

3 **Goal programming for financial portfolio management:**
4 **a state-of-the-art review**

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8 **Abstract** Over the last decades, the Goal Programming (GP) model has been
9 applied to financial portfolio management and/or selection problem in decision-
10 making contexts where several conflicting and incommensurable objectives are
11 simultaneously aggregated. The aim of this paper is to identify the research trends
12 and publication outlets for the application of GP model to portfolio management.
13 We point out an increasing interest and affirmation of more sophisticated models.
14 We present a characterization of the existing GP variants and provide historical data
15 and statistical analysis.

16
17 **Keywords** Goal programming · Financial portfolio selection · Typology
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21 1 Introduction

Author Proof

22 During the last two decades we have noticed a rapid increase of publications using
 23 different variants of the Goal Programming (GP) model for portfolio selection (Lin
 24 and O’Leary 1993; Aouni 2009, 2010; Azmi and Tamiz 2010; Aouni et al. 2014).
 25 The GP model enables the Financial Decision Maker (FDM) to aggregate several
 26 financial dimensions in order to select the best compromise portfolio. The FDM can
 27 be an investor, a portfolio manager, a financial analyst or a financial councillor. The
 28 FDM is requested to choose the appropriate GP variant to deal with a specific
 29 portfolio selection situation depending on the nature of the available information
 30 within the specific financial decision-making situation and the market performance.

31 In this paper we focus on portfolio selection and management that involve the
 32 construction of a portfolio of securities (such as stocks, bonds, treasury bills and
 33 mutual funds), that maximizes the FDM utility and accommodate his/her
 34 preferences. The conducted literature review reveals that there are at least one
 35 hundred and fifty publications applying the GP model to financial portfolio
 36 management. These publications are dealing with decision making situations in
 37 which the type of information can be (a) deterministic (ninety-two papers),
 38 (b) stochastic (twenty-nine papers), and (c) fuzzy or imprecise (thirty-four articles).
 39 The aim of this paper is to review the main theoretical developments and
 40 applications of different GP model variants to financial portfolio selection and
 41 management.

42 The paper is structured as follows: Sect. 2 provides a brief review of the most
 43 important GP variants that have been developed and applied to portfolio
 44 management and points out the advantages of each variant. Section 3, which is
 45 the core of the paper, describes how data have been collected and then classified.
 46 Section 4 is devoted to the presentation of our analysis and to the discussion of the
 47 main results. Finally, Sect. 5 concludes the paper and provides some recommen-
 48 dations for future research.

49 2 Goal programming for financial portfolio selection

50 The bi-criteria financial portfolio selection model was developed by Markowitz
 51 in (1952) and published in a fundamental paper published in the Journal of
 52 Finance. His model aggregates simultaneously the expected return and the risk of
 53 a given portfolio. These two dimensions are incommensurable since both
 54 criteria are measured through different scales and units. The security return and
 55 risk are also conflicting in a situation where high returns are correlated to high
 56 risks and vice versa. The aggregation of both dimensions requires the FDM to
 57 provide some tradeoffs (compromises) based on his/her preferences and value
 58 system.

59 The mathematical formulation of (Markowitz 1952) model reads as follows:

- 60 1. Attribute 1: The expected return of the portfolio, $\sum_{j=1}^n E_j x_j$, to be maximized,

61 2. Attribute 2: The portfolio risk, $\sum_{j=1}^n \sum_{k=1}^n x_j \sigma_{jk} x_k$, to be minimized.

62

63 Subject to:

$$\sum_{j=1}^n x_j = 1,$$

$$x \in F,$$

65 where: x_j , proportion to be invested in the security j ; E_j , expected return of security
66 j ; σ_{jk} , covariance of the returns of securities j and k ; F , set of feasible solutions.

