}), \quad k = 1, 2, \tag{3.11}$$

with \mathbf{p}^{j_k} the tri-momentum of the jet k and \hat{x} (\hat{y}) the unit vector along the x (y)-axis direction.

As pointed out in Refs. [65, 71], a more CP-sensitive observable (especially for the maximal mixing scenario of $\cos\alpha = 1/\sqrt{2}$ considered here) is the oriented azimuthal separation of the two hardest jets. This variable contains information not only on the azimuthal separation of the two jets but also on the sign of the azimuthal angle. We have adopted the definition of this variable of Ref. [72], namely

$$\Delta\phi_{j_1j_2}^{\text{or}} \equiv \frac{(\hat{\mathbf{p}}_T^{j_1} \times \hat{\mathbf{p}}_T^{j_2}) \cdot \hat{z}}{|\hat{\mathbf{p}}_T^{j_1} \times \hat{\mathbf{p}}_T^{j_2}| \cdot \hat{z}} \frac{(\mathbf{p}^{j_1} - \mathbf{p}^{j_2}) \cdot \hat{z}}{|(\mathbf{p}^{j_1} - \mathbf{p}^{j_2}) \cdot \hat{z}|} \arccos(\hat{\mathbf{p}}_T^{j_1} \cdot \hat{\mathbf{p}}_T^{j_2}), \tag{3.12}$$

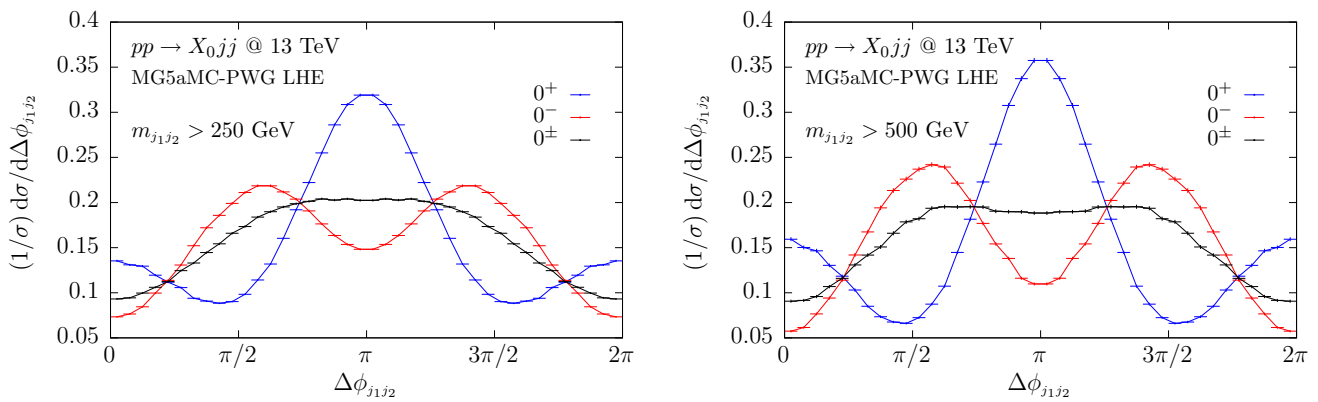


Fig. 7 Normalised differential cross section as a function of the azimuthal separation of the two leading jets (see Eq. (3.10)), for the three CP scenarios. On the left panel, a cut of 250 GeV is imposed on the dijet mass, while on the right panel a cut of 500 GeV is applied. The colour code is the same as in Fig. 1

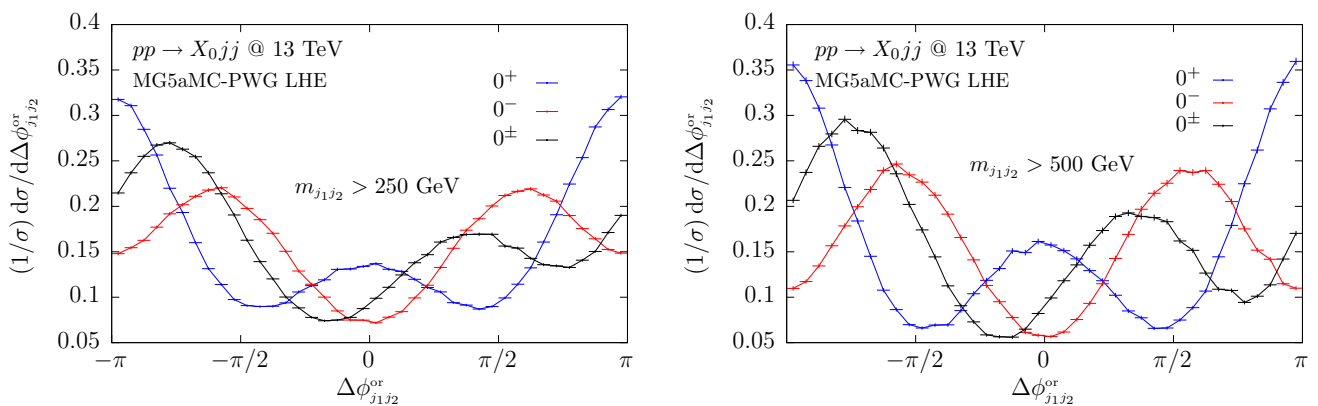


Fig. 8 Normalised differential cross section as a function of the oriented azimuthal separation of the two leading jets, defined in Eq. (3.12), for the three CP scenarios. On the left panel, a cut of 250 GeV is imposed

on the dijet mass, while on the right panel a cut of 500 GeV is applied. The colour code is the same as in Fig. 1

where $\hat{\mathbf{p}}_T^{jk}$ is the jet transverse momentum, normalised to one, and $\hat{\mathbf{z}}$ is the unit vector along the z-axis direction.

