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# ATTI

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A cura di F. Conti e S. Vallergera

A STUDY ON THE PHASE DIAGRAMS OF TWO-COMPONENT PHOSPHOLIPID BILAYERS; PHOSPHATIDYLCHOLINE (PC)/ PHOSPHATIDYLETHANOLAMINE (PE) MIXTURES.

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Abstract - To calculate the phase diagrams of PC/PE mixtures, a generalization of the Priest (1) phenomenological model has been used. A new excess free energy term in the state function has been proposed to consider the two-component phospholipid bilayers where both the chain lengths and the polar heads of the components can be different.

With this proposed state function, the phase diagrams of different experimentally studied PC/PE mixtures have been constructed. Complete miscibility was obtained when the components had the same chain length.  $L_E > L_C$  gave a peritectic system while for  $L_E < L_C$  an eutectic system was originated.

Experimental data from different sources were compared to the theoretical calculations.

Introduction - The lipid composition of biological membranes is complex. This could be connected with the necessity to provide the correct micro-environment for the membrane-bound proteins.

At the moment little is known about the physiological meaning of the different head groups of the phospholipids and their mixing behaviour.

Considering that the phase properties and the function of the lipid membranes are directly related, we have developed a model to study the phase transition properties of a two-component system where both the chain length and the polar heads of the components can be different. Based on Landau phenomenological theory (2) of phase transition, a simple model for binary mixtures of lecithin (PC) homologues, when the lipid components have the same head

group but the chain lengths are different, has been developed by Priest (1). The model contains only two parameters which can be fitted independently.

Starting from this model we have determined the parameters for one component bilayers of PE homologues and taking into consideration the hydrogen bondings between the polar heads of PE molecules, a new excess free energy term in the state function of binary mixtures was constructed.

Theory - The free energy function of PC/PE binary mixtures has been considered similar to that of two-component lecithin bilayers (eq. 18, Ref. 1). Thus,

$$\begin{aligned} \frac{G(X_E, S)}{2RT} = & X_E \frac{F_E(S)}{RT} + (1-X_E) \frac{F_C(S)}{RT} + \\ & + \frac{1}{2} X_E \ln X_E + \frac{1}{2} (1-X_E) \ln(1-X_E) + \\ & + \Delta U \cdot X_E + \frac{(\sigma |\Delta L| + \gamma)}{RT} \left( \frac{1}{2} - S \right) X_E \cdot \\ & \cdot (1 - X_E) \end{aligned} \quad - 1 -$$

where  $\Delta L = L_E - L_C$  and  $X_E$  is the mole fraction of PE component. The first two terms represent the free energy functions of one-component PE and PC bilayers respectively (3) while the third and fourth terms are the entropy of mixing. The difference in chemical potential ( $\Delta U$ ) between the two components of the mixture is also considered and the last term account for the experimental fact that PC/PE mixtures of same length components are not ideal ones, i.e. the excess free energy does not vanish when  $\Delta L = 0$ .

As it has been previously shown (3), the excess free energy reflects the difference of the nearest neighbour interaction energies between the same and different components.

$c|z|$  ( $1/2 - S$ ) and  $\gamma$  ( $1/2 - S$ ) represent the interaction energy differences as a consequence of the different chain lengths and that of the different polar heads respectively.

**Results and discussion.** - The model parameter values employed in the calculations of the phase diagrams are collected in TAB.1. Those concerning PE homologues were determined with the same procedure used by Priest (1) for lecithin molecules. By means of the state function  $-L$ , the phase diagrams of different PC/PE mixtures have been determined. To obtain the points of the solidus and liquidus curves at a given temperature, one has to find out the value or the values of  $\Delta U$  where two or three minima of the state function become global ones and  $X_E$  values belonging to these minima determine the points of the phase diagram.

When  $L_E = L_C$  there are two minima. The first is the PE rich gel minimum at large  $X_E$  value and  $S = 0$ , the second is the PC rich liquid crystalline minimum at a smaller value of the mole fraction. The phase diagrams of DMPC/DMPE and DPPC/DPPE mixtures are represented in Fig. 1 and Fig. 2 respectively.

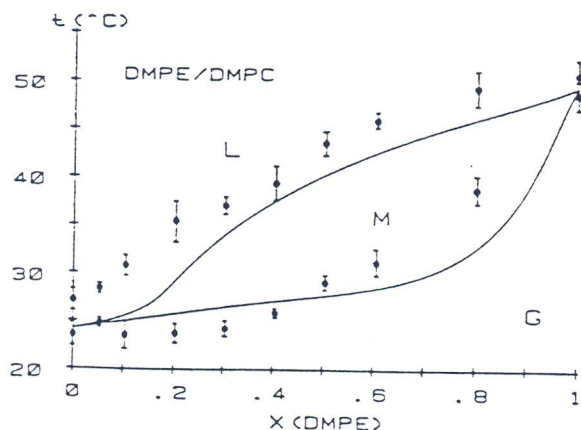


Fig. 1 - Calculated phase diagram of binary mixtures of DMPC and DMPE. DSC experimental data (5)

The upper curves of phase diagrams are the liquidus and the lower ones are the solidus lines. The liquid crystalline phase

is above the liquidus curve while the gel phase is below the solidus line. Between these two lines PC rich liquid crystalline phase coexists in equilibrium with the PE rich gel phase; this is the mixed phase region.

