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Core-proton coupled nature of the $11/2^+$ state in ^{131}Sb probed by lifetime measurements

S. Bottoni^{1,2}, E. R. Gamba^{1,2}, G. De Gregorio^{3,4}, A. Gargano⁴,
 S. Leoni^{1,2}, B. Fornal⁵, N. Brancadori¹, G. Ciconali^{1,2},
 F. C. L. Crespi^{1,2}, N. Cieplicka-Oryńczak⁵,
 L. W. Iskra⁵, G. Colombi^{1,2,6}, Y.H. Kim^{6,†}, U. Köster⁶,
 C. Michelagnoli⁶, F. Dunkel⁷, A. Esmaylzadeh⁷, L. Gerhard⁷,
 J. Jolie⁷, L. Knafla⁷, M. Ley⁷, J.-M. Régis⁷, K. Schomaker⁷,
 M. Sferrazza⁸

¹Dipartimento di Fisica, Università degli Studi di Milano, 20133 Milano, Italy

²INFN Sezione di Milano, 20133, Milano, Italy

³Dipartimento di Matematica e Fisica, Università degli Studi della Campania “Luigi Vanvitelli,” 81100 Caserta, Italy

⁴INFN Sezione di Napoli, 80126, Napoli, Italy

⁵Institute of Nuclear Physics, PAN, 31-342 Kraków, Poland

⁶Institut Laue-Langevin, 38042 Grenoble, France

⁷Universität zu Köln, Institut für Kernphysik, 50937 Köln, Germany

⁸Département de Physique, Université libre de Bruxelles, 1050 Bruxelles, Belgium

E-mail: simone.bottoni@mi.infn.it

Abstract. The structure of the $11/2_1^+$ state in ^{131}Sb was investigated at the LOHENGRIN spectrometer of Institut Laue-Langevin via neutron-induced fission of ^{235}U and lifetime measurements, yielding $T_{1/2}=3(2)$ ps, at the edge of the sensitivity of the experimental method. This first result for the $11/2_1^+$ state half-life in neutron-rich Sb isotopes provides a quadrupole reduced transition probability to the ground state of $B(E2)=1.4_{-0.6}^{+1.5}$ W.u., very close to the $B(E2;2_1^+ \rightarrow 0_1^+)$ in ^{130}Sn . Realistic shell-model calculations reproduce well both the experimental level scheme of ^{131}Sb and the $B(E2;11/2_1^+ \rightarrow 7/2_1^+)$ value, indicating a dominant $2^+(\text{}^{130}\text{Sn}) \otimes \pi g_{7/2}$, core-proton coupled configuration for the $11/2_1^+$ state.

1. Introduction

The energies of the $11/2_1^+$ states in neutron-rich Sb isotopes are almost the same of the 2^+ states in the underlying Sn nuclei [1]. This may suggest that the $11/2_1^+$ state could be interpreted in terms of core-proton coupling. In this scheme, one assumes that the low-lying spectrum of the odd-even system can be well described by coupling the odd nucleon in the lowest allowed orbital to the ground and the 2^+ states of the neighboring even-even core. Particle- and hole-core coupled states around closed shells are of particular interest for nuclear structure, as reported, for example, in Refs. [2] and [3], for Ca isotopes and the ^{133}Sb nucleus, respectively. In the so-called weak coupling limit, the extra particle does not perturb the core and the total quadrupole strength of the multiplet obtained from the 2_1^+ state is conserved [4]. This simple description can

†Present address: Center for Exotic Nuclear Studies, Inst. for Basic Science, Daejeon 34126, Rep. of Korea



break down when particle-core correlations provide extra strength owing to the proton-neutron interaction. In this work, the structure of the $11/2_1^+$ state in ^{131}Sb was investigated by lifetime measurements using γ -ray spectroscopy techniques to probe its $2^+(^{130}\text{Sn}) \otimes \pi g_{7/2}$ core-proton coupled nature. The results are compared with realistic shell-model calculations performed in a large valance space.

2. The experiment

The experiment was performed at Insitutit Laue-Langevin (ILL) with the LOHENGRIN spectrometer [5]. The nuclei of interest were produced by thermal neutron-induced fission of a ^{235}U target. Fission fragments were selected with magnetic and electric fields, according to their A/q and E/q , mass-to-charge and energy-to-charge ratios, respectively. Finally, ions were collimated by a refocusing magnet [6] to the focal plane of the spectrometer, where their γ decay was measured by two HPGe clover detectors and four $\text{LaBr}_3(\text{Ce})$ scintillators. Considering a time of flight of about $2 \mu\text{s}$, only the γ decay from isomeric states can be detected.