The differential cross sections for the three different CP scenarios considered in this paper, as a function of $\Delta\phi_{j_1j_2}^{or}$, are shown in Fig. 8, and their shapes are visibly different.

In particular, the oriented azimuthal separation can also distinguish between the two scenarios with $\cos\alpha = 1/\sqrt{2}$ and $\cos\alpha = -1/\sqrt{2}$, as illustrated in Fig. 9, while $\Delta\phi_{j_1j_2}$ cannot distinguish between them.

3.5 Reweighting

In this section we present a few results obtained with the POWHEG BOX V2 reweighting feature. We have reweighted two of the event samples that we have produced: the scalar and the mixed one. We have then compared the reweighted distributions with the original ones, i.e. those computed from

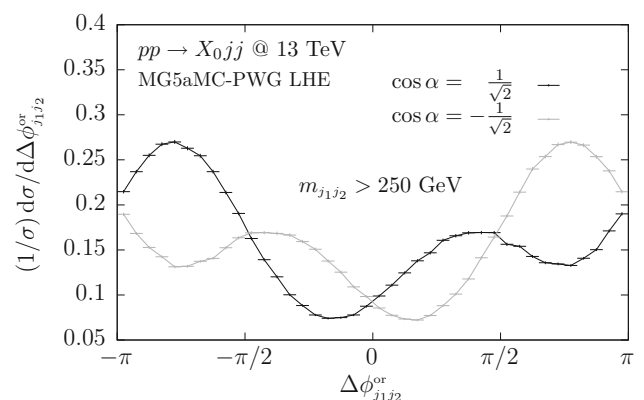


Fig. 9 Normalised differential cross section as a function of the oriented azimuthal separation of the two leading jets, defined in Eq. (3.12), for the two mixed CP scenarios with $\cos\alpha = 1/\sqrt{2}$ (black curve) and $\cos\alpha = -1/\sqrt{2}$ (grey curve). A cut of 250 GeV is imposed on the dijet mass

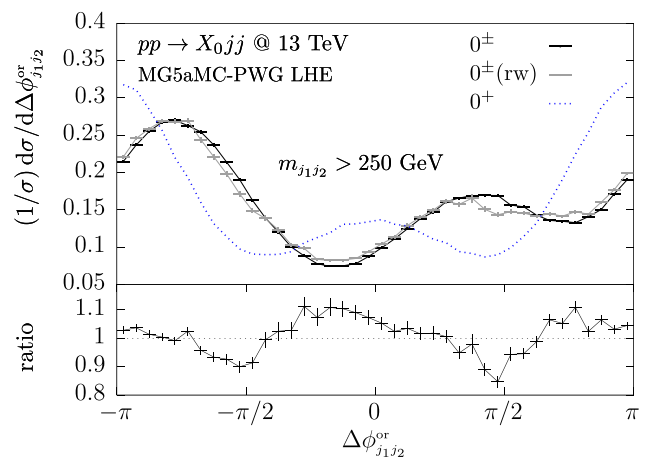
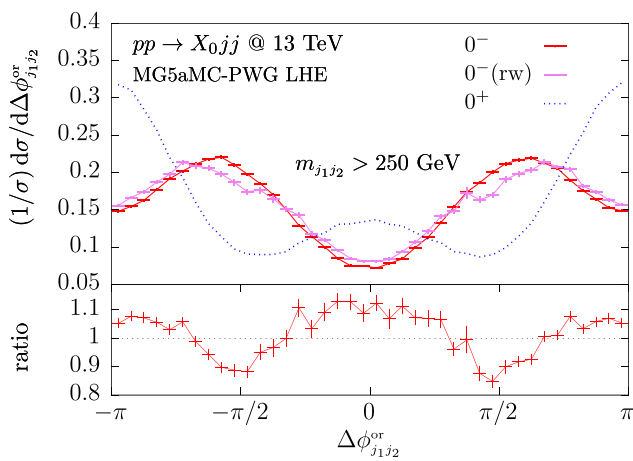


Fig. 10 Normalised differential cross section as a function of the oriented azimuthal separation of the two leading jets, defined in Eq. (3.12), with a cut of 250 GeV imposed on the dijet mass. On the left panel, the pseudoscalar original distribution in red, the pseudoscalar as obtained by reweighting (rw) in pink, and the scalar one in dotted blue. On the

right panel, the CP mixed original distribution in black, the mixed as obtained by reweighting (rw) in gray, and the scalar one in dotted blue. The ratios between the distributions obtained by reweighting and the original ones are also shown