67 The aggregation of both attributes 1 and 2 can be done either by determining the
68 minimum variance portfolio subject to an expected return E^* :

$$\text{Minimize } \sum_{i=1}^n \sum_{j=1}^n x_i \sigma_{ij} x_j$$

70 Subject to:

$$\sum_{i=1}^n E_i x_i = E^*$$

72

$$\sum_{i=1}^n x_i = 1$$

74

$$x \in F$$

76 or by maximizing the expected portfolio return subject to a maximum level of
77 sustainable and affordable risk R^* :

$$\text{Maximize } \sum_{i=1}^n E_i x_i$$

79 Subject to:

$$\sum_{i=1}^n \sum_{j=1}^n x_i \sigma_{ij} x_j \leq R^*$$

81

$$\sum_{i=1}^n x_i = 1$$

83

$$x \in F.$$

85 Since the introduction of Markowitz model, several other attempts have been
87 proposed to consider more sophisticated portfolio models able to capture more
88 investment features and improve the overall performance. In fact, empirical
89 evidence demonstrates that in order to select the best financial portfolio it is required

90 to aggregate more than two dimensions. The FDM may want to optimize
 91 simultaneously several incommensurable and conflicting attributes such as:
 92 (a) return rate; (b) risk; (c) liquidity; (d) gross book value per share; (e) capitalization
 93 ratio; and (f) stock market value of each company. Zopounidis et al. (1999)
 94 identified fifteen criteria and they grouped them into the following three categories:
 95 corporate validity; acceptability of stocks by the investors, and financial vigor.
 96 **AQ2** Within each category, five attributes have been listed (see Table 1).

97 As presented in the above Table 1, solving a portfolio selection problem requires
 98 partial or total attribute aggregation. The GP model is one of the aggregation
 99 procedures that has been widely utilized in portfolio management. Its methodolog-
 100 ical framework is based on the Distance Function (DF) model. In general the DF
 101 model aims at minimizing the following quantity

$$\sum_{i=1}^P [w_i |g_i - f_i(x)|^r]^{1/r}$$

103 that expresses the weighted sum of the Euclidean distance between g_i and $f_i(x)$ for
 104 any x belonging to the feasible set F . The coefficients w_i represent the relative
 105 importance of each objective $f_i(x)$ and r defines the family type of the Euclidean
 106 distance functions. The absolute deviation $|g_i - f_i(x)|$ measures the distance between
 107 the achievement levels $f_i(x)$ and the aspiration levels (goals) g_i . The linear formu-
 108 lation of the DF model, known as Goal Programming model, was introduced by
 109 Charnes et al. (1955) and Charnes and Cooper (1961). Their formulations are
 110 characterized by the presence of positive and negative deviations, both to be

Table 1 Different dimensions for portfolio selection

Category	Attributes
Corporate validity criteria	Gross book value per share Capitalization ratio Stock market value of each firm The marketability of each share Financial position progress
Acceptability of stocks by the investors	Dividend yield Capital gain Exchange flow ratio Round lots traded per day Transaction value per day
Financial vigor criteria	Equity ratio Price/earnings ratio Structure ratio Equity/debt ratio Return on equity

111 minimized: both underachievement and overachievement of objectives are
 112 unwanted according to the satisfying philosophy. In other words, the decision maker
 113 will penalize both positive and negative deviations.