In ^{131}Sb , three isomers are known, namely the $(23/2^+)$, $(19/2^-)$, and $(15/2^-)$ states at 2165.6 keV, 1687.2 keV, and 1676.1 keV, with half-lives of 0.97(3), 4.3(8) and $64(3) \mu\text{s}$, respectively [7, 1]. The $11/2_1^+$ state in ^{131}Sb is fed by the 450-keV transition depopulating the 64- μs isomer and decays to the ground state via a stretched E2 transition of 1126 keV, as shown in the left panel of Fig. 1. In the same picture, the level and decay scheme of ^{131}Sb measured in this experiment is displayed. The 450-1226-keV coincident spectrum is presented on the right panel of Fig. 1 for both HPGe and $\text{LaBr}_3(\text{Ce})$ detectors, showing the selectivity achieved in the present experiment. The lifetime of the $11/2_1^+$ state was measured by using the *generalized centroid difference* (GCD) method [8], applied to the 450-1226-keV, feeding-decay (E_f, E_d) cascade. The background contribution was evaluated with the method introduced in Ref. [9] and already used in Refs. [10, 11, 12]. The lifetime value was obtained by $2\tau = \Delta\text{C-PRD}(E_f, E_d)$, where ΔC is the centroid difference between the delayed (D) and antidelayed (AD) time distributions. The $\text{PRD}(E_f, E_d)$ correction is the so-called *prompt response difference*, which takes into account time-walk effects in $\text{LaBr}_3(\text{Ce})$ detectors [8].

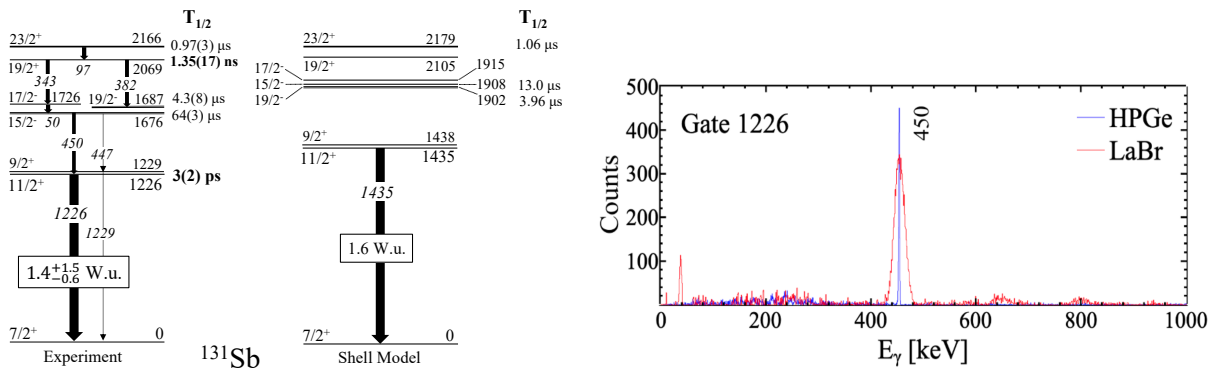


Figure 1. (Left) Experimental level and decay scheme of ^{131}Sb observed in the present experiment compared to shell-model calculations. Half lives measured in this work are highlighted in bold. The obtained $B(E2; 11/2_1^+ \rightarrow 7/2_1^+)$ value is also reported. (Right) Background-subtracted projected spectrum showing a clean coincidence between the 450-keV and 1226-keV γ rays, for both HPGe and $\text{LaBr}_3(\text{Ce})$ detectors.

The result for the lifetime of the $11/2_1^+$ state is $\tau=5(3) \text{ ps}$, which corresponds to $T_{1/2}=3(2) \text{ ps}$, at the limit of the sensitivity of the experimental method. Also the lifetime of the $19/2^+$ state at 2069 keV was measured in this work using the decay slope method, with gates applied on both

the $19/2^+ \rightarrow 17/2^-$ and $19/2^+ \rightarrow 19/2^-$ decaying transitions. The weighted average lifetime obtained from the separate analysis of the D and AD time distributions is $\tau = 1944(246)$ ps, corresponding to $T_{1/2} = 1347(171)$ ps. These results are reported in the left panel of Fig. 1.

3. Discussion

The measured lifetime of the $11/2^+$ state in ^{131}Sb enabled to assess the electric-quadrupole reduced transition probability to the ground state, providing $B(E2; 11/2_1^+ \rightarrow 7/2_1^+) = 1.4_{-0.6}^{+1.5}$ W.u., indicating a non-collective nature of this state. This result is very close to the measured $B(E2; 2_1^+ \rightarrow 0_1^+) = 1.18(26)$ W.u of the ^{130}Sn nucleus [13], suggesting that the extra proton does not perturb the Sn core. As a matter of fact, the $11/2^+$ state is expected to be a member of the $2^+(^{130}\text{Sn}) \otimes \pi g_{7/2}$ multiplet, corresponding to the maximum spin alignment.

