

1                   **ASSESSING THE RELIABILITY OF ELASTIC GEOBAROMETRY METHODS**

2  
3                   Bonazzi<sup>1,\*</sup>, Tumiati<sup>2</sup>, Thomas<sup>3</sup>, Angel<sup>1</sup>, Alvaro<sup>1</sup>

4                   <sup>1</sup>Department of Earth and Environmental Sciences, University of Pavia, Italy

5                   <sup>2</sup>Department of Earth and, University of Milan, Italy

6                   <sup>3</sup>Department of Earth Sciences, Syracuse University, Syracuse, NY 13244, USA

7  
8                   *For submission to: **Lithos***

9                   *Corresponding author: [matteo.alvaro@unipv.it](mailto:matteo.alvaro@unipv.it)*

10  
11  
12                   **Abstract**

13                   Elastic geobarometry makes use of the contrast in elastic proprieties between host inclusion pairs to  
14                   determine entrapment conditions for the inclusions. The theoretical basis has been developed extensively  
15                   in the past few years, but an experimental validation and assessment of the calculated P and T of entrapment  
16                   is still required. We report Raman measurements of quartz inclusions trapped in almandine garnet at  
17                   eclogitic conditions in a piston cylinder apparatus, from which we determined the stress state in the  
18                   inclusions by two methods. The use of a hydrostatic calibration of the 464cm<sup>-1</sup> line of quartz leads to a large  
19                   spread in inclusion ‘pressure’ values for inclusions trapped at 3 GPa, although it is more accurate for  
20                   inclusions trapped at 2.5 GPa. Entrapment pressures calculated via this method can be up to 0.8 GPa in  
21                   error. The use of the mode Grüneisen tensors of quartz enables the full strain state and thus the stress state  
22                   of the inclusion to be determined, and leads to a much smaller spread in mean stress values inferred for  
23                   inclusions, and the calculated entrapment pressures differ from the known experimental values by less than  
24                   0.2 GPa. These results show that the most significant effect of the elastic anisotropy of quartz is on the  
25                   Raman shifts of the inclusion, and not on the subsequent calculation of entrapment conditions.

## 1. INTRODUCTION

26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50

Elastic geobarometry makes use of the contrast in elastic proprieties between host inclusion pairs to determine entrapment pressures for the inclusions. When a host-inclusion pair is exhumed from depth to the Earth's surface non-lithostatic stresses are developed in the inclusion because of the contrast in their elastic properties [Angel et al. \(2015\)](#). Current models for elastic geobarometry only can only be applied to the simple case of elastically isotropic host-inclusion pairs with ideal geometries consisting of a small inclusion trapped in an effectively infinite host [Angel et al. \(2015\)](#). Recent work on elastic geobarometric methods allow us to calculate strains from the Raman shifts of multiple Raman-active bands (Murri et al. 2018). Furthermore, the correct analysis for the shape of the inclusion and the geometry of the inclusion has been developed and discussed by [Mazzucchelli et al. \(2018\)](#) and Campomenosi et al. (2018). The elastic anisotropy of the inclusion can also be included following the approach proposed [by Mazzucchelli et al. \(2019\)](#). Despite the intensive development an experimental validation to crosscheck the calculated P and T of entrapment is still required. Such validation cannot come from measurements on inclusions in natural rocks as we do not know the exact P and T of entrapment, especially when there is evidence of over-stepping of equilibrium reaction boundaries [\(e.g. Spear et al., 2014\)](#). An excellent means for this assessment can be obtained from synthetic host-inclusion pairs that can be produced with laboratory apparatus at controlled high-P and T conditions [\(e.g. Thomas and Spear, 2018\)](#).

The important criteria for such experimental verification is the choice of host-inclusion pairs that are relevant for geological applications (e.g. index mineral phases in UHPM rocks) that can also be synthesized in the laboratory. We chose to work on quartz inclusions in garnet because they are very common minerals in eclogitic rocks and their elastic proprieties are relatively well-known. On the samples recovered from high P-T experiments, the inclusion pressures can be determined using Raman spectroscopy combined with knowledge of the elastic behavior of the inclusion mineral. However, there are still several open questions

51 concerning the exact method to determine “pressures” using Raman spectroscopy for inclusions, such as  
52 quartz, that are not elastically isotropic.

53  
54 In particular, for quartz inclusions the residual or remnant pressure ( $P_{inc}$ ) can be determined in two different  
55 ways. One method (e.g. [Enami et al., 2007](#); [Ashley et al., 2016](#); [Thomas and Spear, 2018](#)) is to interpret the  
56 shifts of the  $464\text{ cm}^{-1}$  Raman mode of inclusions toward higher wavenumbers as a “pressure” using the  
57 calibration of [Schmidt and Ziemann \(2000\)](#). However, their calibration is obtained from hydrostatic  
58 experiments, assuming that the Raman shifts are caused solely by compression of a crystal immersed in a  
59 hydrostatic fluid. However, this is not correct for anisotropic inclusions such as quartz, trapped in other  
60 minerals. If quartz is trapped in a cubic host such as garnet the inclusion will be subject to isotropic strains  
61 imposed by the host and therefore, because it is elastically anisotropic, it will develop deviatoric stresses.  
62 The change in the Raman band positions of a mineral is determined by the strain imposed on it ([Grüneisen,](#)  
63 [1926](#); [Barron et al., 1980](#); [Cantrell, 1980](#); [Angel et al., 2019](#)), and therefore an inclusion crystal will exhibit  
64 different Raman shifts from a free crystal subject to hydrostatic pressure. The strains on a quartz inclusion  
65 crystal can be determined from the observed Raman shifts by using the mode Grüneisen tensors for quartz  
66 ([Murri et al., 2018](#); [Angel et al., 2019](#); [Murri et al., 2019](#)). In this study we synthesised quartz inclusions in  
67 almandine garnet at known pressures and temperatures and measured their Raman spectra. We calculated  
68 the inclusion pressures both via the strains (*c.f.* [Murri et al., 2018](#)), and by using the hydrostatic calibration  
69 of [Schmidt and Ziemann \(2000\)](#). From these residual inclusion pressures we calculated the entrapment  
70 pressures using Eosfit-Pinc ([Angel et al., 2017](#)) and compared them to the known synthesis conditions, in  
71 order to show the effect of the elastic anisotropy of quartz on the calculation of residual or remnant pressures  
72 and consequently of entrapment pressures.

73  
74  
75  
76  
77

## 2. METHODS

### 2.1. Piston-cylinder experiments

78 Quartz inclusions in almandine garnet are the results of hydrothermal synthesis in the piston cylinder  
79 apparatus at Syracuse University Laboratory. The experiments were performed at 3GPa and 775°C and  
80 2.5GPa and 800 °C, typical eclogitic conditions, with run times between 72 and 96 hours. As starting  
81 materials we used an oxide mix of following composition: SiO<sub>2</sub> (amorphous), Al (OH)<sub>3</sub>, FeO, Fe<sub>3</sub>O<sub>4</sub>, Fe<sub>2</sub>O<sub>3</sub>,  
82 FeTiO<sub>3</sub>, and MnO (Alfa Aesar). Details of the oxide mixture are given in the supplementary material (Table  
83 s1). In order to ensure excess silica was present, the oxide mixture corresponded to the composition of  
84 almandine plus 24% excess silica. An equal volume of distilled water was added to wet the oxide mixture  
85 completely following the protocol of [Thomas and Spear \(2018\)](#), and approximately 10-15 mg of mixed  
86 oxides were loaded into silver capsules for each experiment. We used the capsule design of [Trail et al.](#)  
87 [\(2012\)](#) in which the silver capsule of 12.7mm of diameter is formed by two identical parts separated by a  
88 platinum disk (150µm thick) placed between the open ends of the half capsules. One half-capsule contained  
89 the oxide mixture, and the second contained an FMQ buffer assemblage [\(see Fig 1 in Thomas and Spear,](#)  
90 [2018\)](#). We left headspace in both parts of the capsule to avoid contaminating the tops of capsules with their  
91 contents. The cell assembly used in these experiments is the salt-pyrex-graphite with MgO filler design of  
92 [Holland \(1980\)](#). Temperature was measured with D-type thermocouples (W<sub>97</sub>Re<sub>3</sub>–W<sub>75</sub>Re<sub>25</sub>), situated close  
93 to the top of the capsule and was considered accurate to within ~ 10 °C. The pressures in the piston–cylinder  
94 hydraulic rams were measured with Enerpac 140 MPa Bourdon-tube gauges with 18-cm-diameter dials.  
95 Experiments were cold pressurized to the desired run pressure followed by ramping the temperature at  
96 100°C/minute. Runs were quenched to below 100 °C in less than 60 s by turning off the furnace power.  
97 Pressure calibration of the piston cylinder is based on the quartz–coesite phase boundary [\(Boyd and](#)  
98 [England, 1960; Kitahara and Kennedy, 1964\)](#), using the same assemblies as our experiments. Here we  
99 describe the results from two experiments, Alm-1 (T=775°C, P=3GPa) and Alm-2 (T=800°C P=2.5GPa).