114 The standard formulation of the GP introduced by Charnes and Cooper (1961)
 115 reads as follows:

$$\text{Min } \sum_{i=1}^n (\delta_i^- + \delta_i^+)$$

117 Subject to:

$$f_i(x) + \delta_i^- - \delta_i^+ = g_i \quad (i = 1, 2, \dots, p)$$

$$119 \quad x \in F$$

$$121 \quad \delta_i^-, \delta_i^+ \geq 0 \quad (i = 1, 2, \dots, p)$$

123 where δ_i^- and δ_i^+ are the negative and positive deviations, respectively. Since the
 124 objectives are conflicting, the obtained solution can be qualified as the solution of
 125 the best compromise or the most satisfactory solution. According to Martel and
 126 Aouni (1990) and Aouni et al. (2009), the GP model is simpler and easier to
 127 understand and to apply than other Multiple Criteria Decision Aid (MCDA) and/or
 128 Multiple Objective Programming (MOP) techniques. GP models can easily be
 129 implemented by using some powerful commercial software such as AMPL, Lingo,
 130 and CPLEX. The large number of its applications in several domains including
 131 portfolio selection demonstrates its potential and shows its applicability and
 132 effectiveness in practice. Furthermore, in Aouni et al. (2009) the authors showed
 133 that the GP model allows an explicit integration of the DM preferences and it
 134 requires limited information during the process of preference elucidation with
 135 respect to other models used within the MOP paradigm.

136 For more than 60 years, the GP model has become the most popular model in
 137 MCDA and MOP and widely implemented in financial portfolio management
 138 (Aouni et al. 2014). Indeed, different GP variants have been applied and they range
 139 from Weighted Goal Programming (WGP) to Lexicographic Goal programming
 140 (LGP), from Polynomial Goal Programming (PGP) to Stochastic Goal Programming
 141 (SGP), and finally to Fuzzy Goal Programming (FGP). The GP variants were
 142 applied according to the nature of the decision-making situation and the available
 143 information about the objective functions, decision variables and decision-making
 144 parameters (Azmi and Tamiz 2010; Aouni et al. 2014).

145 Through the WGP, the FDM may express his/her preferences by assigning
 146 weights to positive and negative deviations. Pendaraki et al. (2005); Bilbao-Terol
 147 et al. (2015) and Bravo et al. (2010) have utilized the WGP for financial portfolio
 148 selection where the relative importance of both risk and return objectives were
 149 expressed through the weights w_i^+ and w_i^- associated with positive and negative
 150 deviations, respectively. In fact the weights have a double role, namely:
 151 (a) standardization of the units and scales of measurement and (b) valorization of
 152 the Decision-Maker's preferences (Kettani et al. 2004).

153 The LGP, also known as pre-emptive GP, allows the FDM to rank the objectives
 154 according to a lexicographic order based on their relative importance. The
 155 deviations of a higher level of priority are introduced as constraints within the
 156 subsequent mathematical programs related to the objectives of lower levels of
 157 priority. As a result, the objectives in the lower priority levels play a marginal role
 158 in the decision-making process. Lee (1972) has developed the first formulation of
 159 LGP for portfolio selection. This formulation aggregated simultaneously three
 160 dimensions, namely: (a) dividends, (b) the growth of earnings; and (c) 50% dividend
 161 payout ratio. Lee and Lerro (1973) have extended Lee (1972) formulation for
 162 mutual funds and they concluded that their model allowed to obtain quite similar
 163 solutions to those resulting from Markowitz (1952, 1959) and Sharpe (1967)
 164 models. Kumar et al. (1978) applied the LGP for dual-purpose funds managed by an
 165 investment company issuing two types of shares: (a) income shares and (b) capital
 166 shares. In fact, the LGP has been widely applied in financial portfolio selection since
 167 the 1980s.

168 Incorporating skewness into the decision-making process in the context of
 169 portfolio selection may cause major change in composition of the financial portfolio
 170 comparatively to portfolio based only on the mean–variance model. The PGP model
 171 proposed by Lai (1991) allowed incorporating preferences regarding skewness and
 172 other objectives and he claimed that this model was more efficient than LGP model.
 173 In their paper, Canela and Collazo (2007) have reformulated the different PGP
 174 models proposed by Lai (1991), Chunchachinda et al. (1997), (Prakash et al. 2003)
 175 and Sun and Yan (2003) and claimed that these formulations may lead to unfeasible
 176 solutions.

177 Several financial decision-making contexts are characterized by uncertainty in
 178 which the decision-making parameters are random variables. The SGP model
 179 considers goals as stochastic values with a specific probability distribution. Our
 180 literature review reveals that several SGP formulations have been proposed for
 181 financial portfolio selection by using the notion of deterministic equivalent
 182 formulation. However, Aouni and La Torre (2010) introduced the concept of
 183 scenario generation in formulating a SGP model applied to portfolio selection.
 184 Through this model, probabilities were associated with all possible events or
 185 scenarios and the corresponding goals depended on the specific scenario based on
 186 the state of nature.