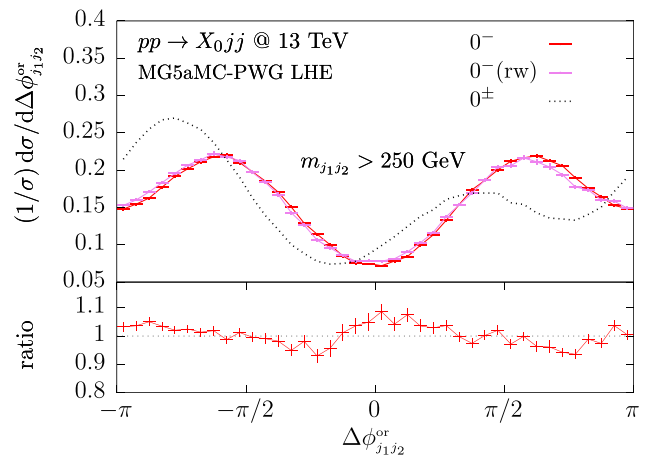
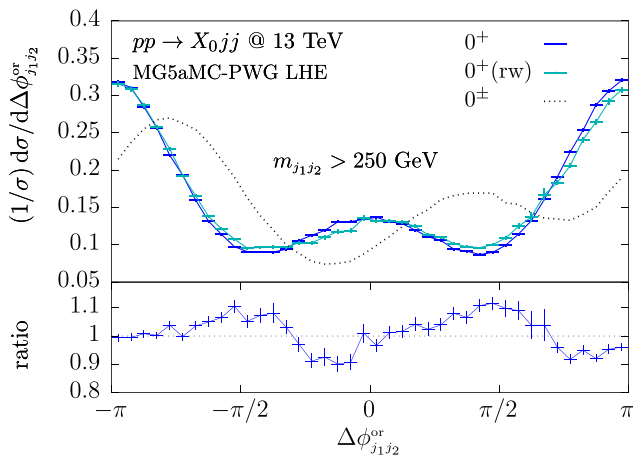


Fig. 11 Same as Fig. 10 but for the reweighting of the CP mixed sample to the scalar case (on the left) and to the pseudoscalar one (on the right)

the beginning with a given value of $\cos \alpha$. In particular, we have reweighted the scalar sample to the pseudoscalar and CP mixed cases, and we have reweighted the mixed sample to the scalar and pseudoscalar ones. We have found an overall good agreement between the reweighted and the original distributions, except for the distribution of the differential cross section expressed as a function of the oriented azimuthal angle, i.e. the distributions most sensitive to the value of the CP parameter $\cos \alpha$.

In Fig. 10 we compare three curves. The $\Delta\phi_{j_1j_2}^{or}$ distribution obtained from the original scalar sample is plotted in dotted blue, on both panels. This curve corresponds to the 0^+ line on the left panel of Fig. 8. The scalar sample is reweighted to the pseudoscalar scenario on the left panel and to the mixed scenario on the right panel. The reweighted sample, indicated with “rw” in the figures, is then compared with the original

distribution. The ratio of the last two curves is also plotted. In both cases, in correspondence to the minima of the 0^+ distribution, the discrepancy between the reweighted distribution and the original one is more than -10% , the minus sign to indicate that the distributions obtained by reweighting underestimate the original ones. The opposite is also true: when the 0^+ distribution has maxima that are not close to the maxima of the 0^- and 0^\pm distributions, we have a discrepancy on the opposite side, up to $+10\%$.

Similar conclusions can be drawn by reweighting the 0^\pm sample, as illustrated in Fig. 11, in order to produce the differential cross section as a function of $\Delta\phi_{j_1j_2}^{or}$ for the 0^+ and 0^- scenarios.

These differences can be explained by noticing that the minima of the above distributions are actually zeros at LO, and the production of events around these regions is then

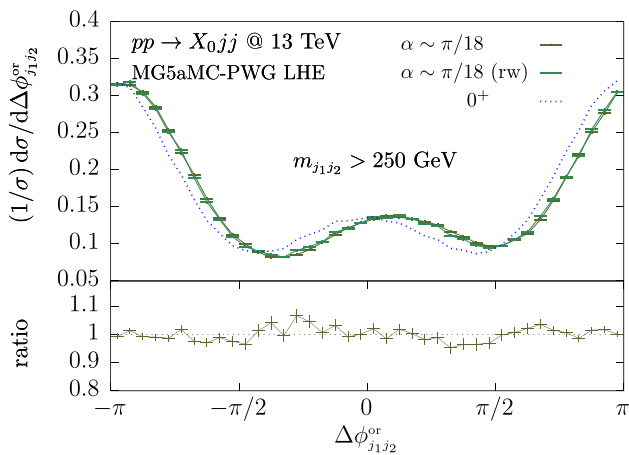


Fig. 12 Same as Fig. 10 but for the reweighting of the scalar sample to the CP scenario defined by $\cos \alpha = 0.985$

suppressed. The reweighting procedure is not able to generate the correct distributions, if the starting one is very different from the final one, i.e., for example, going from $\alpha = 0$ to $\alpha = \pi/2$, for the reweighting of the scalar case to the pseudoscalar one.

Otherwise, if the reweighting procedure is used to reweight distributions with similar values of the angle α , the procedure correctly works. This is shown in Fig. 12, where the distribution computed with $\alpha = 0$ is reweighted to the distribution with $\alpha \sim 10^\circ \sim \pi/18$, and the agreement with the exact one is very good.

3.6 MiNLO

In this section we present a few results for the pseudoscalar X_0 production, obtained within the MiNLO procedure. Although all the cuts applied on the jets in the previous sections are completely removed, the differential cross sec-

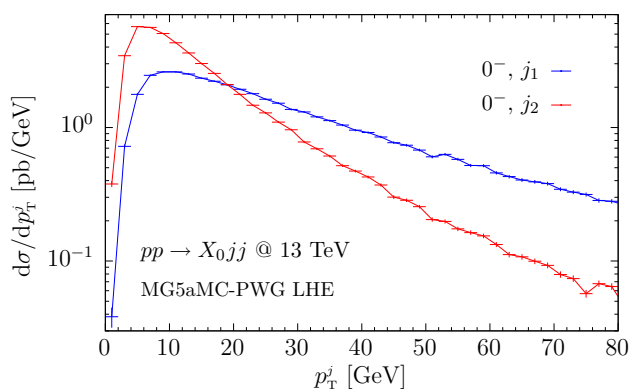


Fig. 13 On the left panel the inclusive differential cross section as a function of the transverse momentum of the hardest jet, in blue, and of the second-to-hardest one, in red. The CP scenario is defined by

tions for inclusive quantities are finite, due to the presence of the MiNLO Sudakov form factor.