100

## 101 2.2 Sample quality assessment

102

103 After quenching the runs the capsule were opened and successful runs were found to contain a mixture of  
104 free single crystals of garnet, and also other minerals, immersed in water. Single crystals were removed

105 from the capsules and the garnet crystals were mounted in epoxy and polished by removing less than 10µm  
106 of garnet material. After polishing the garnet crystals from 60 to 100 µm in diameter (Fig. 1a and 1e). We  
107 selected quartz inclusions by optical microscopy and selected only ideal inclusions to measure with Raman  
108 spectroscopy. An ideal inclusion has to be isolated in a fracture-free garnet host, whose radius must be at  
109 least three times larger than that of the inclusion (Zhang, 1998; Mazzucchelli et al., 2018). Samples were  
110 also inspected using back scattered electron (BSE) and characterized by electron microprobe analyses and  
111 maps using a JEOL JXA 8200 Superprobe equipped with five wavelength-dispersive (WDS)  
112 spectrometers, an energy dispersive (EDS) spectrometer (accelerating potential 15 kV, beam current 15nA),  
113 at the Department of Earth Sciences, University of Milan. The phase assemblages of Alm-1 and Alm-2 are  
114 identical and show many similarities to some natural HP mineral assemblages, and consist of garnet, quartz,  
115 kyanite and ilmenite. The composition of the garnet crystals is almost pure almandine (>99%). Inclusions  
116 in garnet were quartz, rutile, kyanite and rarely orthopyroxene or ilmenite. Kyanite inclusions were mostly  
117 found as small inclusions in the cores of the garnets. The quartz inclusions range from sub-micrometer  
118 spherical inclusions to well-faceted inclusions 15µm in maximum dimension. We observed that the garnet  
119 crystals in Alm-1 are slightly larger than those in Alm-2 (see Fig. 1). Quartz included in the garnet hosts of  
120 Alm-2 are commonly smaller and more numerous than quartz included in the garnet host of Alm-1.

### 121 2.3 Raman spectroscopy measurements

122 The inclusions were measured using parallel-polarized Raman spectra in backscattering geometry with a  
123 Horiba Jobin-Yvon T64000 triple-monochromator spectrometer (spectral resolution of  $\sim 2\text{ cm}^{-1}$ ,  
124 instrumental accuracy in peak positions of  $\sim 0.35\text{ cm}^{-1}$  and 1µm spot size) with a 532nm green laser. All of  
125 the measurements have been carried out at 20°C and room pressure. As standard we used a band of a silicon  
126 metal standard whose theoretical peak position is  $520.7\text{ cm}^{-1}$ . We collected Raman spectra over several  
127 days, and several times each day we measured the Raman spectrum of a free quartz crystal to have a  
128 reference spectrum in order to have good control over instrumental uncertainties and stability.

129 Raman spectra were acquired with a laser spot of 1µm from the center of inclusions because this is the  
130 point where the stress and strain is least disturbed by the shape of the inclusion (Campomenosi et al., 2018).

131 We measured several inclusions in a single garnet host and on some inclusions we repeated the  
132 measurement over several days to estimate the reproducibility of the measurements. Overall, we collected  
133 data on more than 20 inclusions per experiment. All inclusion spectra were acquired for 5 acquisitions of  
134 40 seconds each. Raman spectra were fitted using a B-spline as a baseline correction and pseudo-Voigt  
135 peak functions with the OriginPro 2018b software. The estimated uncertainties on fitted peak positions  
136 were commonly  $< 0.3$  cm. On the quartz included in the almandine we measured the wavenumber shifts  
137 of quartz inclusions relative to the line positions of a free quartz crystal at room temperature (see tables 1a  
138 and 1b). We generally used the shift of three bands of quartz at 128, 206, 464  $\text{cm}^{-1}$  because these bands can  
139 be easily resolved from those of almandine.

140

141

142

### 3. RESULTS AND DISCUSSION

143

#### 3.1 Raman wavenumber shift, inclusion pressure and strain

144

145

146

147

148

149

The residual or remnant pressure can be calculated from the Raman spectra collected on quartz inclusions while still trapped in garnet following different procedures. The most widely used in literature is simply based on the shift of one single Raman band as a function of external pressure (e.g. Enami et al., 2007; Ashley et al., 2016; Thomas and Spear, 2018). For the sole purposes of comparison, we calculated the inclusion pressure ( $P_{inc}^{464}$ ) on the selected inclusion adopting the hydrostatic calibration by Schmidt and Ziemann (2000) for the Raman shift of the 464  $\text{cm}^{-1}$  band using the following equation:

$$P_{inc}^{464} \text{ (MPa)} = 0.36079 \cdot [(\Delta\omega_P)_{464}]^2 + 110.86 \cdot (\Delta\omega_P)_{464} \quad (1)$$

150

151

152

153

154

After fitting of the micro-Raman spectra, the wavenumber shifts have been calculated with respect to the wavenumbers obtained from repeated measurements of the reference quartz crystal in air used as standard. In Fig. 2 the  $P_{inc}^{464}$  calculated from all of our measurements on the samples retrieved from both experimental synthesis conditions (see Tables 3a and 3b) are compared with the  $P_{inc}$  calculated from the known

155 entrapment conditions from the isotropic host-inclusion model for spherical inclusions (Angel et al., 2014;  
156 Angel et al., 2017). This model ignores the effects of the elastic anisotropy on the variation of the inclusion  
157 volume with  $P$  and  $T$ , and the effects of anisotropy on the mutual elastic relaxation of the host and the  
158 inclusion. The discrepancy between the  $P_{inc}^{464}$  measured and the expected  $P_{inc}$  calculated for our synthesis  
159 conditions are smaller than 0.2 GPa for the experiment at 2.5GPa and 800°C whereas for the experiment at  
160 3GPa and 775°C the maximum discrepancy is about 0.7 GPa (see Fig. 2b). These discrepancies arise mostly  
161 from the incorrect assumption of perfectly hydrostatic conditions for an anisotropic inclusion trapped in a  
162 cubic host. Therefore, it is intuitive to understand that the deviations increase with increasing the  
163 encapsulation pressures.

164 We used the same Raman measurements to calculate the strain state ( $\varepsilon_1$  and  $\varepsilon_3$ ) of the inclusion via  
165 the mode Grüneisen tensors of quartz (Murri et al., 2019) using the Strainman software (Angel et al., 2019).  
166 As shown in Fig. 3 in Murri et al. (2018) the slopes of the iso-shift lines for the Raman bands that can be  
167 measured on quartz inclusions trapped in almandine garnet are almost parallel to one another and are nearly  
168 parallel to the isochors. As consequence the correlation between the values of  $\varepsilon_1$  and  $\varepsilon_3$  obtained in this way  
169 is very high (90-99%). The correlation makes it extremely difficult to determine a unique combination of  
170 strains from the measured stresses, and the small differences in Raman peak positions measured from a  
171 series of inclusions trapped under the same conditions leads to a spread in strains that lies sub-parallel to  
172 the isochors (Fig. 3). To minimize the effects of this correlation we performed a series of tests to select the  
173 most reliable bands (at least 3 bands) to be used in the calculations of the strain components. As no  
174 significant improvement has been observed using different combination of bands (128, 206, 264, 464, 696,  
175 1162  $\text{cm}^{-1}$ ) with the correlations always greater than 90%, we restricted our analyses to the three bands with  
176 consistently small instrumental and fitting uncertainties, i.e. those at 128, 206 and 464  $\text{cm}^{-1}$ .  
177 From the determined strain components, we calculated normal stress components ( $\sigma_1=\sigma_2$  and  $\sigma_3$ ) using the  
178 elastic tensor of Wang et al. (2015). From the calculated stresses on the inclusion we calculate the  $P_{inc}^{strains}$   
179 as the mean stress,  $(2\sigma_1+\sigma_3)/3$ . As shown by Wang et al. (2015) the elastic moduli of quartz increase non-

180 linearly with pressure. For small strains the change in elastic moduli is very small compared to the  
181 magnitude of the elastic tensor components at room pressure. Calculations performed with the experimental  
182 elasticity tensor at 1.5 GPa overestimates the  $P_{inc}$  by about 20-24% with respect the calculation using the  
183 tensor at room pressure. We therefore carried out the analyses using the elastic tensor at room pressure.  
184 With this calculation the discrepancy between the measured  $P_{inc}^{strains}$  and the theoretical  $P_{inc}$  calculated with  
185 the isotropic model from our synthesis conditions are smaller than 0.1 GPa (Table 3 and Fig. 2). As shown  
186 in Fig. 2b no significant improvement has been observed in the distribution of the residual pressures for the  
187 inclusions from the low-pressure experiment (Alm-2). They are similar to the deviations obtained from the  
188 calculations based on only the shift of the 464 $cm^{-1}$  line. Conversely for the high-P experiment (Alm-1),  
189 while the deviation from the expected residual pressures using the strain method remains identical to that  
190 of the low-P runs, the deviations for the values calculated using the 464 line are more than 7 times larger  
191 (e.g. up to 0.7 GPa). These results clearly show that the incorrect estimates of  $P_{inc}$  obtained by using the  
192 hydrostatic calibration of the 464  $cm^{-1}$  line become worse at higher inclusion pressures.