187 The FGP model was developed to deal with some financial decisional context in
 188 which the FDM can only provide vague or imprecise goal values (Arenas-Parra
 189 et al. 2001). The FGP is based on the concept of membership function that was
 190 introduced by Zimmerman (1976, 1978, 1983) and Freeling (1980) for modeling the
 191 fuzziness related to the decision-making parameters. In their paper, Bilbao et al.
 192 (2006) provided a formulation based on Sharpe (1967) model by considering
 193 ambiguous and vague parameters and calculating the betas using past observations.
 194 Their model was applied to Spanish mutual funds. Moreover, Mansour et al. (2007)
 195 formulated an imprecise GP model for portfolio selection based on the satisfaction
 196 function where the FDM preferences are explicitly incorporated into the decision-
 197 making process. Their model has been applied to Tunisian stock exchange market.

198 The goals associated with the rate of return, the liquidity and the risk were
199 considered to be imprecise and expressed through an interval-value function.

200 Several other GP variants have been applied to portfolio management over the
201 years. We can mention: the min–max GP variant (Deng et al. 2005), the interactive
202 GP model (Spronk 1980; Perez et al. 2007), the nonlinear GP model (Li and Xu
203 2007), the integer GP (Harrington and Fisher 1980) or the mixed-integer GP model
204 (Aouni et al. 2013) and its variants such as the mixed-integer stochastic GP in
205 Stoyan and Kwon (2011).

206 Recently, the Compromised Programming (CP) model was applied to portfolio
207 selection problem by Ballesteros and Romero (1996) and Ballesteros (1998). Further
208 extensions include a Fuzzy Compromised GP model (Ballesteros et al. 2007) where
209 the distance between fuzzy ideal goal values and the achievement levels were to be
210 minimized. Nowadays, the Chance Constrained Compromise Programming (CCCP)
211 model for the portfolio selection problem (Boswarva and Aouni 2012) is quite
212 popular as well. We remind that the CCCP and the SGP formulations are based on
213 the assumption that aspiration levels of objectives are normally distributed with
214 known mean and variance.

215 When the FDM implements a GP model, he/she is not passive and his/her
216 preferences and opinions can be taken into consideration in the portfolio selection
217 process. In particular, the concept of satisfaction function developed by Martel and
218 Aouni (1990) has been utilized to explicitly incorporate the FDM preferences. In
219 general, satisfaction functions are taking values in the interval $[0, 1]$. Therefore, the
220 satisfaction function gives a value of 1 when the FDM is totally satisfied with the
221 proposed solution. Otherwise, they are monotonically decreasing according to his/
222 her appreciation of the achievement level of each objective.

223 Finally, GP formulations are often combined with other methods and techniques
224 to solve multiple criteria problems: the most used are the Analytic Network Process
225 (ANP); the Decision-Making Trial and Evaluation Laboratory (DEMATEL)
226 method; and the Technique for Order of Preference by Similarity to Ideal Solution
227 (TOPSIS).

228 3 Data collection

229 For the purpose of this paper we extended the dataset of a previous survey produced
230 by Aouni et al. (2014) and deepened the analysis. The most important step in our
231 literature retrieval process was a computer search of Web of Science and Scopus
232 databases. Our search period was not temporally limited. Using the descriptors
233 “Goal Programming”, “Financial Portfolio” and “Portfolio Management”, we
234 retrieved approximately 21 (Web of science) and 136 (Scopus) abstracts to be added
235 to the 91 papers of our previous research for review. Our initial dataset accounted
236 for 248 papers.