This is shown, for example, in Fig. 13, where we plot the inclusive differential cross section as a function of the transverse momentum of the hardest and of the second-to-hardest jet, on the left panel, and the inclusive rapidity of the X_0 boson, on the right one.

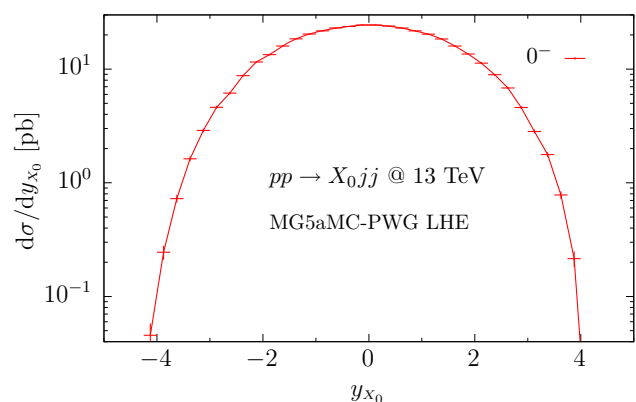
Although finite, we cannot make any claim on the accuracy of these distributions, i.e. they do not reach the NLO accuracy of the MiNLO' method, described in Refs. [25, 73].⁹

4 Conclusions

In this paper we have presented an interface between MADGRAPH5_AMC@NLO and the POWHEG BOX V2, able to build a NLO + parton shower generator for Standard Model and many beyond-the-Standard-Model processes, in an automatic way.

The structure of the interface is such that future developments in MADGRAPH5_AMC@NLO and POWHEG BOX V2 remain independent to a large extent, so that it benefits from all the progresses coming from both sides. In fact, on the one side, MADGRAPH5_AMC@NLO provides the matrix elements for the Born, the colour- and spin-correlated Born, the real and the virtual contributions. On the other, the POWHEG BOX uses these ingredients to generate events accurate at the NLO + parton shower level. In addition, the interface writes

⁹ Our MG5aMC-PWG implementation is NLO accurate only for quantities involving two detected jets. The MiNLO procedure allows to obtain finite and LO accurate predictions for quantities with one or zero detected jets. Otherwise, the only available method able to reach NLO accuracy for one-jet inclusive distributions, for colour-singlet production with two associated jets within the POWHEG-MiNLO method, is the one illustrated in Ref. [73].



$\cos \alpha = 0$, namely, the pseudoscalar case. On the right panel in red, the inclusive rapidity of the X_0 boson, for the same CP scenario as in the left panel. Both plots are obtained with MiNLO

other files needed by the POWHEG BOX V2. Some of them, as the list of processes, are fully finalised. Others, such as the phase-space generator, need to be adjusted in order to deal with the process at hand.

By now the interface only deals with processes for which we aim at NLO QCD accuracy. The extension including the electroweak corrections and the interface with the more recent version of the POWHEG BOX, i.e. the POWHEG BOX RES, is left as future work.

As a case study, using this interface we have generated the code for the production of a spin-0 boson plus two jets, and we have computed a few kinematic distributions, sensitive to the CP properties of the coupling of the boson with a massive top quark. We have compared these distributions with known results in the literature and found full agreement. We have also presented a few results for the pseudoscalar case, obtained within the MiNLO approach.

Finally, we have tested the POWHEG BOX reweighting feature. This procedure works fine for every kinematic distributions we have examined, but for the ones most sensitive to the CP nature of the X_0 boson. In fact, we have observed that it works if the reweighting is done from one distribution to another, with values of the mixing angle α not very different from each other.

Acknowledgements P.N. acknowledges support from Fondazione Cariplo and Regione Lombardia, Grant 2017-2070, and from INFN. We thank S. Frixione and F. Maltoni for useful discussions. We thank A. Grijsan for suggesting the process we implemented.

Data Availability Statement This manuscript has no associated data or the data will not be deposited. [Authors' comment: There are no associated data to our paper.]

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit <http://creativecommons.org/licenses/by/4.0/>.
Funded by SCOAP³.