193

### 194 3.2 Calculation of entrapment conditions

195 From the residual or remnant pressures obtained by the two approaches we calculated inclusion entrapment  
196 pressures using non-linear equations of state (EoS) of the host and the inclusion minerals using the EoSFit-  
197  $P_{inc}$  software (Angel et al., 2017). The following results are based on the isotropic model for both the  
198 relaxation and the thermodynamic calculation (see Angel et al., 2014; Angel et al., 2017 for details). As  
199 could be expected from the results shown in Fig. 2, the  $P_{trap}^{strains}$  (Fig. 4) are in good agreement with the  
200 experimental pressures of synthesis for both experiments. In we show the results together with a confidence  
201 interval of  $\pm 0.2$ GPa (shaded area in Fig. 4) that provides an indication of the magnitude of uncertainties  
202 on these results calculated from the uncertainties in volume strain ( $V_s = 2\varepsilon_1 + \varepsilon_3$ ) at entrapment conditions.  
203 On the other hand, the values of  $P_{trap}^{464}$ , which are derived from the hydrostatic calibration of the Raman  
204 shifts, only agree with the experimental synthesis conditions for the experiment at 2.5 GPa (Fig. 4b). For



205 the experiment at 3 GPa, although some of the  $P_{trap}^{464}$  values are correct, the maximum discrepancy is about  
206 1.2 GPa (Fig. 4a). This spread in pressure is far greater than the expected uncertainties. The difference  
207 between  $P_{trap}$  calculated using the two approaches is greater for the inclusions whose strains deviate most  
208 from those expected for hydrostatic stress (yellow area in Fig. 3), indicating that the source of the errors in  
209  $P_{trap}^{464}$  comes from ignoring the non-hydrostatic stresses in the inclusions.

210

211

#### 4. CONCLUSIONS

212 Prior to this study, it was not clear how the elastic anisotropy of quartz might affect the estimates of  $P_{trap}$   
213 of inclusions based on a hydrostatic and isotropic model. There are two contributions from elastic  
214 anisotropy to this question. The first is that the Raman shifts of a crystal are determined by the strains and  
215 not the pressure or mean stress (e.g. Barron et al., 1982; Angel et al., 2019). Therefore, the Raman shifts  
216 from solid anisotropic inclusions such as quartz inside a cubic host mineral such as garnet are not the same  
217 as those for a quartz crystal under hydrostatic conditions. Second, the anisotropic stresses and the  
218 anisotropic elastic properties will modify both the calculation of the elastic relaxation of the host-inclusion  
219 system, and the calculation of the  $P_{trap}$  from the  $P_{inc}$  (Alvaro et al., 2019; Mazzucchelli et al., 2019). Our  
220 experimental results, summarised in Fig. 2 and 3, clearly show that the  $P_{inc}$  values inferred from the  
221 hydrostatic calibration of the shift of the 464 Raman line are in substantial error when the inclusions are  
222 subject to strains that are significantly different from those of a crystal under hydrostatic stress (Fig. 3).  
223 Therefore, the determination of  $P_{inc}$  as a mean stress derived from the strains based on the measurement of  
224 several Raman lines is much more reliable. Second, the fact that our calculated  $P_{trap}^{strains}$  values based on  
225 these measured  $P_{inc}^{strains}$  are in good agreement with the experimental pressure of synthesis indicates that  
226 the effects of the elastic anisotropy of quartz on the calculation from  $P_{inc}$  to  $P_{trap}$  is smaller than the other  
227 experimental uncertainties.

228 Therefore, in order to obtain reliable estimates of  $P_{trap}$  of quartz inclusions, a number of steps are required.

229 First, it is important to select approximately spherical inclusions for which the shape effects are small and

230 can be corrected (Mazzucchelli et al., 2018). Second, the inclusions must be isolated. Table 3 shows that  
231 partially-exposed inclusions (e.g. Grt2\_I2) have partially-released stresses (Campomenosi et al., 2018;  
232 Mazzucchelli et al., 2018) and the resulting  $P_{\text{trap}}$  values can be up to 0.8 GPa too small for inclusions  
233 entrapped in our experiments at 3 GPa. On the other hand, inclusions that are close to other inclusions (e.g.  
234 Grt6\_I1 in Table 3a) can exhibit inclusion stresses that are higher than isolated inclusions, and thus give  
235  $P_{\text{trap}}$  values that are significantly too high. Once suitable inclusions have been identified the Raman shifts  
236 of several Raman lines from the inclusion must be measured as precisely as possible. This requires that a  
237 reference Raman spectrum is measured at the same time with the same instrument settings from a free  
238 quartz crystal in air. The strains in the inclusion should be determined from the changes in Raman shifts by  
239 using the mode Grüneisen tensors of quartz (Murri et al., 2018; Angel et al., 2019). The  $P_{\text{inc}}$  should then be  
240 calculated from these strains as the mean stress via the room-pressure elastic tensor of quartz (e.g. Wang et  
241 al., 2015). This  $P_{\text{inc}}$  can then be used in calculations based on the isotropic model for the evolution of host-  
242 inclusion systems (e.g. Angel et al., 2017) to calculate reliable  $P_{\text{trap}}$  values. The intrinsic uncertainties and  
243 the correlation in the strains obtained in this way (e.g. Fig. 3) suggest that multiple measurements of a  
244 population of quartz inclusions trapped under the same conditions are required to obtain a statistically  
245 reliable estimate of  $P_{\text{trap}}$  (as in Fig. 4).

246

247

#### 248 **Acknowledgements:**

249 This project has received funding from the European Research Council (ERC) under the European  
250 Union's Horizon 2020 research and innovation programme (grant agreement No 714936) by M. Alvaro.  
251 MA has also been supported by the MIUR-SIR grant "MILE DEEp" (RBSI140351).