237 Then we cleaned the database by removing duplicate rows/works. Each
238 publication was carefully reviewed before taking a decision on its inclusion in
239 this study. We excluded survey papers like Azmi and Tamiz (2010) or works that
240 did not deal with financial portfolio management. A final total of 151 outputs (see

241 **Appendix**) was considered to be acceptable for the purposes of this survey. In
 242 particular, we identified: 131 papers (87%), 3 books (2%), 5 book chapters (3%), 10
 243 conference papers (7%) and 2 working papers (1%). We classified each output
 244 according to the following categories: (a) Year of publication, (b) Journal,
 245 (c) Journal area, (d) Country/institution affiliation of the author, (e) Application
 246 area, (f) GP variants, and (g) Decision type.

247 Obviously, most of the data were available on Scopus and Web of Science. The
 248 journal area was identified according to the journal citation report. The application
 249 area was mainly identified through keywords provided by the authors themselves.
 250 For each paper we indicated the country/countries and whether this country
 251 belonged to the Organization for Economic Co-operation and Development
 252 (OECD), as a proxy for being a developed country. The institution affiliation of
 253 the author(s) was also used to describe the kind of collaboration: we were interested
 254 to identify if the output was due to an academic collaboration or a bridge
 255 collaboration with industry practitioners or governmental officials.

256 Finally, we were able to distinguish among three different families of
 257 information, namely: (a) deterministic, (b) stochastic and (c) fuzzy or imprecise.
 258 The remaining categories are self-explanatory.

259 4 Bibliographical analysis

260 This section summarizes the results and discusses the findings for each of our
 261 classified categories. As shown in Fig. 1, there is an increasing interest on the
 262 application of the GP model to financial portfolio selection. We notice ten
 263 publications in the 1970s, forty-nine papers during 2000s and fifty-eight

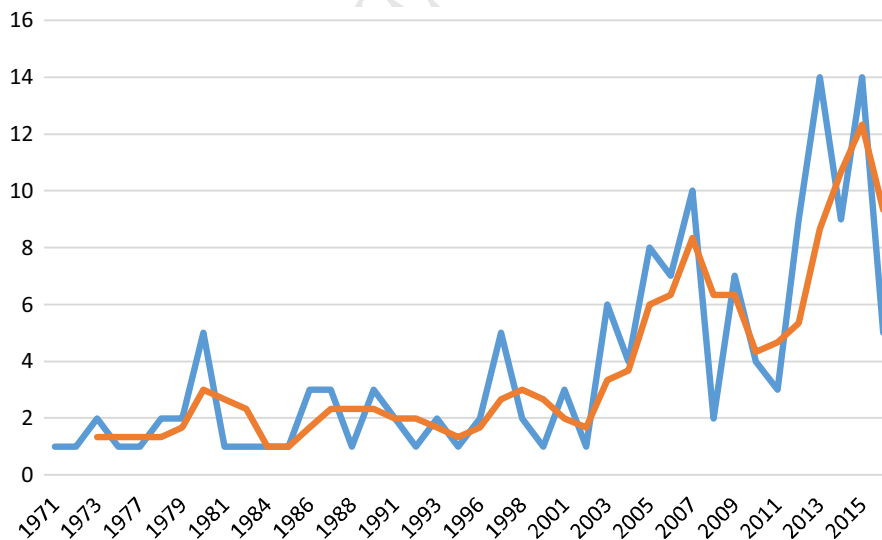


Fig. 1 Time evolution of the publications

264 publications during 2010s. The establishment of international conferences (e.g.
 265 MOPGP¹ conferences) might have impacted on this positive trend. The number of
 266 papers published in each year ranges from 1 to 14 (with an average equal to 3.8).
 267 Due to the possible time lag in reviewing and revising the submitted manuscripts
 268 and the scheduling of journal publications, it is justifiable to look at a three-year
 269 simple moving average for the publications (red line of Fig. 1). As expected, the
 270 values of the moving averages clearly confirm a steadily increasing trend.