References

1. S. Frixione, Z. Kunszt, A. Signer, Three jet cross-sections to next-to-leading order. *Nucl. Phys. B* **467**, 399 (1996). [https://doi.org/10.1016/0550-3213\(96\)00110-1](https://doi.org/10.1016/0550-3213(96)00110-1). arXiv:hep-ph/9512328
2. S. Catani, M.H. Seymour, A general algorithm for calculating jet cross-sections in NLO QCD. *Nucl. Phys. B* **485**, 291 (1997). [https://doi.org/10.1016/S0550-3213\(96\)00589-5](https://doi.org/10.1016/S0550-3213(96)00589-5). [https://doi.org/10.1016/S0550-3213\(98\)81022-5](https://doi.org/10.1016/S0550-3213(98)81022-5). arXiv:hep-ph/9605323
3. S. Frixione, B.R. Webber, Matching NLO QCD computations and parton shower simulations. *JHEP* **06**, 029 (2002). <https://doi.org/10.1088/1126-6708/2002/06/029>. arXiv:hep-ph/0204244
4. P. Nason, A new method for combining NLO QCD with shower Monte Carlo algorithms. *JHEP* **11**, 040 (2004). <https://doi.org/10.1088/1126-6708/2004/11/040>. arXiv:hep-ph/0409146
5. S. Frixione, P. Nason, C. Oleari, Matching NLO QCD computations with Parton Shower simulations: the POWHEG method. *JHEP* **11**, 070 (2007). <https://doi.org/10.1088/1126-6708/2007/11/070>. arXiv:0709.2092
6. S. Jadach, W. Placzek, S. Sapeta, A. Siódmok, M. Skrzypek, Matching NLO QCD with parton shower in Monte Carlo scheme—the KrkNLO method. *JHEP* **10**, 052 (2015). [https://doi.org/10.1007/JHEP10\(2015\)052](https://doi.org/10.1007/JHEP10(2015)052). arXiv:1503.06849
7. S. Alioli, C.W. Bauer, C.J. Berggren, A. Hornig, F.J. Tackmann, C.K. Vermilion et al., Combining higher-order resummation with multiple NLO calculations and parton showers in GENEVA. *JHEP* **09**, 120 (2013). [https://doi.org/10.1007/JHEP09\(2013\)120](https://doi.org/10.1007/JHEP09(2013)120). arXiv:1211.7049
8. L. Lönnblad, S. Prestel, Merging multi-leg NLO matrix elements with parton showers. *JHEP* **03**, 166 (2013). [https://doi.org/10.1007/JHEP03\(2013\)166](https://doi.org/10.1007/JHEP03(2013)166). arXiv:1211.7278
9. J. Alwall, R. Frederix, S. Frixione, V. Hirschi, F. Maltoni, O. Mattelaer et al., The automated computation of tree-level and next-to-leading order differential cross sections, and their matching to parton shower simulations. *JHEP* **07**, 079 (2014). [https://doi.org/10.1007/JHEP07\(2014\)079](https://doi.org/10.1007/JHEP07(2014)079). arXiv:1405.0301
10. F. Cascioli, P. Maierhofer, S. Pozzorini, Scattering amplitudes with open loops. *Phys. Rev. Lett.* **108**, 111601 (2012). <https://doi.org/10.1103/PhysRevLett.108.111601>. arXiv:1111.5206
11. G. Cullen, N. Greiner, G. Heinrich, G. Luisoni, P. Mastrolia, G. Ossola et al., Automated one-loop calculations with GoSam. *Eur. Phys. J. C* **72**, 1889 (2012). <https://doi.org/10.1140/epjc/s10052-012-1889-1>. arXiv:1111.2034
12. S. Actis, A. Denner, L. Hofer, J.-N. Lang, A. Scharf, S. Uccirati, RECOLA: REcursive Computation of One-Loop Amplitudes. *Comput. Phys. Commun.* **214**, 140 (2017). <https://doi.org/10.1016/j.cpc.2017.01.004>. arXiv:1605.01090
13. C. Berger, Z. Bern, L. Dixon, F. Febres Cordero, D. Forde, H. Ita et al., An automated implementation of on-shell methods for one-loop amplitudes. *Phys. Rev. D* **78**, 036003 (2008). <https://doi.org/10.1103/PhysRevD.78.036003>. arXiv:0803.4180
14. S. Alioli, P. Nason, C. Oleari, E. Re, A general framework for implementing NLO calculations in shower Monte Carlo programs: the POWHEG BOX. *JHEP* **06**, 043 (2010). [https://doi.org/10.1007/JHEP06\(2010\)043](https://doi.org/10.1007/JHEP06(2010)043). arXiv:1002.2581
15. T. Gleisberg, S. Hoeche, F. Krauss, A. Schaliche, S. Schumann, J.-C. Winter, SHERPA 1. alpha: a proof of concept version. *JHEP* **02**, 056 (2004). <https://doi.org/10.1088/1126-6708/2004/02/056>. arXiv:hep-ph/0311263
16. M. Bahr et al., Herwig++ Physics and Manual. *Eur. Phys. J. C* **58**, 639 (2008). <https://doi.org/10.1140/epjc/s10052-008-0798-9>. arXiv:0803.0883
17. S. Alioli, C.W. Bauer, C. Berggren, F.J. Tackmann, J.R. Walsh, Drell–Yan production at NNLL'+NNLO matched to parton showers. *Phys. Rev. D* **92**, 094020 (2015). <https://doi.org/10.1103/PhysRevD.92.094020>. arXiv:1508.01475
18. C. Degrande, C. Duhr, B. Fuks, D. Grellscheid, O. Mattelaer, T. Reiter, UFO—the universal FeynRules output. *Comput. Phys. Commun.* **183**, 1201 (2012). <https://doi.org/10.1016/j.cpc.2012.01.022>. arXiv:1108.2040
19. N.D. Christensen, C. Duhr, FeynRules—Feynman rules made easy. *Comput. Phys. Commun.* **180**, 1614 (2009). <https://doi.org/10.1016/j.cpc.2009.02.018>. arXiv:0806.4194
20. A. Alloul, N.D. Christensen, C. Degrande, C. Duhr, B. Fuks, FeynRules 2.0—a complete toolbox for tree-level phenomenol-