252

253

254

255

## REFERENCES

- 256  
257
- 258 Alvaro, M., Luca, M.M., John, A.R., Mara, M., Nicola, C., Marco, S., Federica, M., Andrey, K.,  
259 Marta, M., 2019. Quartz inclusions from eclogite xenoliths record past subduction. in prep.
- 260 Angel, R.J., Mazzucchelli, M.L., Alvaro, M., Nestola, F., 2017. EosFit-Pinc: A simple GUI for host-  
261 inclusion elastic thermobarometry. *American Mineralogist* 102, 1957-1960.
- 262 Angel, R.J., Mazzucchelli, M.L., Alvaro, M., Nimis, P., Nestola, F., 2014. Geobarometry from  
263 host-inclusion systems: The role of elastic relaxation. *American Mineralogist* 99, 2146-2149.
- 264 Angel, R.J., Murri, M., Mihailova, B., Alvaro, M., 2019. Stress, strain and Raman shifts. *Zeitschrift  
265 fur kristallograhie - Crystalline Material* 234, 11.
- 266 Angel, R.J., Nimis, P., Mazzucchelli, M.L., Alvaro, M., Nestola, F., 2015. How large are departures  
267 from lithostatic pressure? Constraints from host-inclusion elasticity. *Journal of Metamorphic  
268 Geology* 33, 801-813.
- 269 Ashley, K.T., Steele-MacInnis, M., Bodnar, R.J., Darling, R.S., 2016. Quartz-in-garnet inclusion  
270 barometry under fire: Reducing uncertainty from model estimates. *Geology* 44, 699-702.
- 271 Barron, T.H.K., Collins, J.F., Smith, T.W., White, G.K., 1982. Thermal expansion, Grüneisen  
272 functions and static lattice properties of quartz. *Journal of Physics C: Solid State Physics* 15,  
273 4311-4326.
- 274 Barron, T.H.K., Collins, J.G., White, G.K., 1980. Thermal expansion of solids at low temperatures.  
275 *Advances in Physics* 29, 609-730.
- 276 Boyd, F.R., England, J.L., 1960. The quartz-coesite transition. *Journal of Geophysical Research  
277 (1896-1977)* 65, 749-756.
- 278 Campomenosi, N., Mazzucchelli, M.L., Mihailova, B.D., Scambelluri, M., Angel, R.J., Nestola, F.,  
279 Reali, A., Alvaro, M., 2018. How geometry and anisotropy affect residual strain in host inclusion  
280 system: coupling experimental and numerical approaches. *American Mineralogist* 103, 2032-  
281 2035.
- 282 Cantrell, J.H., 1980. Generalized Grüneisen tensor from solid nonlinearity parameters. *Physical  
283 Review B* 21, 4191-4195.
- 284 Enami, M., Nishiyama, T., Mouri, T., 2007. Laser Raman microspectrometry of metamorphic  
285 quartz: A simple method for comparison of metamorphic pressures. *American Mineralogist* 92,  
286 1303-1315.
- 287 Grüneisen, E., 1926. Zustand des festen Körpers, in: Drucker, C., Grüneisen, E., Kohnstamm, P.,  
288 Körber, F., Scheel, K., Schrödinger, E., Simon, F., van der Waals, J.D., Henning, F. (Eds.),  
289 *Thermische Eigenschaften der Stoffe*. Springer Berlin Heidelberg, Berlin, Heidelberg, pp. 1-59.
- 290 Holland, T., 1980. The reaction albite= jadeite+ quartz determined experimentally in the range  
291 600–1200 C. *American Mineralogist* 65, 129-134.
- 292 Kitahara, S., Kennedy, G.C., 1964. The quartz-coesite transition. *Journal of Geophysical Research  
293 (1896-1977)* 69, 5395-5400.
- 294 Mazzucchelli, M.L., Burnley, P., Angel, R.J., Morganti, S., Domeneghetti, M.C., Nestola, F.,  
295 Alvaro, M., 2018. Elastic geothermobarometry: Corrections for the geometry of the host-  
296 inclusion system. *Geology* 46, 231-234.
- 297 Mazzucchelli, M.L., Morganti, S., Reali, A., Chiara Domeneghetti, M., Angel, R.J., Alvaro, M.,  
298 2019. Elastic geobarometry: relaxation of elastically anisotropic inclusions.

299 Murri, M., Alvaro, M., Angel, R.J., Prencipe, M., Mihailova, B.D., 2019. The effects of non-  
300 hydrostatic stress on the structure and properties of alpha-quartz. *Physics and Chemistry of*  
301 *Minerals*.

302 Murri, M., Mazzucchelli, M.L., Campomenosi, N., Korsakov, A.V., Prencipe, M., Mihailova, B.D.,  
303 Scambelluri, M., Angel, R.J., Alvaro, M., 2018. Raman elastic geobarometry for anisotropic  
304 mineral inclusions. *American Mineralogist* 103, 1869-1872.

305 Schmidt, C., Ziemann, M.A., 2000. In-situ Raman spectroscopy of quartz: A pressure sensor for  
306 hydrothermal diamond-anvil cell experiments at elevated temperatures. *American Mineralogist*  
307 85, 1725-1734.

308 Spear, F.S., Thomas, J.B., Hallett, B.W., 2014. Overstepping the garnet isograd: a comparison of  
309 QuiG barometry and thermodynamic modeling. *Contributions to Mineralogy and Petrology* 168,  
310 1059.

311 Thomas, J.B., Spear, F.S., 2018. Experimental study of quartz inclusions in garnet at pressures  
312 up to 3.0 GPa: evaluating validity of the quartz-in-garnet inclusion elastic thermobarometer.  
313 *Contributions to Mineralogy and Petrology* 173.

314 Trail, D., Bruce Watson, E., Tailby, N.D., 2012. Ce and Eu anomalies in zircon as proxies for the  
315 oxidation state of magmas. *Geochimica et Cosmochimica Acta* 97, 70-87.

316 Wang, J., Mao, Z., Jiang, F., Duffy, T.S., 2015. Elasticity of single-crystal quartz to 10 GPa. *Physics*  
317 *and Chemistry of Minerals* 42, 203-212.

318 Zhang, Y., 1998. Mechanical and phase equilibria in inclusion–host systems. *Earth and Planetary*  
319 *Science Letters* 157, 209-222.

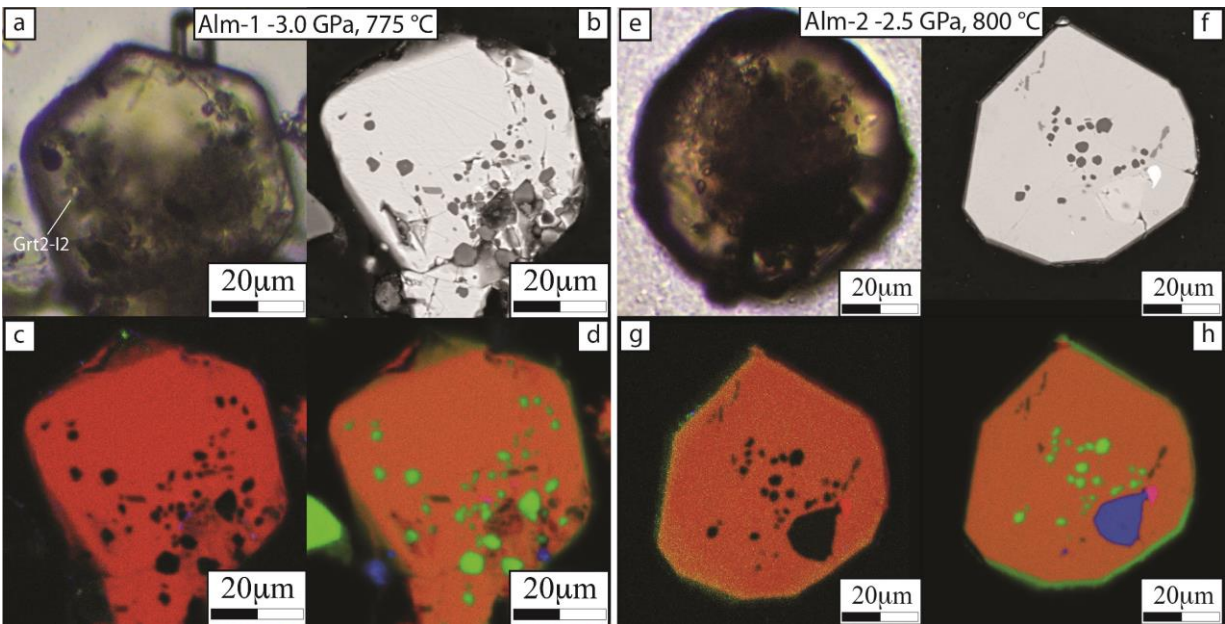
320

321

322

## Figures

323



**Fig. 1.** Optical microphotographs and SEM-BSE image of the samples Alm-1 synthesized at 3.0GPa and 775°C and Alm-2 synthesized at 2.5GPa and 800°C.

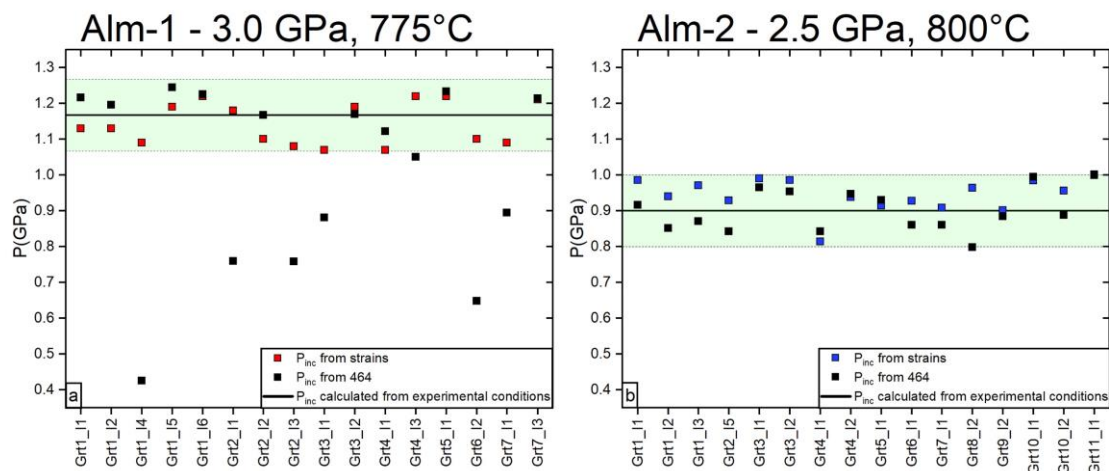
(a,e) In optical microphotographs the garnets appear to be euhedral with several trapped inclusions. (b,f) Inclusions exposed on the surface are visible in the SEM-BSE images and therefore have not been used for further analyses. (c,g) The combined Fe-Mg-Ca chemical element maps in RGB show that almandine garnet is very homogeneous. (d,h) The combined Fe-Si-Ti chemical element maps in RGB show the different inclusion phases with quartz in green, rutile in blue and in pyroxene in pink.