271 Figure 2 summarizes the number of papers, related to financial portfolio selection
 272 through the GP model, by country. There are a total of 225 researchers affiliated with
 273 different institutions in 36 countries across the world. They have written an average of
 274 1.7 output thus it is a fragmented production. However, we can identify some top
 275 authors, namely A. Bilbao Terol (13), B. Aouni (12), M. Arenas Parra (10) and F. Ben
 276 Abdelaziz (10). The largest number of authors are affiliated with an American
 277 university (22.6%), followed by affiliations with Spanish (12.4%), Canadian (6.5%),
 278 Tunisian (4.8%) and British universities (4.8%). Together, these five countries (CR5)
 279 account for 51.1%, the community is slightly concentrate. There are some
 280 considerations to be done in relation to authors' affiliation: during their academic
 281 life researchers change universities and countries, in other words the same author can
 282 contribute to different 'national' productions. Moreover, a researcher can have a
 283 double affiliation and this affects the final results, and makes impossible to provide an
 284 accurate measure of the contribution of a single author/country.

285 Grouping the publications related to the application of the GP model to financial
 286 portfolio selection by continent, we found that Europe (29.8%) is the most
 287 productive continent, followed by North America (23.8%), Asia (22.5%), Africa
 288 (3.3%) and Oceania (0.7%). Our literature review revealed that there are also
 289 several intercontinental collaborations (19.9%).

290 Most papers have been written by more than one author (88.1%) and the average
 291 number of authors per paper is 2.49. As regards the degree of development of a
 292 country, we distinguished between works written by authors affiliated with an
 293 institution in a developed (OECD members) or developing countries with a dummy
 294 variable that takes value 2 when all authors work in an institution of an OECD country
 295 or a set of OECD countries (but not one or more developing countries), 1 if at least one
 296 of the authors works an institution of an OECD country and 0 otherwise. 96 of the
 297 works (63.6%) are from the 21 developed countries, and 35 (23.2%) are from the 15
 298 developing countries. Our review indicates that, 20 of the 151 research paper (13.2%)
 299 are collaborations between authors from OECD and non-OECD countries. It is clear
 300 the predominant role played by Institutions host in developed countries.

301 With regard to the type of affiliated institution, most of the papers (135 or 89.4%)
 302 were written by university professors and researchers from 129 different univer-
 303 sities, 2 (1.4%) were authored by industry practitioners and government officials,
 304 and 14 (9.3%) were jointly written by authors from both sectors. The top
 305 universities in terms of output are the University of Oviedo (13 papers), followed by
 306 Laurentian University (10 papers), Technical University of Madrid, University of
 307 Milan, University of Rhode Island, and University of Tunis (6 papers each). These

1FL01 ¹ The first MOPGP conference was held at the University of Portsmouth, United Kingdom, June, 1994.

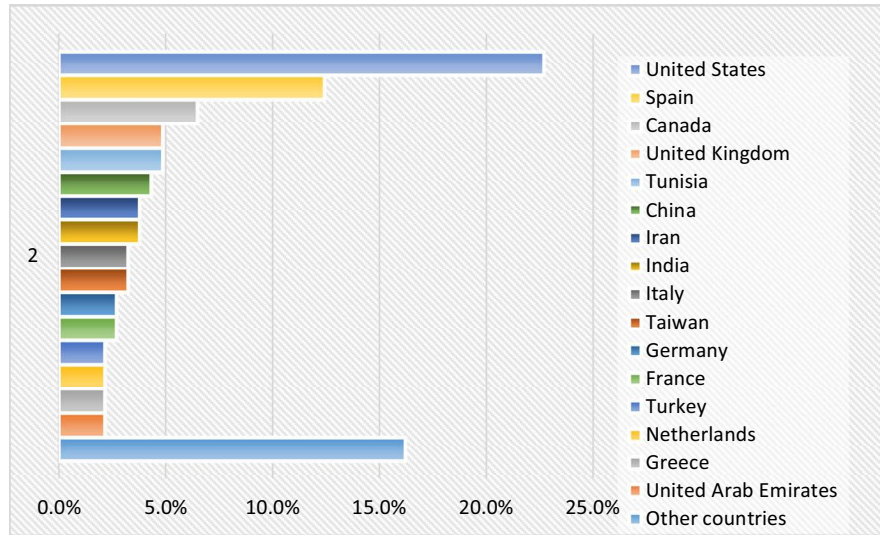


Fig. 2 Distribution by country

308 data confirm the key role played by European universities in this community and
 309 reflect the location of the top authors.