- ogy. Comput. Phys. Commun. **185**, 2250 (2014). <https://doi.org/10.1016/j.cpc.2014.04.012>. arXiv:1310.1921
21. C. Degrande, Automatic evaluation of UV and R2 terms for beyond the Standard Model Lagrangians: a proof-of-principle. Comput. Phys. Commun. **197**, 239 (2015). <https://doi.org/10.1016/j.cpc.2015.08.015>. arXiv:1406.3030
 22. S. Frixione, B. Fuks, V. Hirschi, K. Mawatari, H.-S. Shao, P. Sudder et al., Automated simulations beyond the Standard Model: supersymmetry. JHEP **12**, 008 (2019). [https://doi.org/10.1007/JHEP12\(2019\)008](https://doi.org/10.1007/JHEP12(2019)008). arXiv:1907.04898
 23. R. Frederix, S. Frixione, S. Prestel, P. Torrielli, On the reduction of negative weights in MC@NLO-type matching procedures. arXiv:2002.12716
 24. K. Hamilton, P. Nason, G. Zanderighi, MINLO: multi-scale improved NLO. JHEP **10**, 155 (2012). [https://doi.org/10.1007/JHEP10\(2012\)155](https://doi.org/10.1007/JHEP10(2012)155). arXiv:1206.3572
 25. K. Hamilton, P. Nason, C. Oleari, G. Zanderighi, Merging H/W/Z + 0 and 1 jet at NLO with no merging scale: a path to parton shower + NNLO matching. JHEP **05**, 082 (2013). [https://doi.org/10.1007/JHEP05\(2013\)082](https://doi.org/10.1007/JHEP05(2013)082). arXiv:1212.4504
 26. K. Hamilton, P. Nason, E. Re, G. Zanderighi, NNLOPS simulation of Higgs boson production. JHEP **10**, 222 (2013). [https://doi.org/10.1007/JHEP10\(2013\)222](https://doi.org/10.1007/JHEP10(2013)222). arXiv:1309.0017
 27. P.F. Monni, P. Nason, E. Re, M. Wiesemann, G. Zanderighi, MiNNLO_{PS}: a new method to match NNLO QCD to parton showers. JHEP **05**, 143 (2020). [https://doi.org/10.1007/JHEP05\(2020\)143](https://doi.org/10.1007/JHEP05(2020)143). arXiv:1908.06987
 28. P.F. Monni, E. Re, M. Wiesemann, MiNNLO_{PS}: Optimizing 2 → 1 hadronic processes. arXiv:2006.04133
 29. R. Frederix, S. Frixione, Merging meets matching in MC@NLO. JHEP **12**, 061 (2012). [https://doi.org/10.1007/JHEP12\(2012\)061](https://doi.org/10.1007/JHEP12(2012)061). arXiv:1209.6215
 30. S. Alioli, C.W. Bauer, C. Berggren, F.J. Tackmann, J.R. Walsh, S. Zuberi, Matching fully differential NNLO calculations and parton showers. JHEP **06**, 089 (2014). [https://doi.org/10.1007/JHEP06\(2014\)089](https://doi.org/10.1007/JHEP06(2014)089). arXiv:1311.0286
 31. S. Höche, Y. Li, S. Prestel, Drell–Yan lepton pair production at NNLO QCD with parton showers. Phys. Rev. D **91**, 074015 (2015). <https://doi.org/10.1103/PhysRevD.91.074015>. arXiv:1405.3607
 32. T. Ježo, P. Nason, On the treatment of resonances in next-to-leading order calculations matched to a parton shower. JHEP **12**, 065 (2015). [https://doi.org/10.1007/JHEP12\(2015\)065](https://doi.org/10.1007/JHEP12(2015)065). arXiv:1509.09071
 33. R. Frederix, S. Frixione, A.S. Papanastasiou, S. Prestel, P. Torrielli, Off-shell single-top production at NLO matched to parton showers. JHEP **06**, 027 (2016). [https://doi.org/10.1007/JHEP06\(2016\)027](https://doi.org/10.1007/JHEP06(2016)027). arXiv:1603.01178
 34. J.M. Campbell, R. Ellis, R. Frederix, P. Nason, C. Oleari, C. Williams, NLO Higgs boson production plus one and two jets using the POWHEG BOX, MadGraph4 and MCFM. JHEP **07**, 092 (2012). [https://doi.org/10.1007/JHEP07\(2012\)092](https://doi.org/10.1007/JHEP07(2012)092). arXiv:1202.5475
 35. G. Luisoni, P. Nason, C. Oleari, F. Tramontano, $H W^\pm / H Z + 0$ and 1 jet at NLO with the POWHEG BOX interfaced to GoSam and their merging within MiNLO. JHEP **10**, 083 (2013). [https://doi.org/10.1007/JHEP10\(2013\)083](https://doi.org/10.1007/JHEP10(2013)083). arXiv:1306.2542
 36. G. Luisoni, C. Oleari, F. Tramontano, $W b \bar{b} j$ production at NLO with POWHEG+MiNLO. JHEP **04**, 161 (2015). [https://doi.org/10.1007/JHEP04\(2015\)161](https://doi.org/10.1007/JHEP04(2015)161). arXiv:1502.01213
 37. T. Ježo, J.M. Lindert, P. Nason, C. Oleari, S. Pozzorini, An NLO+PS generator for $t\bar{t}$ and $W t$ production and decay including non-resonant and interference effects. Eur. Phys. J. C **76**, 691 (2016). <https://doi.org/10.1140/epjc/s10052-016-4538-2>. arXiv:1607.04538