324

325

326

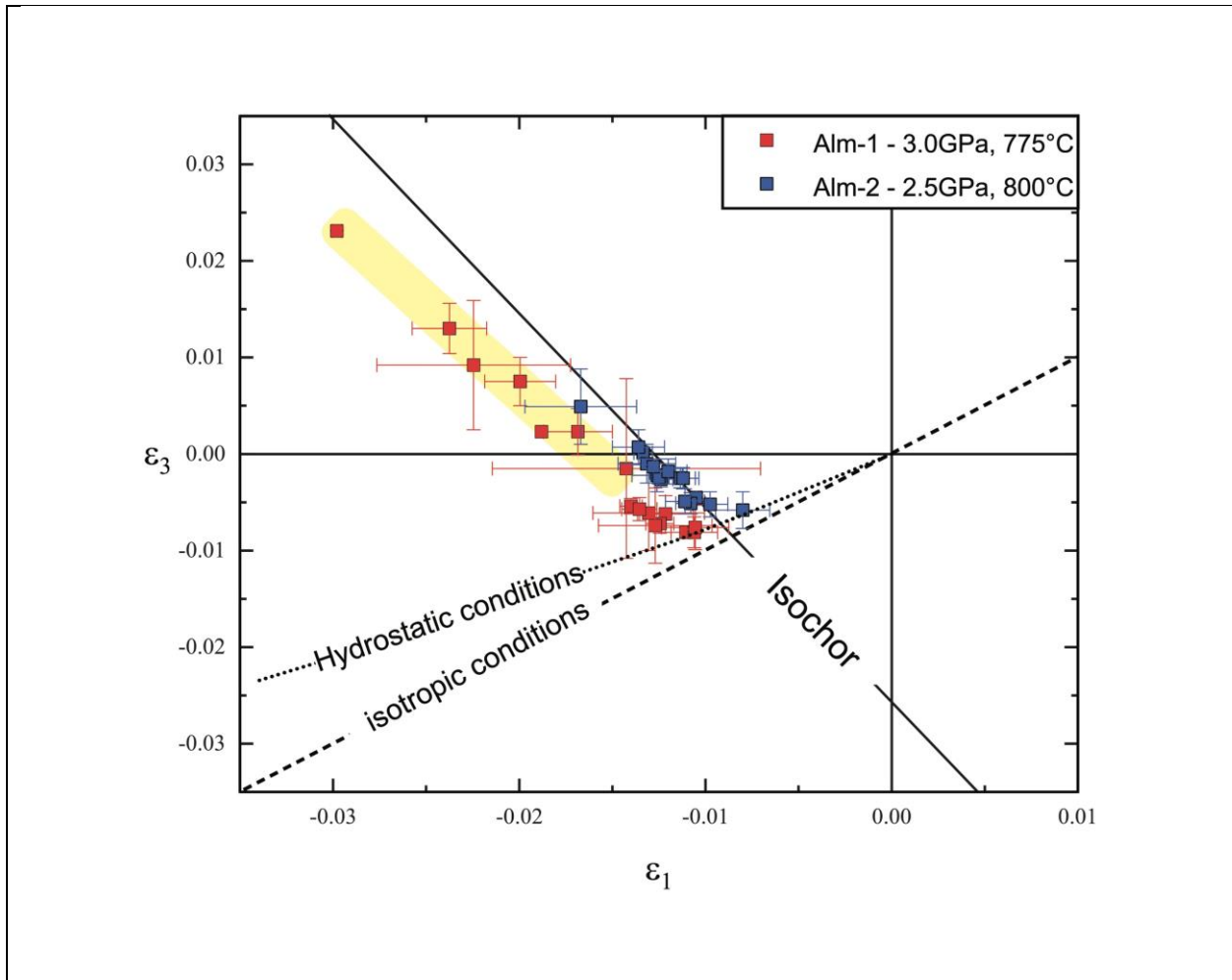
327



**Fig. 2.** Inclusion pressures calculated for the quartz inclusion in garnet from synthesis at 3.0 GPa (a, Alm-1) and 2.5GPa (b, Alm-2). The black line represents the inclusion pressure ( $P_{inc}$ ) calculated from the synthesis conditions for quartz trapped in almandine garnet with the isotropic host-inclusion model, and the green shaded area represents the maximum allowed discrepancy following the uncertainties of the calculation.  $P_{inc}$  calculated using the hydrostatic calibration ( $P_{inc}^{464}$ , *black squares*) from the shift of the 464 Raman band show a much larger discrepancy than those obtained from the strain components ( $P_{inc}^{strains}$ , *red squares*) for experiment at 3.0GPa (Alm-1). Much closer agreement between the two approaches has been obtained for the experiments at 2.5GPa (Alm-2, blue squares in part b).

328

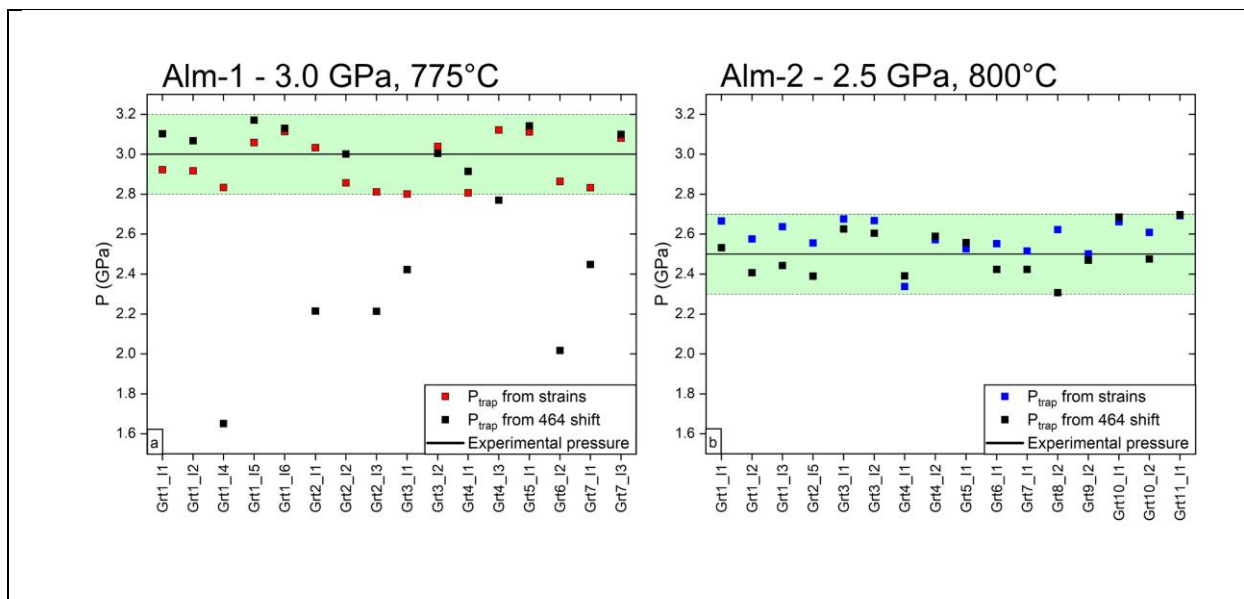
329



**Fig. 3.** Strain components determined at room temperature for quartz inclusions from experiments Alm-1 (red squares) and Alm-2 (blue squares). Lines for hydrostatic conditions (dotted), for isotropic conditions (dashed) and an isochor (filled) are also shown. The strains from both experiments lie almost parallel to the isochor and are clustered close to, but clearly above, the strains for hydrostatic conditions. The spread in values for the 2.5GPa experiment is much smaller than that for the inclusions synthesised at 3.0GPa. The yellow area indicates the inclusions in Alm-1 that have discrepancies in  $P_{inc}^{464}$  larger than the experimental uncertainties (Fig. 2a).

330

331



**Fig. 4.** Entrapment pressures calculated on the quartz inclusion in garnet synthesised at 3.0 GPa (a, Alm-1) and 2.5GPa (b, Alm-2). The black line represents the experimental pressure ( $P_{trap}$ ) of the synthesis conditions for quartz trapped in almandine garnet and the green shaded area represents the maximum estimated uncertainty propagated through the calculation of  $P_{trap}$ . The uncertainty of the calibration of the piston cylinder is less than 0.02 GPa.  $P_{trap}^{strains}$  obtained from  $P_{trap}^{464}$  are represented by red squares and are in good agreement with experimental entrapment pressures for both experiments (Alm-1 and Alm-2).  $P_{trap}^{464}$  (black squares) calculated from  $P_{inc}^{464}$  showed a good agreement in the experiments at lower pressure and much larger spread in values in the experiment at higher pressure (Alm-1 3.0 GPa). The  $P_{trap}^{464}$  values outside the uncertainty band are from the inclusions highlighted in yellow in Fig. 3.