310 Moving to technical issues related to different GP variants, we noticed that the
 311 majority of papers using GP model for portfolio selection and portfolio management
 312 are using other variants of GP rather than its standard formulation. Moreover, 31.6%
 313 of the papers are using nonlinear GP, interactive GP and CP. Since 2000, fuzzy
 314 techniques are getting more and more popular and they account for 17.4% of the
 315 papers, whilst SGP is the most recent but the less used model (7.7%) in financial
 316 portfolio selection. The WGP variant is still quite popular (18.1%) over the years.
 317 LGP (11.0%) and PGP (14.2%) have been used in a limited manner over the
 318 decades. Table 2 shows the most commonly used models for each application area.
 319 These categories were developed in response to the papers that we found. The first
 320 categories refer to the specific type of securities (e.g. Bank portfolio, Dual-Purpose
 321 Funds or SRI). The other categories refer to the different aspects of investment
 322 decision (investment analysis, portfolio formation and portfolio management) or to
 323 the employed mathematical technique (mathematical modeling or optimization).

324 A wide variety of techniques are utilized in all different areas. Most works deal
 325 with portfolio selection and portfolio management, and the more innovative models
 326 are concentrated in these two area. A recent area of application concerns socially
 327 responsible investment (SRI): in recent years, sustainable development and social
 328 responsibility have become important issues around the globe, thus investment

Table 2 GP variants by application area^a

GP models	Asset liability management	Bank portfolio	Dual-purpose funds	Equity mutual funds	SRI	Stock market	Financial planning	Portfolio analysis	Portfolio selection	Portfolio management	Portfolio modelling	Portfolio optimization	Other	Total
WGP	2	2	3	3	3	2	2	10	3	3	2	2	27	
LGP	1	1	2	3	1	1	6	2	1	1	1	1	17	
PGP	2	1	1				3	9	2	2	5	5	22	
SGP								9	3	3			12	
FGP				1	2	1	1	18	4	4		1	27	
Other GP	1	2		1	2	3	2	22	5	2	6	2	49	
Total	5	6	2	8	7	3	6	74	19	3	11	6	154	

^a Two papers present more GP variants



329 strategy employs criteria (based on social, environmental and ethical screens²) other
330 than financial risk and return when selecting firms in which to invest.

331 Another interesting aspect to explore is about the area and the journals publishing
332 papers related to the application of GP to portfolio selection that may help to better
333 understand the GP community active in this research field. The top journals are in
334 the Operation Research area, namely: European Journal of Operational Research
335 (11.5%), INFOR (6.9%), Journal of the Operational Research Society (4.6%), and
336 Annals of Operations Research (3.8%). It seems that operational researchers tend to
337 publish their results in OR journals rather than address specialized journals in
338 Finance or Management. We also have some management journals, such as
339 Decision Sciences, Journal of Banking and Finance, and Omega (3.8% each). All
340 application areas are represented in the journals (Table 3).

341 Table 4 shows the classification of GP variants based on the type of information
342 related to the parameters of the decision-making situation. We noticed that the GP
343 model is largely applied in deterministic contexts. More recently, we count some
344 applications related to stochastic and fuzzy decision-making contexts.