 38. R. Frederix, S. Frixione, V. Hirschi, D. Pagani, H.-S. Shao, M. Zaro, The automation of next-to-leading order electroweak calculations. JHEP **07**, 185 (2018). [https://doi.org/10.1007/JHEP07\(2018\)185](https://doi.org/10.1007/JHEP07(2018)185). arXiv:1804.10017
 39. V. Hirschi, R. Frederix, S. Frixione, M.V. Garzelli, F. Maltoni, R. Pittau, Automation of one-loop QCD corrections. JHEP **05**, 044 (2011). [https://doi.org/10.1007/JHEP05\(2011\)044](https://doi.org/10.1007/JHEP05(2011)044). arXiv:1103.0621
 40. G. Ossola, C.G. Papadopoulos, R. Pittau, Reducing full one-loop amplitudes to scalar integrals at the integrand level. Nucl. Phys. B **763**, 147 (2007). <https://doi.org/10.1016/j.nuclphysb.2006.11.012>. arXiv:hep-ph/0609007
 41. P. Mastrolia, E. Mirabella, T. Peraro, Integrand reduction of one-loop scattering amplitudes through Laurent series expansion. JHEP **06**, 095 (2012). [https://doi.org/10.1007/JHEP11\(2012\)128](https://doi.org/10.1007/JHEP11(2012)128). arXiv:1203.0291
 42. G. Passarino, M. Veltman, One loop corrections for e^+e^- annihilation into $\mu^+\mu^-$ in the Weinberg model. Nucl. Phys. B **160**, 151 (1979). [https://doi.org/10.1016/0550-3213\(79\)90234-7](https://doi.org/10.1016/0550-3213(79)90234-7)
 43. A.I. Davydychev, A simple formula for reducing Feynman diagrams to scalar integrals. Phys. Lett. B **263**, 107 (1991). [https://doi.org/10.1016/0370-2693\(91\)91715-8](https://doi.org/10.1016/0370-2693(91)91715-8)
 44. A. Denner, S. Dittmaier, Reduction schemes for one-loop tensor integrals. Nucl. Phys. B **734**, 62 (2006). <https://doi.org/10.1016/j.nuclphysb.2005.11.007>. arXiv:hep-ph/0509141
 45. G. Ossola, C.G. Papadopoulos, R. Pittau, CutTools: a program implementing the OPP reduction method to compute one-loop amplitudes. JHEP **03**, 042 (2008). <https://doi.org/10.1088/1126-6708/2008/03/042>. arXiv:0711.3596
 46. T. Peraro, Ninja: automated integrand reduction via Laurent expansion for one-loop amplitudes. Comput. Phys. Commun. **185**, 2771 (2014). <https://doi.org/10.1016/j.cpc.2014.06.017>. arXiv:1403.1229
 47. V. Hirschi, T. Peraro, Tensor integrand reduction via Laurent expansion. JHEP **06**, 060 (2016). [https://doi.org/10.1007/JHEP06\(2016\)060](https://doi.org/10.1007/JHEP06(2016)060). arXiv:1604.01363
 48. A. Denner, S. Dittmaier, L. Hofer, Collier: a fortran-based Complex One-Loop Library in Extended Regularizations. Comput. Phys. Commun. **212**, 220 (2017). <https://doi.org/10.1016/j.cpc.2016.10.013>. arXiv:1604.06792
 49. P. de Aquino, W. Link, F. Maltoni, O. Mattelaer, T. Stelzer, ALOHA: automatic libraries of helicity amplitudes for Feynman diagram computations. Comput. Phys. Commun. **183**, 2254 (2012). <https://doi.org/10.1016/j.cpc.2012.05.004>. arXiv:1108.2041
 50. S. Alioli, P. Nason, C. Oleari, E. Re, NLO Higgs boson production via gluon fusion matched with shower in POWHEG. JHEP **04**, 002 (2009). <https://doi.org/10.1088/1126-6708/2009/04/002>. arXiv:0812.0578
 51. F. Demartin, F. Maltoni, K. Mawatari, B. Page, M. Zaro, Higgs characterisation at NLO in QCD: CP properties of the top-quark Yukawa interaction. Eur. Phys. J. C **74**, 3065 (2014). <https://doi.org/10.1140/epjc/s10052-014-3065-2>. arXiv:1407.5089
 52. P. Artoisenet et al., A framework for Higgs characterisation. JHEP **11**, 043 (2013). [https://doi.org/10.1007/JHEP11\(2013\)043](https://doi.org/10.1007/JHEP11(2013)043). arXiv:1306.6464
 53. F. Maltoni, K. Mawatari, M. Zaro, Higgs characterisation via vector-boson fusion and associated production: NLO and parton-shower effects. Eur. Phys. J. C **74**, 2710 (2014). <https://doi.org/10.1140/epjc/s10052-013-2710-5>. arXiv:1311.1829
 54. F. Demartin, F. Maltoni, K. Mawatari, M. Zaro, Higgs production in association with a single top quark at the LHC. Eur. Phys. J. C **75**, 267 (2015). <https://doi.org/10.1140/epjc/s10052-015-3475-9>. arXiv:1504.00611
 55. F. Demartin, B. Maier, F. Maltoni, K. Mawatari, M. Zaro, tWH associated production at the LHC. Eur. Phys. J. C **77**, 34 (2017). <https://doi.org/10.1140/epjc/s10052-017-4601-7>. arXiv:1607.05862