334

335

Tables

**Table 1a.** Raman peak positions and wavenumber shifts for quartz inclusions in garnet from experimental runs at 3.0 GPa and 775°C.

ALM1

date	hosts	inclusions	wave numbers $\omega(\text{cm}^{-1})$				wave number shifts $\Delta\omega (\text{cm}^{-1})$				
			128 $\square(\text{cm}^{-1})$	e.s.d.	206 ( $\text{cm}^{-1}$ )	e.s.d.	464 ( $\text{cm}^{-1}$ )	e.s.d.	128 ( $\text{cm}^{-1}$ )	206 ( $\text{cm}^{-1}$ )	464 ( $\text{cm}^{-1}$ )
<b>ideal inclusions</b>											
05-12-18		I1	133.868	0.059	232.416	0.167	475.302	0.015	6.25	25.463	10.6
12-06-18		I2	132.878	0.266	231.051	0.36	474.503	0.041	5.643	25.089	10.432
12-06-18	<b>Grt1</b>	I4	128.542	0.467	225.754	1.124	467.863	0.045	1.307	19.792	3.791
12-06-18		I5	133.722	0.171	232.654	0.296	474.918	0.034	6.487	26.692	10.846
12-06-18		I6	133.528	0.419	232.917	0.635	474.75	0.086	6.293	26.955	10.679
12-06-18		I1	131.968	0.306	229.953	0.861	470.771	0.058	4.733	23.992	6.699
05-12-18	<b>Grt2</b>	I2	133.908	0.098	231.747	0.319	474.897	0.027	6.29	24.793	10.196
12-06-18		I3	131.177	0.619	227.919	1.181	470.769	0.07	3.942	21.957	6.697
05-12-18		I1	133.855	0.161	230.241	0.42	472.453	0.027	6.237	23.287	7.751
05-12-18	<b>Grt3</b>	I2	134.292	0.056	233.304	0.163	474.911	0.073	6.674	26.35	10.209
12-06-18		I1	133.432	0.238	230.139	0.251	473.876	0.021	6.197	24.177	9.804
12-06-18	<b>Grt4</b>	I3	132.264	0.289	231.796	0.461	473.271	0.073	5.029	25.834	9.199
05-12-18	<b>Grt5</b>	I1	134.655	0.055	234.24	0.113	475.452	0.014	7.037	27.287	10.751
12-06-18	<b>Grt6</b>	I2	130.461	0.324	227.636	0.954	469.815	0.043	3.226	21.674	5.743
27-11-18		I1	132.75	0.098	228.93	0.141	472.781	0.012	4.765	22.968	7.871
27-11-18	<b>Grt7</b>	I3	134.328	0.09	232.656	0.295	475.499	0.032	6.343	26.694	10.589
<b>not-ideal inclusions</b>											
12-06-18	<b>Grt1</b>	I2	131.534	0.376	223.81	0.691	471.938	0.039	4.299	17.848	7.867
12-06-18		I4	133.826	0.121	230.239	0.268	474.144	0.022	6.208	23.285	9.442
12-06-18	<b>Grt2</b>	I2	131.239	0.879	233.673	0.682	473.886	0.133	4.004	27.711	9.815
12-06-18		I1	131.388	0.808	235.222	1.13	471.412	0.133	4.153	29.26	7.34
12-06-18	<b>Grt6</b>	I3	132.091	0.161	225.545	0.934	472.481	0.041	4.856	19.583	8.409
12-06-18		I4	132.084	0.147	227.818	0.488	471.818	0.024	4.849	21.856	7.747
12-06-18		I2	134.341	0.101	234.468	0.225	475.36	0.029	6.356	28.506	10.451
12-06-18	<b>Grt7</b>	I4	134.111	0.305	233.13	0.26	474.523	0.035	6.126	27.169	9.613

Note: Wavenumber shifts and their e.s.d.'s have been obtained as described in the text. Not-ideal inclusions cannot be used to calculate the entrapment pressure.

**Table 1b.** Raman peak positions and wavenumber shifts for quartz inclusions in garnet from experimental runs at 2.5 GPa and 800°C.

date	hosts	inclusions	wave numbers $\omega(\text{cm}^{-1})$				wave number shifts $\Delta\omega(\text{cm}^{-1})$				
			128 (cm <sup>-1</sup> )	e.s.d.	206 (cm <sup>-1</sup> )	e.s.d.	464 (cm <sup>-1</sup> )	e.s.d.	128 (cm <sup>-1</sup> )	206 (cm <sup>-1</sup> )	464 (cm <sup>-1</sup> )
<b>ideal inclusions</b>											
07-12-18		I1	132.774	0.041	228.331	0.088	472.838	0.008	4.904	21.448	8.057
08-12-18	<b>Grt1</b>	I2	131.907	0.042	226.990	0.080	472.279	0.006	4.037	20.107	7.498
09-12-18		I3	132.572	0.060	227.852	0.186	472.449	0.012	4.703	20.968	7.667
13-06-18	<b>Grt2</b>	I5	131.705	0.102	227.078	0.224	472.206	0.017	3.737	19.767	7.416
05-12-18	<b>Grt3</b>	I1	132.511	0.058	228.470	0.183	473.254	0.019	4.641	21.587	8.473
05-12-18		I2	132.481	0.059	228.348	0.214	473.160	0.017	4.611	21.464	8.379
07-12-18	<b>Grt4</b>	I1	132.591	0.042	225.216	0.070	472.205	0.008	4.721	18.333	7.423
07-12-18		I2	132.723	0.032	227.654	0.117	473.099	0.008	4.853	20.770	8.318
07-12-18	<b>Grt5</b>	I1	132.854	0.042	227.263	0.053	472.951	0.006	4.985	20.380	8.170
05-12-18	<b>Grt6</b>	I1	132.413	0.047	227.041	0.234	472.357	0.015	4.543	20.158	7.576
07-12-18	<b>Grt7</b>	I1	132.377	0.058	226.707	0.137	472.359	0.010	4.508	19.824	7.578
13-06-18	<b>Grt8</b>	I2	130.914	0.209	227.137	1.184	471.827	0.046	2.946	19.826	7.037
22-11-18	<b>Grt9</b>	I2	132.164	0.162	226.978	0.273	472.572	0.021	4.196	19.667	7.782
22-11-18		I1	133.222	0.067	229.171	0.283	473.518	0.024	5.254	21.860	8.728
22-11-18	<b>Grt10</b>	I2	132.391	0.079	227.980	0.249	472.598	0.066	4.422	20.669	7.808
22-11-18	<b>Grt11</b>	I1	133.301	0.043	229.476	0.156	473.573	0.017	5.332	22.164	8.783
<b>not-ideal inclusions</b>											
13-06-18	<b>Grt2</b>	I4	131.462	0.165	226.831	0.278	472.199	0.019	3.493	19.520	7.409
13-06-18		I7	130.954	0.059	222.136	0.098	470.469	0.011	2.986	14.825	5.679
07-12-18	<b>Grt4</b>	I2	133.604	0.063	230.322	0.152	473.950	0.017	5.734	23.438	9.169
07-12-18		I3	133.370	0.050	229.798	0.119	474.289	0.010	5.500	22.915	9.508
05-12-18	<b>Grt6</b>	I2	133.223	0.050	229.927	0.150	473.721	0.014	5.353	23.044	8.940
22-11-18	<b>Grt9</b>	I1	132.809	0.227	230.383	0.534	474.276	0.050	4.841	23.072	9.486
22-11-18		I3	133.353	0.115	230.690	0.355	473.992	0.033	5.384	23.379	9.202
22-11-18	<b>Grt10</b>	I3	133.431	0.083	229.832	0.086	473.803	0.008	5.462	22.520	9.013
22-11-18	<b>Grt11</b>	I2	132.998	0.047	229.855	0.158	473.749	0.013	5.029	22.544	8.959

Note: Wavenumber shifts and their e.s.d.'s have been obtained as described in the text. Not-ideal inclusions cannot be used to calculate the entrapment pressure.