345 5 Concluding remarks

346 The aim of this paper is to provide a categorization of the applications of different
347 GP variants for financial portfolio selection and portfolio management according to
348 different characteristics (ranging from the type of information related to the
349 decision-making situation to the application area or the demographic variables
350 across the last decades). The performed literature review shows that the number of
351 papers related to this subject has increased steadily especially over the past two
352 decades, and this trend is expected to continue as the applicability of GP technique
353 in financial portfolio management is fully recognized by researchers worldwide,
354 with a focus in the European area, and in the developed countries in general. With
355 regard to publication outlets, it seems that over the years most academicians have
356 preferred to publish in top journals in operation research. This is due to an
357 increasing use of more sophisticated models (SGP and FGP models) able to provide
358 a more complete representation of complexity, or at least a more complete
359 understanding of the real world (see Table 4).

360 We also notice that researchers within the field of Management Science and
361 Operations Research are very active in applying the GP model to portfolio selection
362 that was traditionally related to the field of Finance. The rapid increase in using GP
363 model can be explained by the fact that it is an easy tool to be understood and
364 implemented, and it is supported by commercial optimization software. Moreover,
365 the GP model is more flexible than the other MCDA techniques. It is a learning
366 process in which the FDM can interact and continuously adjust the parameters in
367 order to improve the decision-making process through a progressive and evolving

2FL01 ² The environment concern includes climate change and clean technologies or pollution. Under the social
2FL02 concerns we can look at human rights and labor relations for instance. Ethical or governance concerns
2FL03 relate to board issues. Popular negative screens refer to the sin screens (production of alcohol, tobacco or
2FL04 gambling products) or military weapons, just to mention a few.

Table 3 Classification by journal

GP models	ANOR	Applications of management science	Applied mathematics and computation	Applied soft computing journal	Computers and industrial engineering	Decision sciences	EJOR	Expert systems with applications	Financial systems with applications	Financial Markets and portfolio management	Fuzzy optimization and decision making	INFOR	Information sciences
WGP	1		1			4					1		
LGP						2	2						
PGP						2	2	2	2				
FGP	1	1	1			1	2	2	1	1	1	2	2
SGP	1					1	1				4		
Other GP	2	1	4		2	2	6	1	1	1	3	1	
Total	5	2	4	2	2	5	15	3	2	2	9	3	2
GP models	IRJFE	ITOR	Journal of banking and finance	Journal of multicriteria decision analysis	JORS	LNEMS	Management science	Omega	Conference paper	WP	Book and chapter	Total	
WGP			1	1	3	1	2	1		1	11	26	
LGP	2									1	10	16	
PGP	3					1	1	4	1	1	8	22	
FGP				2				3			8	26	
SGP	1	1						2			2	11	
Other GP	2		3	3	1	2	1	1	2	5	10	48	
Total	3	5	2	6	3	2	5	9	3	5	38	151	

Table 4 Information type and GP model in portfolio management^a

	1970s	1980s	1990s	2000s	2010s	Total
Deterministic	10	17	12	27	26	92
WGP	2	5	5	6	8	26
LGP	6	5	1	1	4	17
PGP		1	3	11	7	22
Other GP	2	6	3	9	7	27
Fuzzy		1	1	12	20	34
WGP					2	2
FGP		1	1	8	16	26
Other GP				4	2	6
Stochastic		1	2	13	16	29
FGP					1	1
SGP				4	8	11
Other GP		1	2	6	7	16
Grand total	10	19	15	49	62	155

^a Two papers present more GP variants

368 sequence of actions. The investment decisions are taken by the FDM and the GP
 369 model is a tool to support and not to replace humans' decisions. The GP model
 370 allows the FDM to express his/her preferences based on his/her intuition, experience
 371 and knowledge. In addition, the behavior of the financial portfolio management
 372 depends on several external factors that are difficult to control and to predict during
 373 the modeling process. These factors are related to: (a) international economy;
 374 (b) national economy; (c) international political stability; (d) natural phenomena;
 375 and (e) the FDM psychology. Future avenues in GP theory and modeling include the
 376 formulation of more complex GP variants that will also try to model the effect of
 377 external factors as well as the subjectivity nature of the financial decision making
 378 process. In this perspective a more intense collaboration between academic
 379 researchers and industry practitioners will be beneficial.

380 Appendix

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