56. R.D. Ball et al., Parton distributions with LHC data. Nucl. Phys. B **867**, 244 (2013). <https://doi.org/10.1016/j.nuclphysb.2012.10.003>. [arXiv:1207.1303](https://arxiv.org/abs/1207.1303)
57. M. Whalley, D. Bourilkov, R. Group, The Les Houches accord PDFs (LHAPDF) and LHAGLUE. In: HERA and the LHC: A Workshop on the Implications of HERA and LHC Physics (Startup Meeting, CERN, 26–27 March 2004; Midterm Meeting, CERN, 11–13 October 2004), pp. 575–581 (2005). [arXiv:hep-ph/0508110](https://arxiv.org/abs/hep-ph/0508110)
58. A. Buckley, J. Ferrando, S. Lloyd, K. Nordström, B. Page, M. Rüfenacht et al., LHAPDF6: parton density access in the LHC precision era. Eur. Phys. J. C **75**, 132 (2015). <https://doi.org/10.1140/epjc/s10052-015-3318-8>. [arXiv:1412.7420](https://arxiv.org/abs/1412.7420)
59. M. Cacciari, G.P. Salam, G. Soyez, The anti- k_t jet clustering algorithm. JHEP **04**, 063 (2008). <https://doi.org/10.1088/1126-6708/2008/04/063>. [arXiv:0802.1189](https://arxiv.org/abs/hep-ph/0802.1189)
60. M. Cacciari, G.P. Salam, G. Soyez, FastJet User Manual. Eur. Phys. J. C **72**, 1896 (2012). <https://doi.org/10.1140/epjc/s10052-012-1896-2>. [arXiv:1111.6097](https://arxiv.org/abs/1111.6097)
61. K. Hagiwara, Q. Li, K. Mawatari, Jet angular correlation in vector-boson fusion processes at hadron colliders. JHEP **07**, 101 (2009). <https://doi.org/10.1088/1126-6708/2009/07/101>. [arXiv:0905.4314](https://arxiv.org/abs/0905.4314)
62. V. Del Duca, W. Kilgore, C. Oleari, C. Schmidt, D. Zeppenfeld, Gluon fusion contributions to H + 2 jet production. Nucl. Phys. B **616**, 367 (2001). [https://doi.org/10.1016/S0550-3213\(01\)00446-1](https://doi.org/10.1016/S0550-3213(01)00446-1). [arXiv:hep-ph/0108030](https://arxiv.org/abs/hep-ph/0108030)
63. V. Del Duca, W. Kilgore, C. Oleari, C. Schmidt, D. Zeppenfeld, Higgs + 2 jets via gluon fusion. Phys. Rev. Lett. **87**, 122001 (2001). <https://doi.org/10.1103/PhysRevLett.87.122001>. [arXiv:hep-ph/0105129](https://arxiv.org/abs/hep-ph/0105129)
64. T. Plehn, D.L. Rainwater, D. Zeppenfeld, Determining the structure of Higgs couplings at the LHC. Phys. Rev. Lett. **88**, 051801 (2002). <https://doi.org/10.1103/PhysRevLett.88.051801>. [arXiv:hep-ph/0105325](https://arxiv.org/abs/hep-ph/0105325)
65. G. Klamke, D. Zeppenfeld, Higgs plus two jet production via gluon fusion as a signal at the CERN LHC. JHEP **04**, 052 (2007). <https://doi.org/10.1088/1126-6708/2007/04/052>. [arXiv:hep-ph/0703202](https://arxiv.org/abs/hep-ph/0703202)
66. J.R. Andersen, K. Arnold, D. Zeppenfeld, Azimuthal angle correlations for Higgs boson plus multi-jet events. JHEP **06**, 091 (2010). [https://doi.org/10.1007/JHEP06\(2010\)091](https://doi.org/10.1007/JHEP06(2010)091). [arXiv:1001.3822](https://arxiv.org/abs/1001.3822)
67. F. Campanario, M. Kubocz, D. Zeppenfeld, Gluon-fusion contributions to Φ + 2 jet production. Phys. Rev. D **84**, 095025 (2011). <https://doi.org/10.1103/PhysRevD.84.095025>. [arXiv:1011.3819](https://arxiv.org/abs/1011.3819)
68. C. Englert, M. Spannowsky, M. Takeuchi, Measuring Higgs CP and couplings with hadronic event shapes. JHEP **06**, 108 (2012). [https://doi.org/10.1007/JHEP06\(2012\)108](https://doi.org/10.1007/JHEP06(2012)108). [arXiv:1203.5788](https://arxiv.org/abs/1203.5788)
69. C. Englert, D. Goncalves-Netto, K. Mawatari, T. Plehn, Higgs quantum numbers in weak boson fusion. JHEP **01**, 148 (2013). [https://doi.org/10.1007/JHEP01\(2013\)148](https://doi.org/10.1007/JHEP01(2013)148). [arXiv:1212.0843](https://arxiv.org/abs/1212.0843)
70. M.J. Dolan, P. Harris, M. Jankowiak, M. Spannowsky, Constraining CP-violating Higgs sectors at the LHC using gluon fusion. Phys. Rev. D **90**, 073008 (2014). <https://doi.org/10.1103/PhysRevD.90.073008>. [arXiv:1406.3322](https://arxiv.org/abs/1406.3322)
71. V. Hankele, G. Klamke, D. Zeppenfeld, T. Figy, Anomalous Higgs boson couplings in vector boson fusion at the CERN LHC. Phys. Rev. D **74**, 095001 (2006). <https://doi.org/10.1103/PhysRevD.74.095001>. [arXiv:hep-ph/0609075](https://arxiv.org/abs/hep-ph/0609075)
72. A.V. Gritsan, J. Roskes, U. Sarica, M. Schulze, M. Xiao, Y. Zhou, New features in the JHU generator framework: constraining Higgs boson properties from on-shell and off-shell production. Phys. Rev. D **102**(5), 056022 (2020). <https://doi.org/10.1103/PhysRevD.102.056022>
73. R. Frederix, K. Hamilton, Extending the MINLO method. JHEP **05**, 042 (2016). [https://doi.org/10.1007/JHEP05\(2016\)042](https://doi.org/10.1007/JHEP05(2016)042). [arXiv:1512.02663](https://arxiv.org/abs/1512.02663)