**Table 2a.** Calculated strains for quartz inclusions in garnet from experimental runs at 3.0 GPa and 775°C.

	date	host	inclusion	$\epsilon_{1+\epsilon_2}$	e.s.d.	$\epsilon_3$	e.s.d.	$\epsilon_V$	e.s.d.	Covariance (x10 <sup>6</sup> )	Correlation (%)	$\chi^2$
<b>ALM1</b>	<b>ideal inclusions</b>											
	05-12-18		I1	-0.0221	0.0004	-0.0081	0.0003	-0.0302	0.0002	-0.12	-99	0.00
	12-06-18		I2	-0.0243	0.0030	-0.0062	0.0019	-0.0305	0.0011	-5.64	-99	0.12
	12-06-18	<b>Gr1</b>	I4	-0.0596	0.0005	0.0231	0.0003	-0.0365	0.0002	-0.14	-99	0.00
	12-06-18		I5	-0.0249	0.0015	-0.0072	0.0010	-0.0322	0.0006	-1.38	-99	0.03
	12-06-18		I6	-0.0280	0.0012	-0.0054	0.0008	-0.0333	0.0005	-0.95	-99	0.02
	12-06-18		I1	-0.0449	0.0104	0.0092	0.0067	-0.0358	0.0039	-69.35	-99	1.44
	05-12-18	<b>Gr2</b>	I2	-0.0212	0.0025	-0.0081	0.0016	-0.0293	0.0009	-3.97	-99	0.08
	12-06-18		I3	-0.0399	0.0038	0.0075	0.0025	-0.0324	0.0014	-9.43	-99	0.20
	05-12-18	<b>Gr3</b>	I1	-0.0285	0.0144	-0.0015	0.0093	-0.0300	0.0054	-	-99	2.77
	05-12-18		I2	-0.0261	0.0060	-0.0061	0.0039	-0.0322	0.0022	-22.75	-99	0.47
	12-06-18	<b>Gr4</b>	I1	-0.0211	0.0036	-0.0076	0.0023	-0.0287	0.0013	-8.28	-99	0.17
	12-06-18		I3	-0.0376	0.0000	0.0023	0.0000	-0.0353	0.0000	0.00	-99	0.00
	05-12-18	<b>Gr5</b>	I1	-0.0254	0.0061	-0.0074	0.0039	-0.0328	0.0023	-23.45	-99	0.49
	12-06-18	<b>Gr6</b>	I2	-0.0475	0.0040	0.0130	0.0026	-0.0345	0.0015	-10.22	-99	0.21
	27-11-18	<b>Gr7</b>	I1	-0.0337	0.0037	0.0023	0.0024	-0.0314	0.0014	-8.57	-99	0.18
27-11-18		I3	-0.0271	0.0019	-0.0057	0.0012	-0.0328	0.0007	-2.27	-99	0.05	
<b>not-ideal inclusions</b>												
12-06-18	<b>Gr1</b>	I2	-0.01341	0.00261	-0.00712	0.00168	-0.02053	0.00097	-4.35	-99	0.09	
12-06-18	<b>Gr2</b>	I4	-0.01916	0.00509	-0.00807	0.00329	-0.02723	0.00189	-16.55	-99	0.34	
12-06-18	<b>Gr4</b>	I2	-0.04741	0.00908	0.00734	0.00586	-0.04007	0.00338	-52.71	-99	1.1	
12-06-18		I1	-0.06742	0.00627	0.01991	0.00405	-0.04751	0.00233	-25.13	-99	0.52	
12-06-18	<b>Gr6</b>	I3	-0.01527	0.00072	-0.00741	0.00046	-0.02268	0.00027	-0.33	-99	0.01	
12-06-18		I4	-0.02906	0.00421	0.0001	0.00272	-0.02896	0.00157	-11.36	-99	0.24	
12-06-18	<b>Gr7</b>	I2	-0.0358	0.00384	-0.00135	0.00248	-0.03714	0.00143	-9.41	-99	0.2	
12-06-18		I4	-0.03574	0.00599	-0.00014	0.00387	-0.03588	0.00223	-22.98	-99	0.48	

Note: Values calculated using strainman software ([Angel et al 2018](#)) as described in the text. Not-ideal inclusions cannot be used to calculate the entrapment pressure.

**Table 2b.** Calculated strains for quartz inclusions in garnet from experimental runs at 2.5 GPa and 800°C. Values calculated using strainman software as described in the text.

	date	host	inclusion	$\epsilon_{1+\epsilon_2}$	e.s.d.	$\epsilon_3$	e.s.d.	$\epsilon_V$	e.s.d.	Covariance (x10 <sup>6</sup> )	Correlation (%)	$\chi^2$
<b>ALM2</b>	<b>ideal inclusions</b>											
	07-12-18		I1	-0.0252	0.0027	-0.0022	0.0017	-0.0274	0.0010	-4.52	-99	0.09
	08-12-18	<b>Grt1</b>	I2	-0.0267	0.0010	0.0001	0.0006	-0.0267	0.0004	-0.62	-99	0.01
	09-12-18		I3	-0.0263	0.0031	-0.0010	0.0020	-0.0273	0.0012	-6.19	-99	0.13
	13-06-18	<b>Grt2</b>	I5	-0.0272	0.0028	0.0007	0.0018	-0.0265	0.0010	-4.95	-99	0.1
	05-12-18	<b>Grt3</b>	I1	-0.0248	0.0013	-0.0026	0.0008	-0.0275	0.0005	-1.05	-99	0.02
	05-12-18		I2	-0.0250	0.0011	-0.0024	0.0007	-0.0274	0.0004	-0.70	-99	0.01
	07-12-18	<b>Grt4</b>	I1	-0.0160	0.0029	-0.0058	0.0019	-0.0217	0.0011	-5.51	-99	0.11
	07-12-18		I2	-0.0210	0.0005	-0.0045	0.0003	-0.0255	0.0002	-0.15	-99	0
	07-12-18	<b>Grt5</b>	I1	-0.0195	0.0019	-0.0052	0.0013	-0.0247	0.0007	-2.39	-99	0.05
	05-12-18	<b>Grt6</b>	I1	-0.0240	0.0020	-0.0018	0.0013	-0.0259	0.0008	-2.65	-99	0.06
07-12-18	<b>Grt7</b>	I1	-0.0227	0.0016	-0.0025	0.0010	-0.0252	0.0006	-1.59	-99	0.03	
13-06-18	<b>Grt8</b>	I2	-0.0334	0.0060	0.0049	0.0039	-0.0285	0.0022	-23.22	-99	0.48	
22-11-18	<b>Grt9</b>	I2	-0.0224	0.0017	-0.0025	0.0011	-0.0250	0.0006	-1.91	-99	0.04	
22-11-18	<b>Grt10</b>	I1	-0.0216	0.0016	-0.0051	0.0011	-0.0267	0.0006	-1.72	-99	0.04	
22-11-18		I2	-0.0256	0.0003	-0.0013	0.0002	-0.0268	0.0001	-0.05	-99		
22-11-18	<b>Grt11</b>	I1	-0.0222	0.0021	-0.0049	0.0013	-0.0272	0.0008	-2.70	-99	0.06	
<b>not-ideal inclusions</b>												
13-06-18	<b>Grt2</b>	I4	-0.0273	0.0045	0.0010	0.0029	-0.0263	0.0017	-13.17	-99	0.27	
13-06-18		I7	-0.0188	0.0015	-0.0006	0.0010	-0.0194	0.0006	-1.40	-99	0.03	
07-12-18	<b>Grt4</b>	I2	-0.0237	0.0035	-0.0051	0.0022	-0.0288	0.0013	-7.67	-99	0.16	
07-12-18		I3	-0.0206	0.0003	-0.0068	0.0002	-0.0274	0.0001	-0.05	-99	0	
05-12-18	<b>Grt6</b>	I2	-0.0251	0.0019	-0.0037	0.0012	-0.0289	0.0007	-2.28	-99	0.05	
22-11-18	<b>Grt9</b>	I1	-0.0247	0.0045	-0.0041	0.0029	-0.0288	0.0017	-12.96	-99	0.27	
22-11-18		I3	-0.0250	0.0009	-0.0042	0.0006	-0.0291	0.0003	-0.50	-99	0.01	
22-11-18	<b>Grt10</b>	I3	-0.0219	0.0019	-0.0055	0.0012	-0.0274	0.0007	-2.33	-99	0.05	
22-11-18	<b>Grt11</b>	I2	-0.0244	0.0007	-0.0038	0.0005	-0.0282	0.0003	-0.32	-99	0.01	

Note: Values calculated using strainman software (Angel et al 2018) as described in the text. Not-ideal inclusions cannot be used to calculate the entrapment pressure.

**Table 3a.** Principal stress components ( $\sigma_1=\sigma_2$  and  $\sigma_3$ ), inclusion pressure (Pinc) and entrapment pressure (Ptrap) calculated for quartz inclusions in garnet from experimental runs at 3.0 GPa and 775°C.