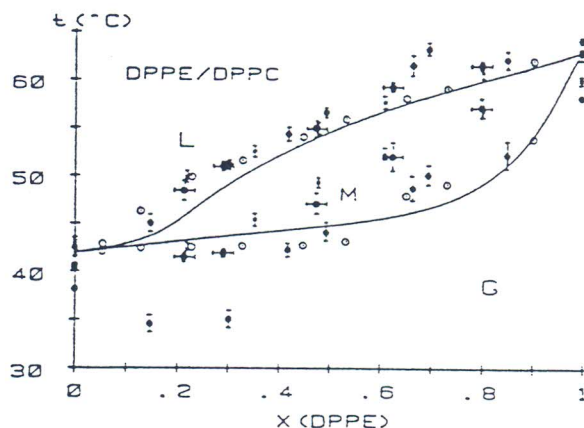


Fig. 2 - DPPC/DPPE mixture phase diagram. Solid curves are the model results. Experimental data: DSC, (6, 7); ESR, (8); fluorescence, (9).

A more complex situation is obtained when  $L_E > L_C$ . In the  $(X_E, G)$  plane local minima are three: a liquid crystalline, a PC rich gel and a PE rich gel minimum. At P (in Fig. 3 for DMPC/DPPE mixture) all three phases coexist in equilibrium. In the MG (mixed gel) region the two gel phases coexist in equilibrium.

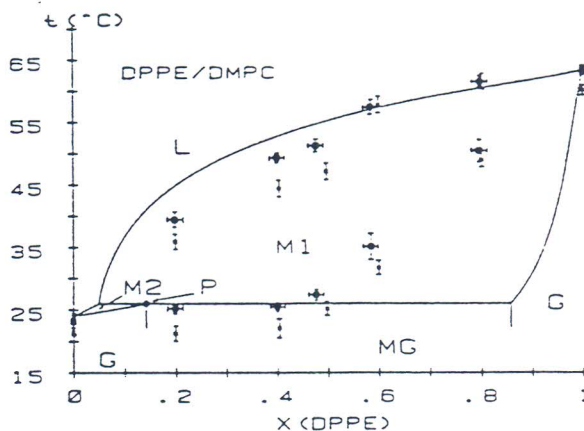


Fig. 3 - Phase diagram for DMPC/DPPE mixture. Experimental data: ESR, (10); fluorescence, (11).

In the M1 region a PC rich liquid crystalline phase coexists with a PE rich gel phase while in M2 a PC rich crystalline



phase coexists with a PC rich gel phase. Also in the cases where  $L_E < L_C$  there are three important local minima. The phase diagrams of DPPC/DMPE and DSPC/DMPE mixtures are represented in Fig. 4 and 5 respectively.

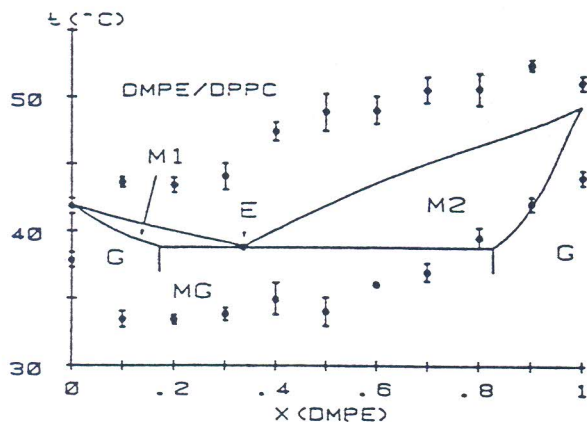


Fig. 4 - Phase diagram for the binary mixture DPPC/DMPE. DSC experimental data (4).

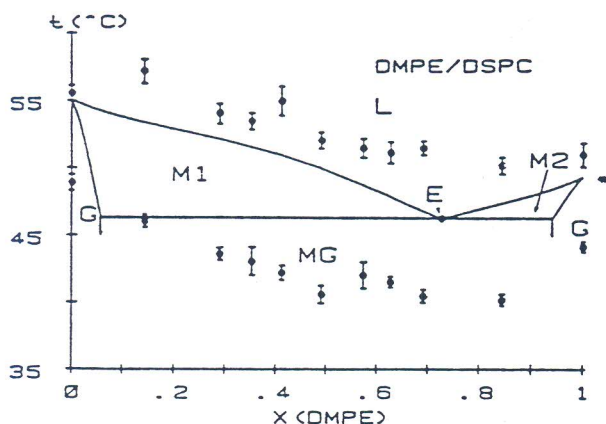


Fig. 5 - Phase diagram for the binary mixture DSPC/DMPE. DSC experimental data (4)

These systems are eutectic mixtures as was also concluded by Blume and Ackermann (4) analyzing their calorimetric data. The obtained results indicate that, depending on the chain length differences, three types of PC/PE mixed systems can be differentiated as summarized in Tab. II. The calculated liquidus curves fit quite well the available experimental data. For the solidus curves the agreement is good only for calorimetric data.

Table I. Model parameter values for phosphatidylcholine and phosphatidylethanolamine homologues.

Pi	Z <sub>1</sub> /R	W <sub>1</sub> /R	σ/R	γ/R
	°K	°K	°K	°K
PC	-275.1	-1085	125	0
PE	-188.5	-1117.8	125	500

Table II

L <sub>C</sub>	L <sub>E</sub>	Mixtures	Results
14	14	DMPC/DMPE	complete miscibility
16	16	DPPC/DPPE	complete miscibility
14	16	DMPC/DPPE	peritectic system
16	14	DPPC/DMPE	eutectic system
18	14	DSPC/DMPE	eutectic system

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Abbreviations: DPPC, L-α-dipalmitoylphosphatidylcholine; DMPC, L-α-dimyristoylphosphatidylcholine; DSPC, L-α-distearoylphosphatidylcholine; DPPE, L-α-dipalmitoylphosphatidylethanolamine; DMPE, L-α-dimyristoylphosphatidylethanolamine.