Experimental data are compared with realistic shell-model calculations performed with the KSHELL code [14]. An inert ^{100}Sn core was considered, with a valence space composed by the $0g_{7/2}$, $1d_{5/2}$, $1d_{3/2}$, $2s_{1/2}$ and $0h_{11/2}$ orbitals for both protons and neutrons. In this framework, the two-body effective interaction was derived with many-body perturbation theory from the CD-Bonn nucleon-nucleon potential [15] renormalized by way of the $V_{\text{low-k}}$ approach [16] with the addition of the Coulomb potential. The \hat{Q} - box folded-diagram approach [17] was adopted, including one and two-body diagrams up to the third order. Effective charges are chosen to be $e_p = 1.7e$ and $e_n = 0.67e$, in order to reproduce the experimental $B(E2; 2_1^+ \rightarrow 0_1^+) = 31.5(1.0)$ and $1.18(26)$ W.u. of ^{134}Te and ^{130}Sn , respectively. The calculated energies and wave-function components of low-lying state in ^{131}Sb are shown in Tab. 1.

Table 1. Calculated energies and wave-function structure of low-lying states in ^{131}Sb in terms of $^{130}\text{Sn} \otimes \pi(lj)$. Only components ≥ 0.02 are reported.

j^π	E [MeV]	$0_1^+ \otimes g_{7/2}$	$2_1^+ \otimes g_{7/2}$	$2_2^+ \otimes g_{7/2}$	$4_1^+ \otimes g_{7/2}$	$0_1^+ \otimes d_{3/2}$	$0_1^+ \otimes d_{5/2}$	$2_1^+ \otimes d_{5/2}$
$7/2_1^+$	0.0	0.91	0.06	-	-	-	-	-
$5/2_1^+$	0.942	-	0.03	-	-	-	0.90	0.03
$5/2_2^+$	1.359	-	0.91	-	-	-	0.02	0.02
$3/2_1^+$	1.381	0.79	-	-	0.20	-	-	-
$11/2_1^+$	1.435	-	0.88	-	0.08	-	-	-
$9/2_1^+$	1.438	-	0.73	-	0.13	-	-	-
$7/2_2^+$	1.696	0.03	0.55	0.11	0.24	-	-	-

First of all, we note that a good agreement is found in terms of spin-parity sequences and energies, compared to the experimental level scheme shown in Fig. 1. The theoretical level scheme of ^{131}Sb is also shown in Fig. 1. Moreover, the calculated wave function of the $11/2_1^+$ state is dominated by the $2^+(^{130}\text{Sn}) \otimes \pi g_{7/2}$ configuration (88%) and the predicted $B(E2; 11/2_1^+ \rightarrow 7/2_1^+) = 1.6$ W.u. results to be in perfect agreement with the experimental value of $1.4_{-0.6}^{+1.5}$ W.u. obtained in this work. Overall, both the experimental result and realistic shell-model calculations point to a good description of the $11/2_1^+$ state in ^{131}Sb in terms of proton-core coupling.

It is interesting to compare this finding with the results for the neighbouring ^{129}Sb nucleus [18]. In this case, a larger fragmentation of the wave function is predicted, with a 78% coming from the $2^+(^{128}\text{Sn}) \otimes \pi g_{7/2}$ coupling. On top of this, a $B(E2; 11/2_1^+ \rightarrow 7/2_1^+)$ value of 7.5(5) W.u. is reported, which exceeds the $B(E2; 2_1^+ \rightarrow 0_1^+) = 4.2(3)$ W.u of the ^{128}Sn core [19]. This enhancement is partially predicted by shell-model calculations, with a calculated $B(E2; 11/2_1^+ \rightarrow 7/2_1^+)$ of 5.1 W.u. which can be ascribed to a constructive interference of the

proton-neutron term in the quadrupole strength. In the case of ^{131}Sb , the latter is found to be smaller and of the same order of magnitude of the proton term. Finally, we note that also the $15/2_1^+$ states in both ^{131}Sb and ^{129}Sb were calculated within the same shell-model framework. Their wave functions were found to be dominated by the $4^+(^4\text{Sn}) \otimes \pi g_{7/2}$ component (85% and 80%, respectively), indicating that the core-proton coupling scheme can be extended also to higher-spin states along the Sb isotopic chain.

4. Conclusions

In conclusion, the lifetime of the $11/2^+$ state in ^{131}Sb was measured at the LOHENGRIN spectrometer of Institut Laue-Langevin, using neutron-induced fission of ^{235}U and the fast timing technique. A half-life of 3(2) ps was found, at the edge of the experimental method, which corresponds to a $B(E2; 11/2_1^+ \rightarrow 7/2_1^+) = 1.4_{-0.6}^{+1.5}$ W.u. for its stretched E2 decay. This result, along with the known $B(E2; 2_1^+ \rightarrow 0_1^+)$ value in ^{130}Sn and realistic shell model calculations, indicate an almost pure core-proton coupled structure for this state, dominated by the $2^+(^{130}\text{Sn}) \otimes \pi g_{7/2}$ configuration.

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