	From 464 wavenumber shift				From strain components				
	date	hosts	inclusions	Pinc (GPa)	Ptrap(GPa)	$\sigma_1=\sigma_2$ (GPa)	$\sigma_3$ (GPa)	Pinc $\Delta\sigma$ (GPa)	Ptrap(GPa)
	ideal inclusions								
<b>ALM1</b>	05-12-18		I1	1.22	3.10	-1.13	-1.14	1.13	2.92
	12-06-18		I2	1.20	3.07	-1.21	-0.96	1.13	2.92
	12-06-18	<b>Grt1</b>	I4	0.43	1.65	-2.49	1.72	1.09	2.83
	12-06-18		I5	1.24	3.17	-1.25	-1.08	1.19	3.06
	12-06-18		I6	1.22	3.13	-1.37	-0.92	1.22	3.11
	12-06-18		I1	0.76	2.22	-1.98	0.42	1.18	3.03
	05-12-18	<b>Grt2</b>	I2	1.17	3.00	-1.09	-1.12	1.10	2.86
	12-06-18		I3	0.76	2.21	-1.77	0.30	1.08	2.81
	05-12-18	<b>Grt3</b>	I1	0.88	2.42	-1.35	-0.51	1.07	2.80
	05-12-18		I2	1.17	3.00	-1.29	-0.97	1.19	3.04
	12-06-18	<b>Grt4</b>	I1	1.12	2.91	-1.08	-1.07	1.07	2.81
	12-06-18		I3	1.05	2.77	-1.72	-0.22	1.22	3.12
	05-12-18	<b>Grt5</b>	I1	1.23	3.14	-1.28	-1.10	1.22	3.11
	12-06-18	<b>Grt6</b>	i2	0.65	2.018	-2.05	0.80	1.10	2.86
	27-11-18	<b>Grt7</b>	I1	0.89	2.448	-1.54	-0.18	1.09	2.83
	27-11-18		I3	1.21	3.1	-1.34	-0.95	1.21	3.08
	not-ideal inclusions								
	12-06-18	<b>Grt1</b>	I2	0.89	2.466	-0.71	-0.92	0.78	2.24
12-06-18	<b>Grt2</b>	I4	1.08	2.815	-0.99	-1.10	1.03	2.71	
12-06-18	<b>Grt4</b>	I2	1.12	2.917	-2.12	0.19	1.35	3.40	
12-06-18		I1	0.83	2.352	-2.90	1.28	1.51	3.76	
12-06-18	<b>Grt6</b>	I3	0.96	2.588	-0.80	-0.98	0.86	2.39	
12-06-18		I4	0.88	2.44	-1.35	-0.35	1.02	2.69	
12-06-18	<b>Grt7</b>	I2	1.20	3.066	-1.69	-0.59	1.32	3.34	
12-06-18		I4	1.10	2.856	-1.67	-0.46	1.27	3.21	

Note: Principal stress components have been calculated using the full elastic tensor by Wang et al. (2015) as described in the text. Values of  $P_{inc}$  have been calculated from the stress components as described in the text.  $P_{trap}$  values have been calculated using EosFit-Pinc (Angel et al., 2017). Not ideal inclusions show the wrong pressure, the problems can be a lot, for example they are partially exposed or to be close the host boundary or to be close fracture.

**Table 3b** Principal stress components ( $\sigma_1=\sigma_2$  and  $\sigma_3$ ), inclusion pressure (Pinc) and entrapment pressure (Ptrap) calculated for quartz inclusions in garnet from experimental runs at 2.5 GPa and 800°C.

		From 464 wavenumber shift			From strain components			
date	hosts	inclusions	Pinc (GPa)	Ptrap(GPa)	$\sigma_1=\sigma_2$ (GPa)	$\sigma_3$ (GPa)	Pinc $\Delta\sigma$ (GPa)	Ptrap(GPa)
<b>ideal inclusions</b>								
07-12-18		I1	0.92	2.532	-1.20	-0.54	0.98	2.67
08-12-18	<b>Grt1</b>	I2	0.85	2.407	-1.25	-0.33	0.94	2.58
09-12-18		I3	0.87	2.443	-1.24	-0.43	0.97	2.64
13-06-18	<b>Grt2</b>	I5	0.84	2.39	-1.26	-0.27	0.93	2.56
05-12-18	<b>Grt3</b>	I1	0.97	2.626	-1.19	-0.59	0.99	2.68
05-12-18		I2	0.95	2.605	-1.19	-0.57	0.99	2.67
07-12-18	<b>Grt4</b>	I1	0.84	2.391	-0.82	-0.81	0.81	2.34
07-12-18		I2	0.95	2.589	-1.04	-0.74	0.94	2.57
07-12-18	<b>Grt5</b>	I1	0.93	2.557	-0.97	-0.79	0.91	2.53
05-12-18	<b>Grt6</b>	I1	0.86	2.424	-1.14	-0.49	0.93	2.55
07-12-18	<b>Grt7</b>	I1	0.86	2.424	-1.09	-0.54	0.91	2.52
13-06-18	<b>Grt8</b>	I2	0.80	2.307	-1.50	0.11	0.96	2.62
22-11-18	<b>Grt9</b>	I2	0.88	2.47	-1.08	-0.55	0.90	2.50
22-11-18	<b>Grt10</b>	I1	1.00	2.685	-1.07	-0.81	0.98	2.66
22-11-18		I2	0.89	2.476	-1.21	-0.45	0.96	2.61
22-11-18	<b>Grt11</b>	I1	1.00	2.698	-1.10	-0.80	1.00	2.69
<b>not-ideal inclusions</b>								
13-06-18	<b>Grt2</b>	I4	0.84	2.388	-1.29	-0.44	1.01	2.71
13-06-18		I7	0.64	2.03	-0.89	-0.30	0.69	2.11
07-12-18	<b>Grt4</b>	I2	1.05	2.789	-1.17	-0.83	1.06	2.81
07-12-18		I3	1.09	2.87	-1.05	-0.97	1.02	2.74
05-12-18	<b>Grt6</b>	I2	1.02	2.734	-1.22	-0.71	1.05	2.79
22-11-18	<b>Grt9</b>	I1	1.08	2.865	-1.20	-0.74	1.05	2.80
22-11-18		I3	1.05	2.797	-1.22	-0.75	1.06	2.82
22-11-18	<b>Grt10</b>	I3	1.03	2.753	-1.09	-0.86	1.01	2.72
22-11-18	<b>Grt11</b>	I2	1.02	2.738	-1.19	-0.71	1.03	2.75

ALM2



Note: Principal stress components have been calculated using the full elastic tensor by Wang et al. (2015) as described in the text. Values of  $P_{inc}$  have been calculated from the stress components as described in the text.  $P_{trap}$  values have been calculated using EosFit-Pinc (Angel et al., 2017). Not ideal inclusions show the wrong pressure, the problems can be a lot, for example they are partially exposed or to be close the host boundary or to be close fracture.



Supplementary materials

S1 composition of oxides mixture used to synthesise garnet with quartz inclusions

starting material  
(QuiG 13-02-16)

oxide	wt%
SiO <sub>2</sub>	59,23
Al <sub>2</sub> O <sub>3</sub>	15,39
FeO	10,1
Fe <sub>2</sub> O <sub>3</sub>	8,13
TiO <sub>2</sub>	7,16

composition of buffer used to control oxygen fugacity of experiments

FMQ

oxide	wt%
SiO <sub>2</sub>	23,43
FeO	38,59
Fe <sub>3</sub> O <sub>4</sub>	37,98

1

S2 Quartz reference

	<b>DATE</b>	<b>STANDARD</b>	<b>SAMPLE</b>	<b>location</b>	<b>128 (cm<sup>-1</sup>)</b>	<b>e.s.d.</b>	<b>206 (cm<sup>-1</sup>)</b>	<b>e.s.d.</b>	<b>464 (cm<sup>-1</sup>)</b>	<b>e.s.d.</b>
<b>ALM1</b>	12-06-18	quartz thin section	THIN SECTION	eclogitic_ Fjordorf	127.235	0.038	205.962	0.046	464.072	0.016
	27-11-18	quartz thin section	THIN SECTION	granite_Ivrea Verbano Zone	127.985	0.021	207.236	0.064	464.910	0.006
	05-12-18	quartz free crystal	FREE CRYSTAL	unknow	127.617	0.026	206.954	0.066	464.702	0.006
<b>ALM2</b>	13-06-18	quartz thin section	THIN SECTION	Eclogitic_ Fjordorf	126.648	0.023	205.319	0.036	463.480	0.009
	22-11-18	quartz thin section	THIN SECTION	granite- Ivrea Verbano Zone	127.969	0.019	207.311	0.059	464.790	0.010
	05-12-18	quartz free crystal	FREE CRYSTAL	unknow	127.870	0.023	206.883	0.055	464.781	0.006

2

3

4

5  
6